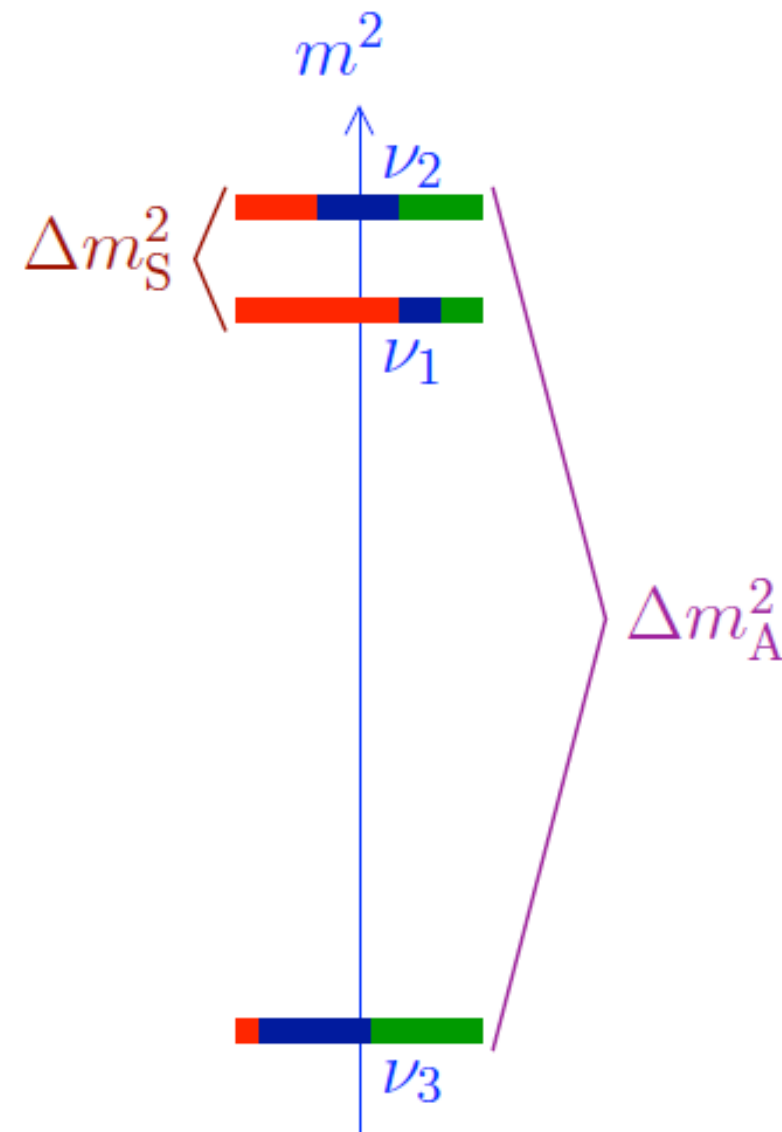
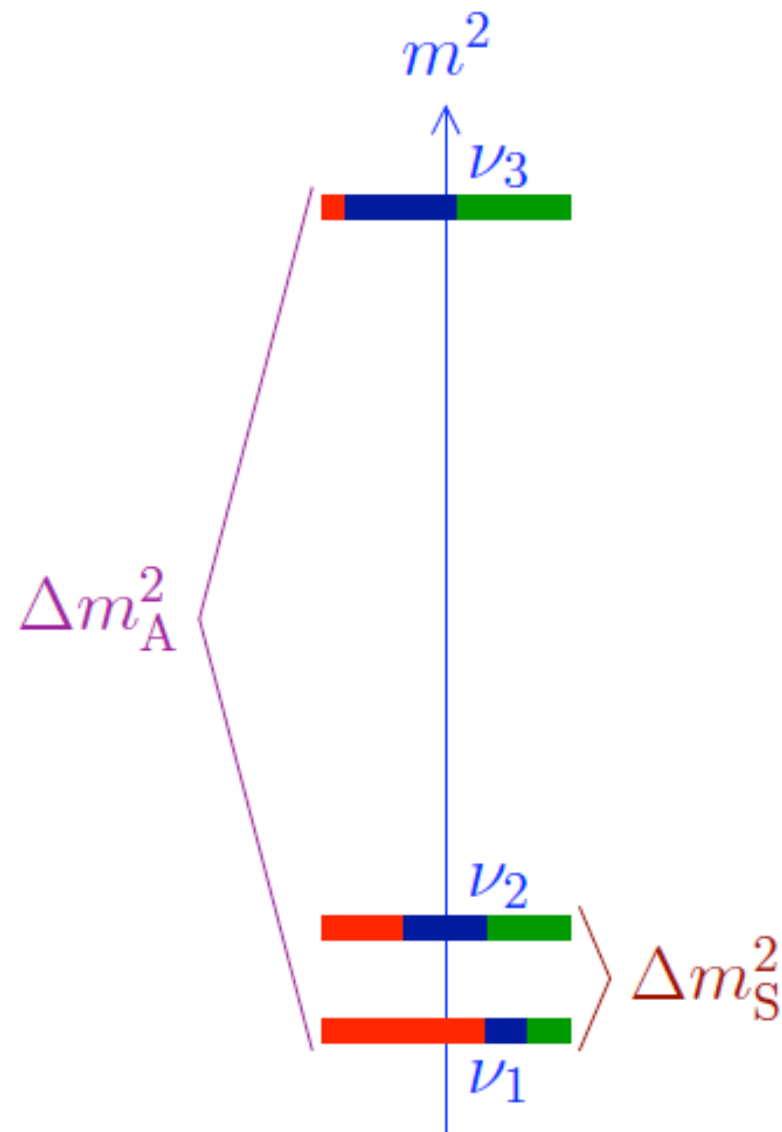


Lecture I: Direct measurement of neutrino masses

PhD Cycle XXXV

Three-Neutrino Mixing Paradigm

ν_e ν_μ ν_τ

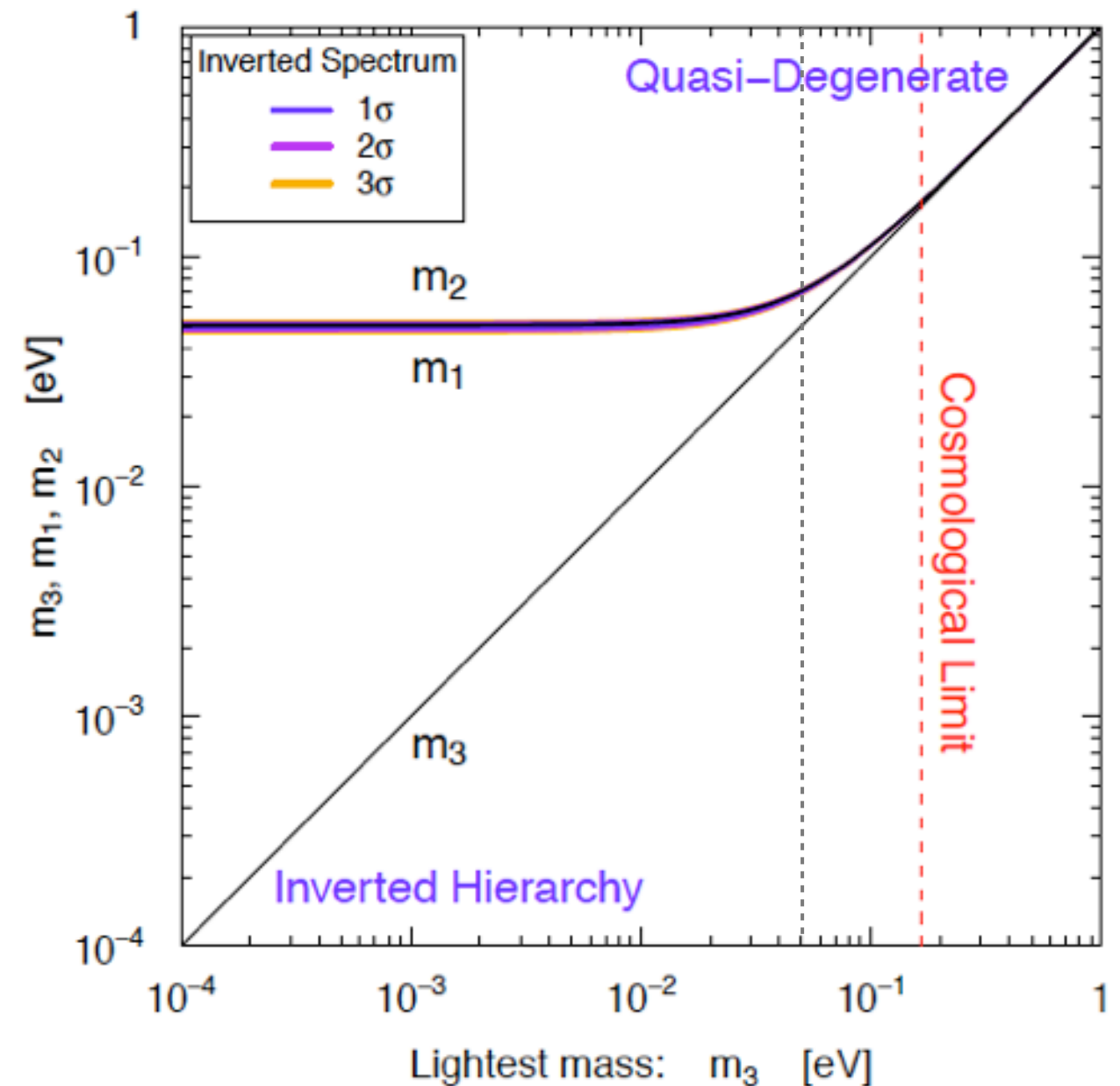
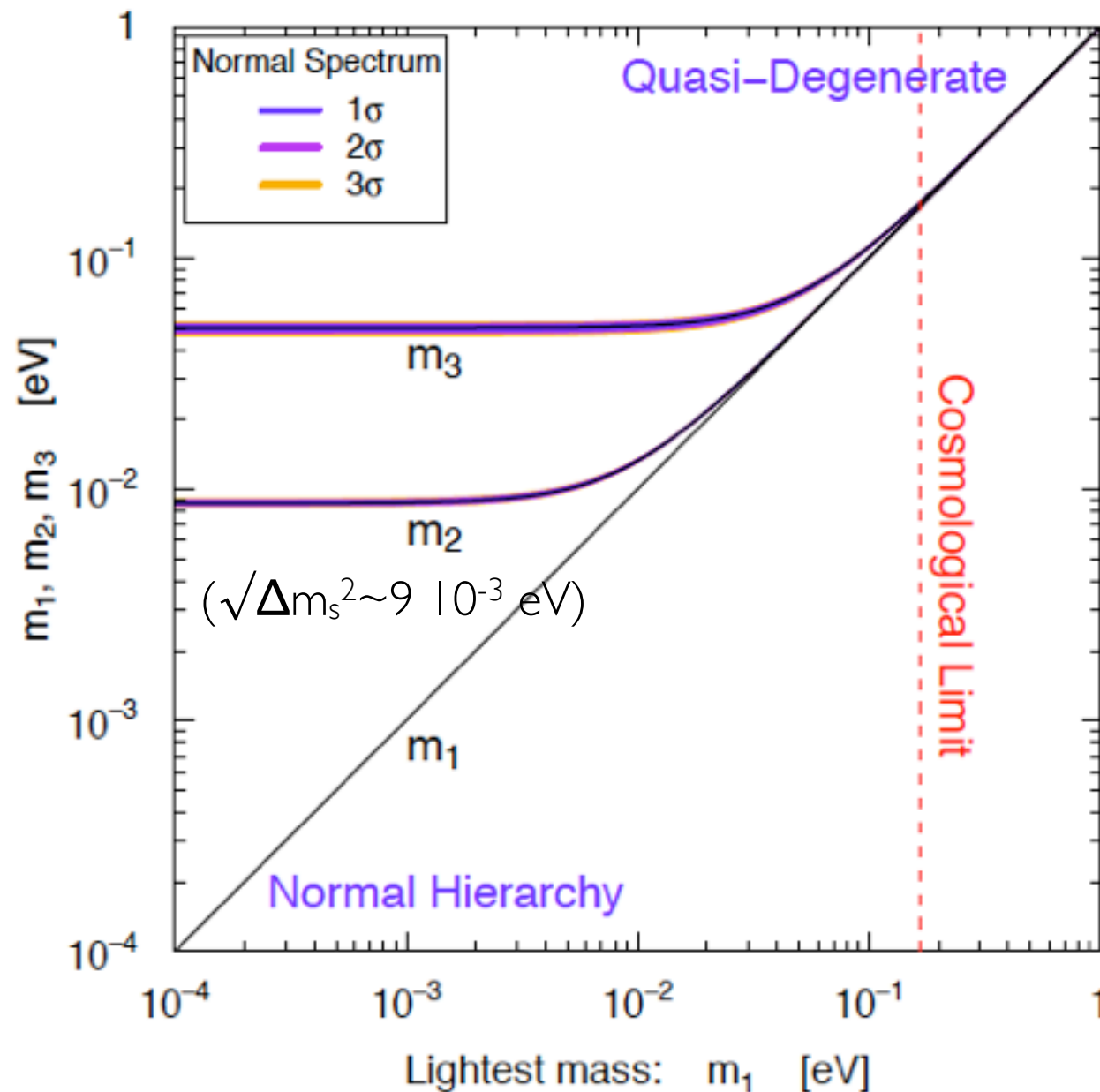


absolute scale is not determined by neutrino oscillation data

C. Giunti — Neutrino Mass: Overview of $\beta\beta_{0\nu}$, Cosmology and Direct Measurements

Parameter	best-fit
Δm_{21}^2 [10^{-5} eV ²]	7.37
$\Delta m_{31(23)}^2$ [10^{-3} eV ²]	2.56 (2.54)

Absolute Values of Neutrino Masses



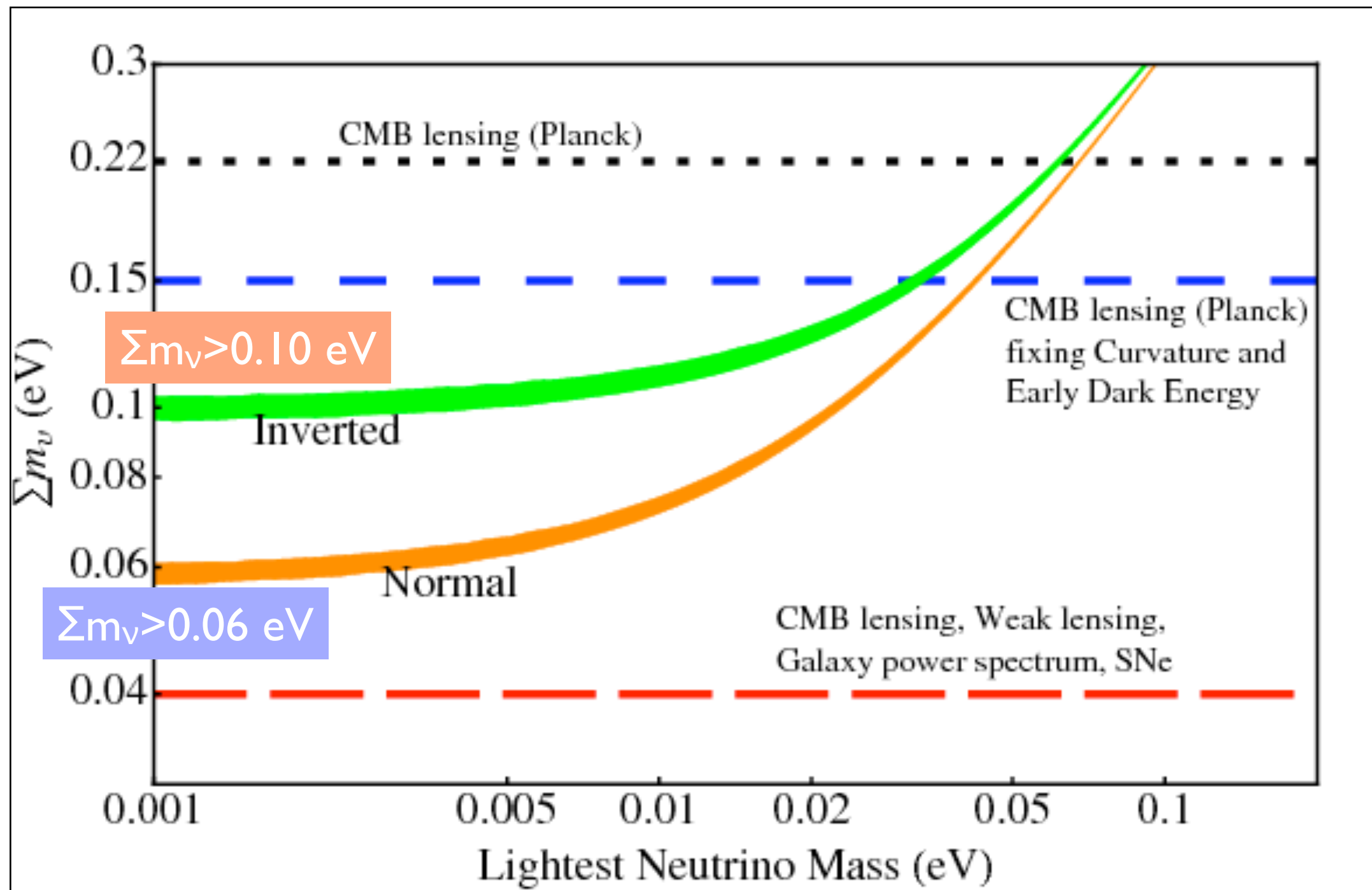
$$m_2^2 = m_1^2 + \Delta m_{21}^2 = m_1^2 + \Delta m_S^2$$

$$m_3^2 = m_1^2 + \Delta m_{31}^2 = m_1^2 + \Delta m_A^2$$

$$m_1^2 = m_3^2 - \Delta m_{31}^2 = m_3^2 + \Delta m_A^2$$

$$m_2^2 = m_1^2 + \Delta m_{21}^2 \simeq m_3^2 + \Delta m_A^2$$

Quasi-Degenerate for $m_1 \simeq m_2 \simeq m_3 \simeq m_\nu \gg \sqrt{\Delta m_A^2} \simeq 5 \times 10^{-2} \text{ eV}$



$$m_2^2 = m_1^2 + \Delta m_{21}^2 = m_1^2 + \Delta m_S^2$$

$$m_3^2 = m_1^2 + \Delta m_{31}^2 = m_1^2 + \Delta m_A^2$$

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$$m_2^2 = m_1^2 + \Delta m_{21}^2 \simeq m_3^2 + \Delta m_A^2$$

Parameter	best-fit
Δm_{21}^2 [10^{-5} eV ²]	7.37
$\Delta m_{31(23)}^2$ [10^{-3} eV ²]	2.56 (2.54)

Observables sensitive to m_ν

The absolute mass scale can be measured through:
(numbers on the right are current upper limits)

- tritium beta decay

$$m_\beta \equiv \left[\sum |U_{ei}|^2 m_i^2 \right]^{1/2} \quad (2.05 - 2.3 \text{ eV @ 95\%CL})$$

- neutrinoless double beta decay

$$m_{\beta\beta} \equiv \left| \sum U_{ei}^2 m_i \right| \quad (0.06 - 0.16 \text{ eV @ 90\%CL})$$

- cosmological observations

$$\sum m_\nu \equiv \sum_i m_i \quad (0.2 - 0.7 \text{ eV @ 95\%CL})$$

Observables sensitive to m_ν

The absolute mass scale can be measured through:
(numbers on the right are current upper limits)

- tritium beta decay

TODAY

$$m_\beta \equiv \left[\sum |U_{ei}|^2 m_i^2 \right]^{1/2} \quad (2.05 - 2.3 \text{ eV @ 95\%CL})$$

- neutrinoless double beta decay

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NOT HERE

Observables sensitive to m_ν

The absolute mass scale can be measured through:
(numbers on the right are current upper limits)

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- cosmological observations

$$\sum m_\nu \equiv \sum_i m_i \quad (0.2 - 0.7 \text{ eV @ 95\%CL})$$

LAST LECTURE

Direct mass measurements

Beta decay: direct ν_e mass

The most sensitive known method to measure the electron neutrino mass is by observing the electron spectrum in nuclear β -decay

$$\mathcal{N}(A, Z) \rightarrow \mathcal{N}(A, Z + 1) + e^- + \bar{\nu}_e, \quad (14.1)$$

where A and Z are, respectively, the mass and atomic numbers of the parent nucleus.

As we have seen in sections 6.1 and 6.2.1, the electron neutrino, in general, does not have a definite mass, but is a mixture of massive neutrinos. However, following the tradition, in this section we treat the electron neutrino as a mass eigenstate. We will discuss the effects of neutrino mixing in nuclear β -decay in section 14.1.1.

The differential decay rate in allowed⁷⁴ β -decays is given by

$$\frac{d\Gamma}{dE_e} = \frac{G_F^2 m_e^5}{2\pi^3} \cos^2 \theta_C |\mathcal{M}|^2 F(Z, E_e) E_e p_e E_\nu p_\nu, \quad (14.2)$$

where θ_C is the Cabibbo angle, \mathcal{M} is the nuclear matrix element, E_e (E_ν) and p_e (p_ν) are the electron (neutrino) energy and momentum, and $F(Z, E_e)$ is the Fermi

with the intermediate nucleus (with the surrounding electrons). The two factors $E_i p_i$ in eqn (14.2), with $i = e, \nu$, come from the phase-space factor of the final state: $d^3 p_i = p_i^2 dp_i d\cos\theta_i d\phi_i = p_i E_i dE_i d\cos\theta_i d\phi_i$, where θ_i and ϕ_i are the polar angular coordinates of \vec{p}_i .

massless. On the other hand, if the electron neutrino has a mass m_{ν_e} , the maximal kinetic energy of the electron is

$$T_{\max} = Q_{\beta} - m_{\nu_e} \quad (14.5)$$

Since the neutrino momentum is given by

$$p_{\nu} = \sqrt{E_{\nu}^2 - m_{\nu_e}^2} = \sqrt{(Q_{\beta} - T)^2 - m_{\nu_e}^2}, \quad (14.6)$$

the differential decay rate in eqn (14.2) can be written, for $T \leq T_{\max}$, as⁷⁵

$$\frac{d\Gamma}{dT} = \frac{G_F^2 m_e^5}{2\pi^3} \cos^2 \theta_C |\mathcal{M}|^2 F(Z, E_e) E_e p_e (Q_{\beta} - T) \sqrt{(Q_{\beta} - T)^2 - m_{\nu_e}^2}, \quad (14.8)$$

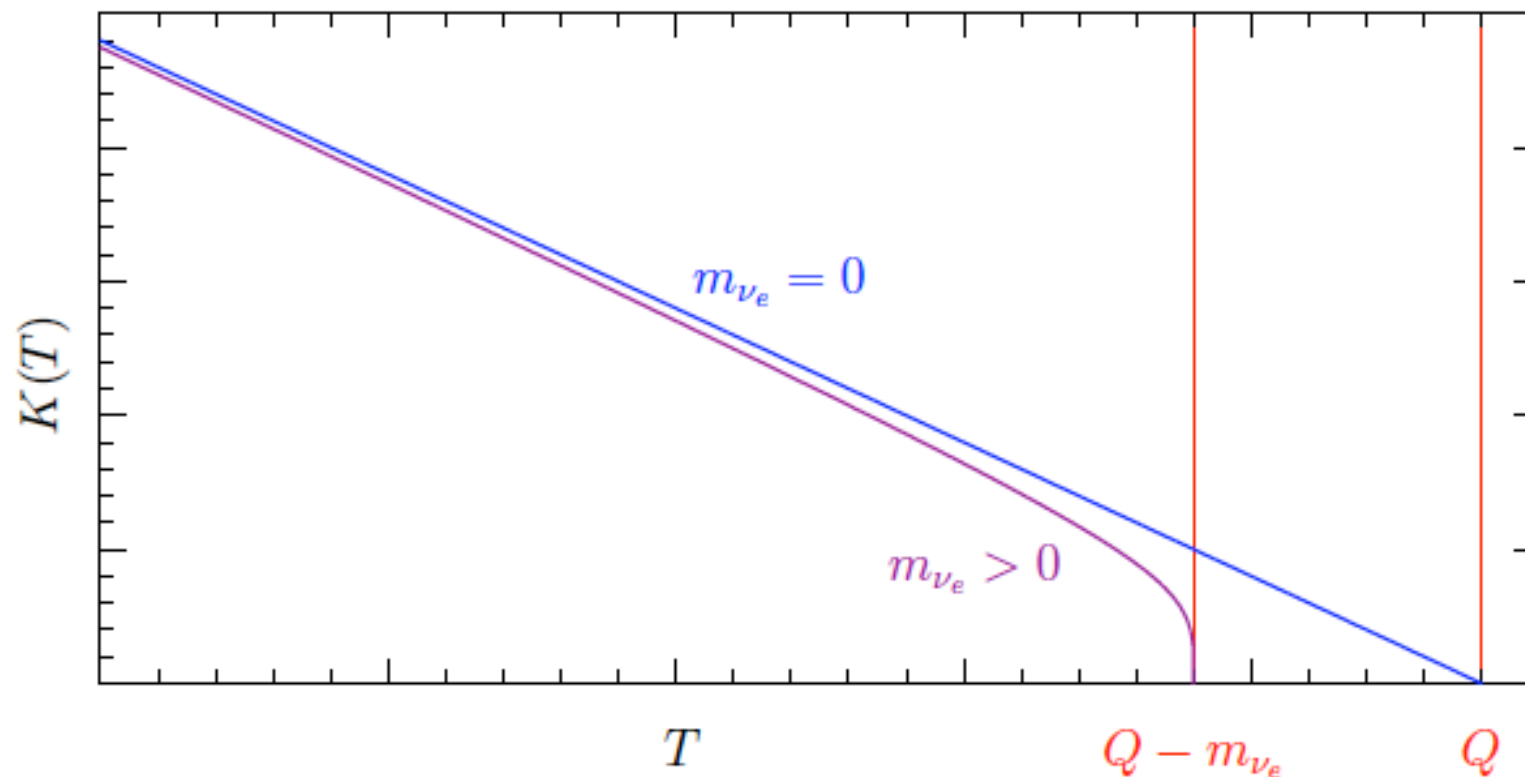
➡ What we measure:

Kurie plot

$$K(T) = \sqrt{\frac{\frac{d\Gamma}{dT}}{\frac{(\cos\theta_C G_F)^2}{2\pi^3} |\mathcal{M}|^2 F(E) pE}} = \left[(Q - T) \sqrt{(Q - T)^2 - m_{\nu_e}^2} \right]^{1/2}$$

Kurie plot

$$K(T) = \sqrt{\frac{\frac{d\Gamma/dT}{(\cos\vartheta_C G_F)^2} |\mathcal{M}|^2 F(E) pE}{2\pi^3}} = \left[(Q - T) \sqrt{(Q - T)^2 - m_{\nu_e}^2} \right]^{1/2}$$



$$m_{\nu_e} < 2.2 \text{ eV} \quad (95\% \text{ C.L.})$$

Mainz & Troitsk

[Weinheimer, hep-ex/0210050]

future: KATRIN

[www.katrin.kit.edu]

sensitivity: $m_{\nu_e} \simeq 0.2 \text{ eV}$

C. Giunti — Neutrino Mass: Overview of $\beta\beta_{0\nu}$, Cosmology and Direct Measurements — 14 May 2012 — 4/17

The mass is extracted from a fit to the end-point

Pros and cons

end-point of the electron spectrum is that very few events occur near the end-point. We can estimate the relative number of events occurring in an interval of energy ΔT below the end-point as follows. Below the end-point we have

$$T \simeq Q_\beta \quad \Rightarrow \quad \begin{cases} E_e \simeq Q_\beta + m_e \\ p_e = \sqrt{E_e^2 - m_e^2} \simeq \sqrt{Q_\beta (Q_\beta + 2m_e)}. \end{cases} \quad (14.9)$$

Ignoring the neutrino mass and the Fermi function, we have

$$\left. \frac{d\Gamma}{dT} \right|_{\substack{T \simeq Q_\beta \\ m_{\nu_e} = 0}} \propto (Q_\beta + m_e) \sqrt{Q_\beta (Q_\beta + 2m_e)} (Q_\beta - T)^2, \quad (14.10)$$

and

$$\int_{Q_\beta - \Delta T}^{Q_\beta} \frac{d\Gamma}{dT} dT \propto (Q_\beta + m_e) \sqrt{Q_\beta (Q_\beta + 2m_e)} (\Delta T)^3. \quad (14.11)$$

The total number of events is proportional to

$$\int_0^{Q_\beta} \frac{d\Gamma}{dT} dT \propto \int_0^{Q_\beta} (T + m_e) \sqrt{T (T + 2m_e)} (Q_\beta - T)^2 dT, \quad (14.12)$$

where we have neglected again the Fermi function and the neutrino mass. Since we are interested in an order-of-magnitude estimate, we consider $Q_\beta \gg m_e$, which leads to the approximation

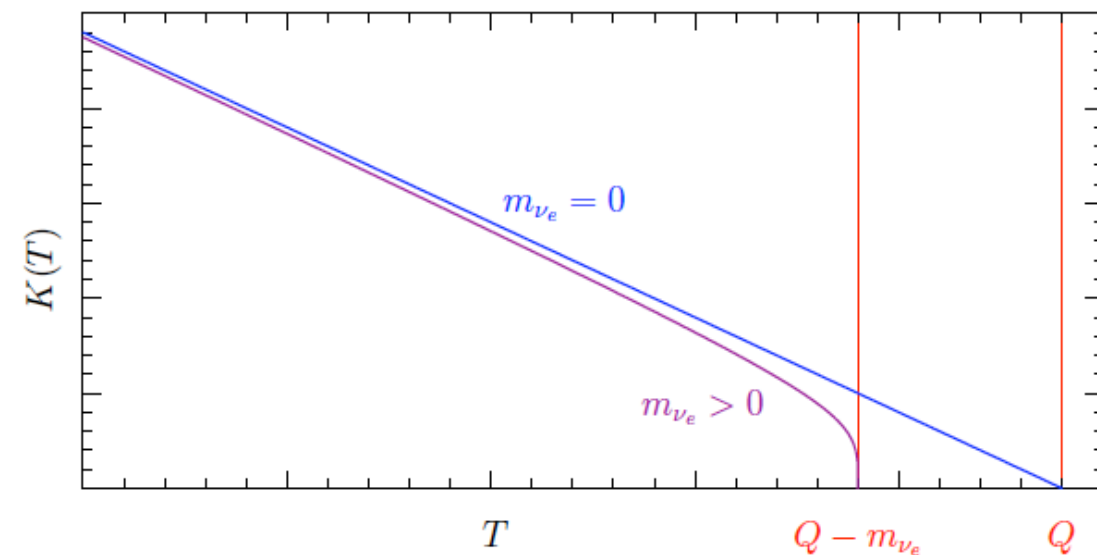
$$\int_0^{Q_\beta} \frac{d\Gamma}{dT} dT \propto Q_\beta^5. \quad (14.13)$$

Thus, the relative number of events occurring in an interval of energy ΔT below the end-point is given by

$$\frac{n(\Delta T)}{n} \propto \left(\frac{\Delta T}{Q_\beta} \right)^3. \quad (14.14)$$

One can obtain the same result considering $Q_\beta \ll m_e$. From eqn (14.14) it is clear that in order to maintain a constant relative error, ΔT must be proportional to Q_β .

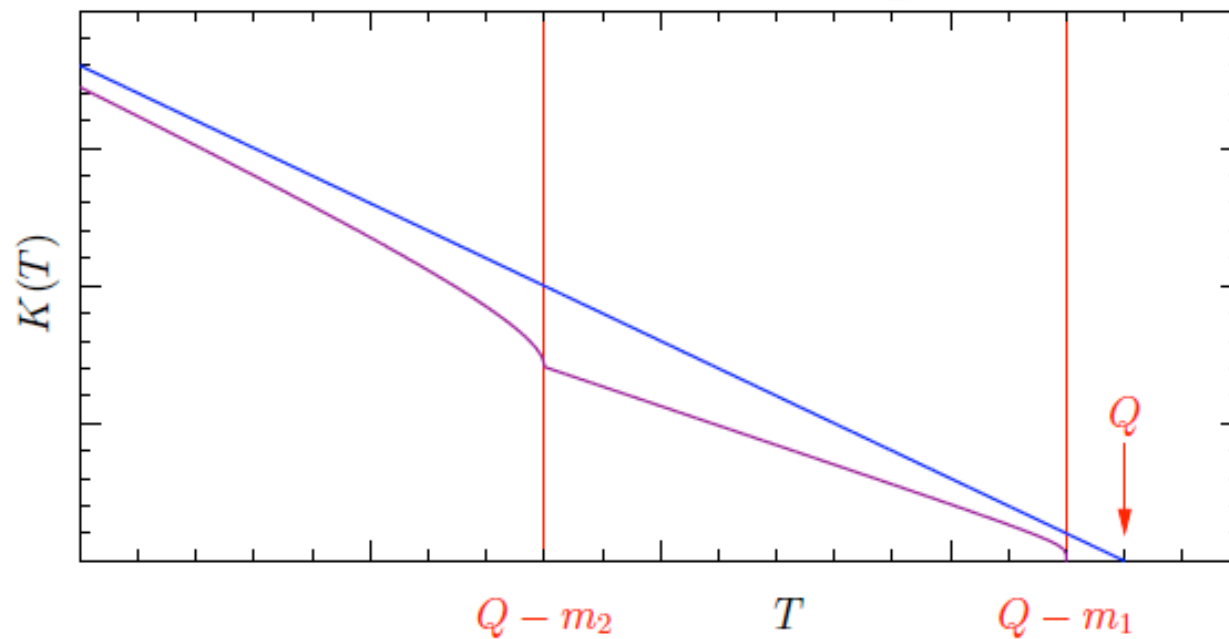
- + : This method relies **purely** on 3-body kinematics, without any assumption on the nature of the ν (e.g. Dirac/Majorana)
- : statistics, especially at the end point



The smaller the Q_β , the better for the relative stat error just below the end-point

Added complication: mix

Neutrino Mixing $\Rightarrow K(T) = \left[(Q - T) \sum_k |U_{ek}|^2 \sqrt{(Q - T)^2 - m_k^2} \right]^{1/2}$



analysis of data is
different from the
no-mixing case:

$2N - 1$ parameters

$$\left(\sum_k |U_{ek}|^2 = 1 \right)$$

if experiment is not sensitive to masses ($m_k \ll Q - T$)

effective mass: $m_\beta^2 = \sum_k |U_{ek}|^2 m_k^2$

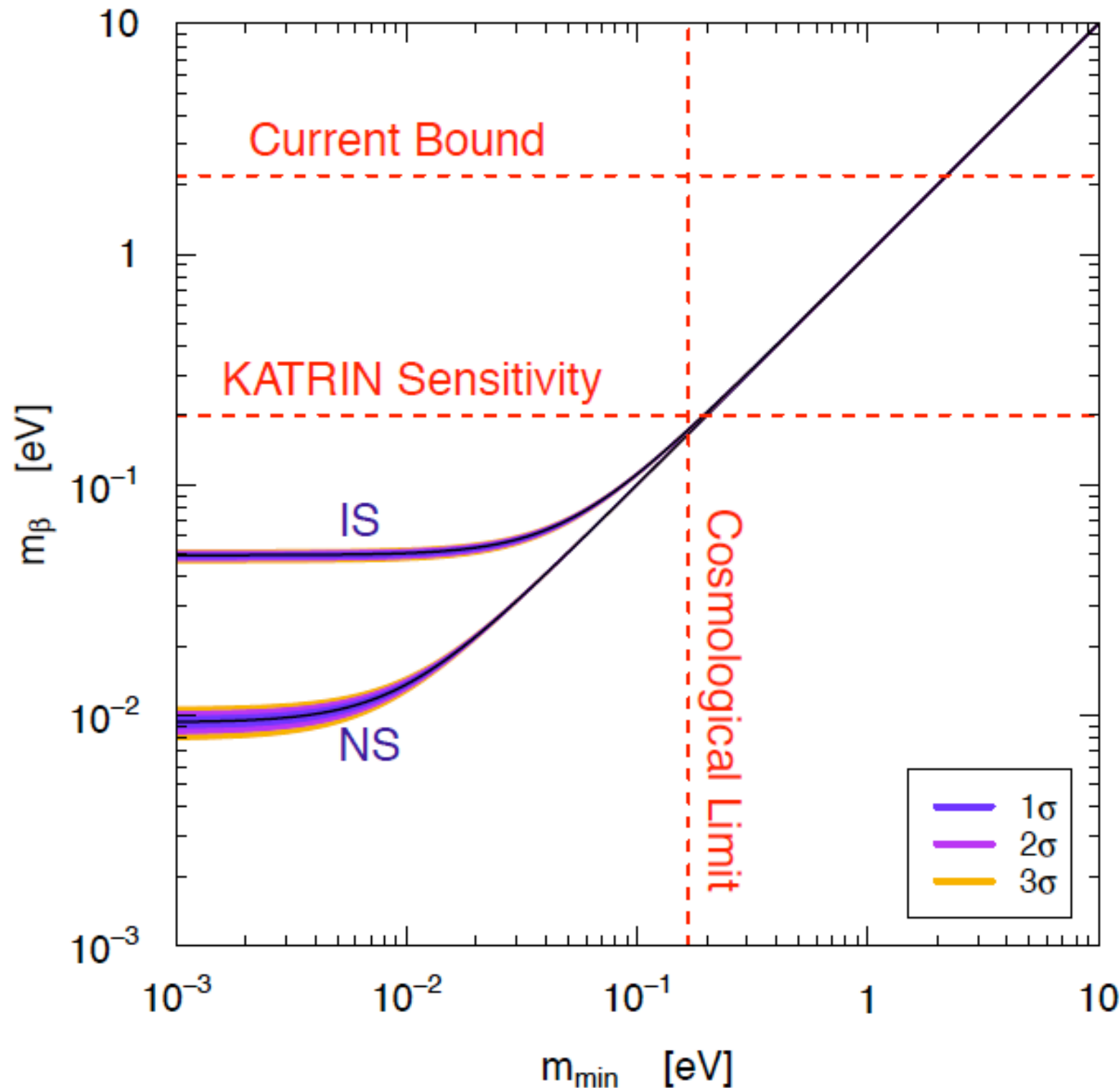
$$\begin{aligned} K^2 &= (Q - T)^2 \sum_k |U_{ek}|^2 \sqrt{1 - \frac{m_k^2}{(Q - T)^2}} \simeq (Q - T)^2 \sum_k |U_{ek}|^2 \left[1 - \frac{1}{2} \frac{m_k^2}{(Q - T)^2} \right] \\ &= (Q - T)^2 \left[1 - \frac{1}{2} \frac{m_\beta^2}{(Q - T)^2} \right] \simeq (Q - T) \sqrt{(Q - T)^2 - m_\beta^2} \end{aligned}$$

Kurie plot

$$K(T) = \sqrt{\frac{\frac{d\Gamma/dT}{(\cos\vartheta_c G_F)^2}}{\frac{2\pi^3}{|\mathcal{M}|^2 F(E) pE}}} = \left[(Q - T) \sqrt{(Q - T)^2 - m_{\nu_e}^2} \right]^{1/2}$$

Predictions of 3ν -Mixing Paradigm

$$m_\beta^2 = |U_{e1}|^2 m_1^2 + |U_{e2}|^2 m_2^2 + |U_{e3}|^2 m_3^2$$



► Quasi-Degenerate:

$$m_\beta^2 \simeq m_\nu^2 \sum_k |U_{ek}|^2 = m_\nu^2$$

► Inverted Hierarchy:

$$m_\beta^2 \simeq (1 - s_{13}^2) \Delta m_A^2 \simeq \Delta m_A^2$$

► Normal Hierarchy:

$$m_\beta^2 \simeq s_{12}^2 c_{13}^2 \Delta m_S^2 + s_{13}^2 \Delta m_A^2 \\ \simeq 2 \times 10^{-5} + 6 \times 10^{-5} \text{ eV}^2$$

► If $m_\beta \lesssim 4 \times 10^{-2} \text{ eV}$



Normal Spectrum

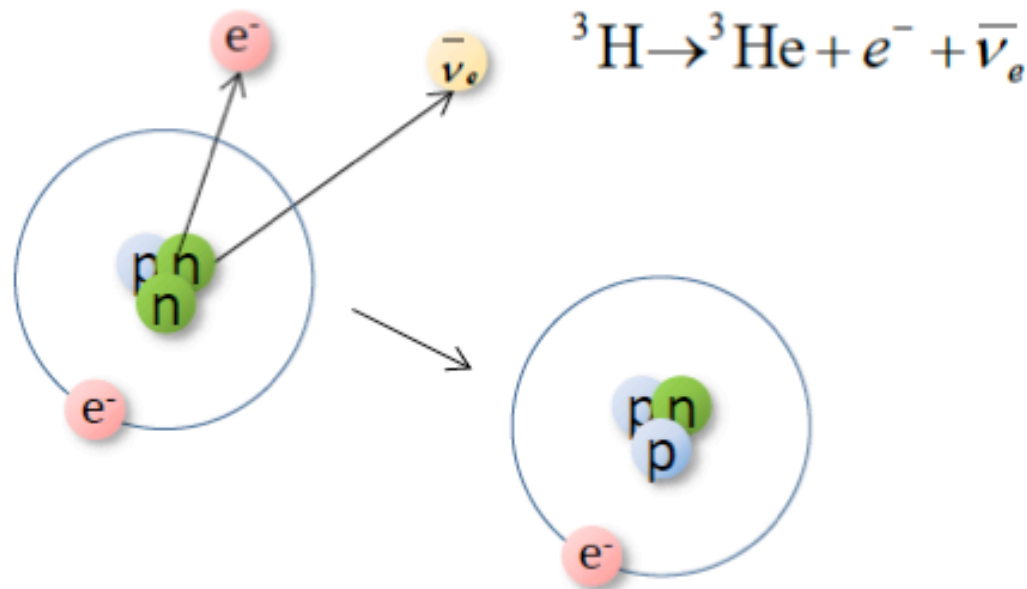
Remember: $\sqrt{\Delta m_A^2} \simeq 5 \times 10^{-2} \text{ eV}$

Beta decay of ^3H

$$Q = M_{^3\text{H}} - M_{^3\text{He}} - m_e = 18.58 \text{ keV}$$

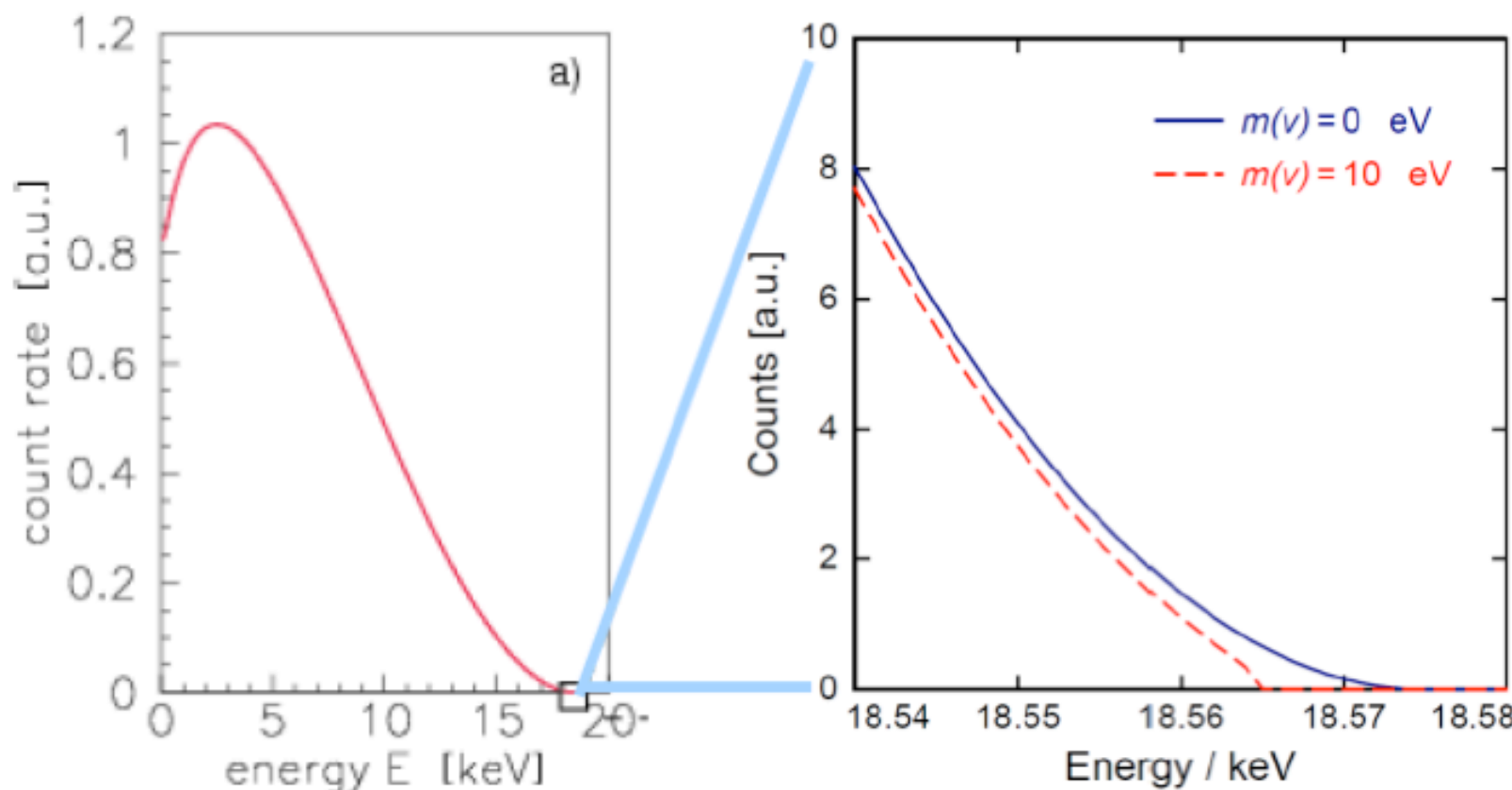
$$\tau_{1/2} \cong 12.3 \text{ years} \quad (4 \cdot 10^8 \text{ atoms for 1 Bq})$$

reasonably short lifetime



^3H : chosen because:

- ✓ low $Q \Rightarrow$ enhanced $\frac{n(\Delta T)}{n} \propto \left(\frac{\Delta T}{Q_\beta}\right)^3$
- ✓ simple atomic structure (small uncertainties on $|\mathcal{M}|^2 F(Z, E_e)$)



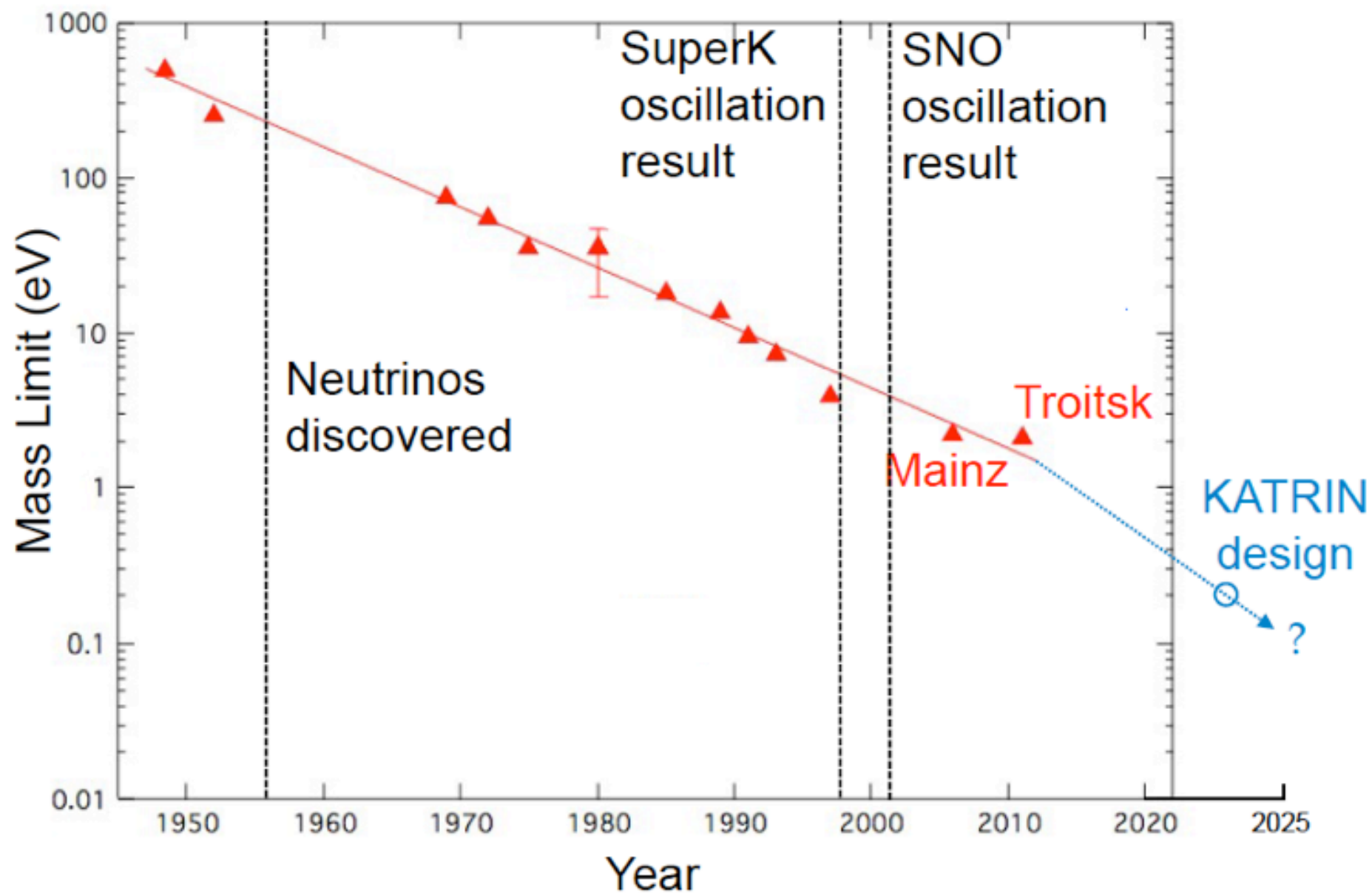
Only a small fraction of events
in the last eV below the endpoint:
 $2 \cdot 10^{-13}$

Tritium is present as
bi-atomic molecules

TRITIUM



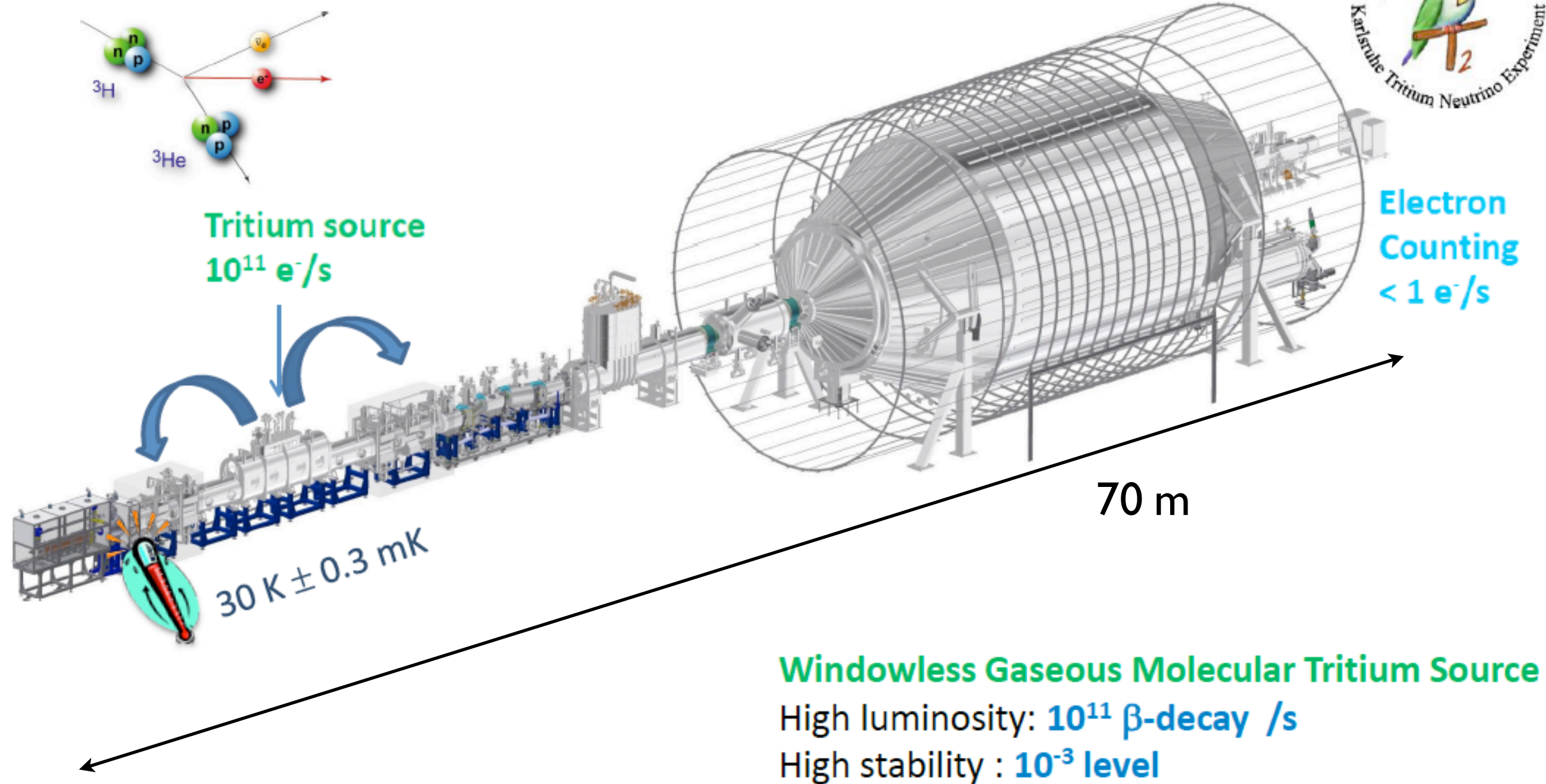
$m_{\nu, \text{eff}}^2$: A Brief History in Tritium



Adapted from J. Wilkerson, Neutrino 2012

The KATRIN experiment

The source should be transparent to the emitted electrons: gas or thin layers



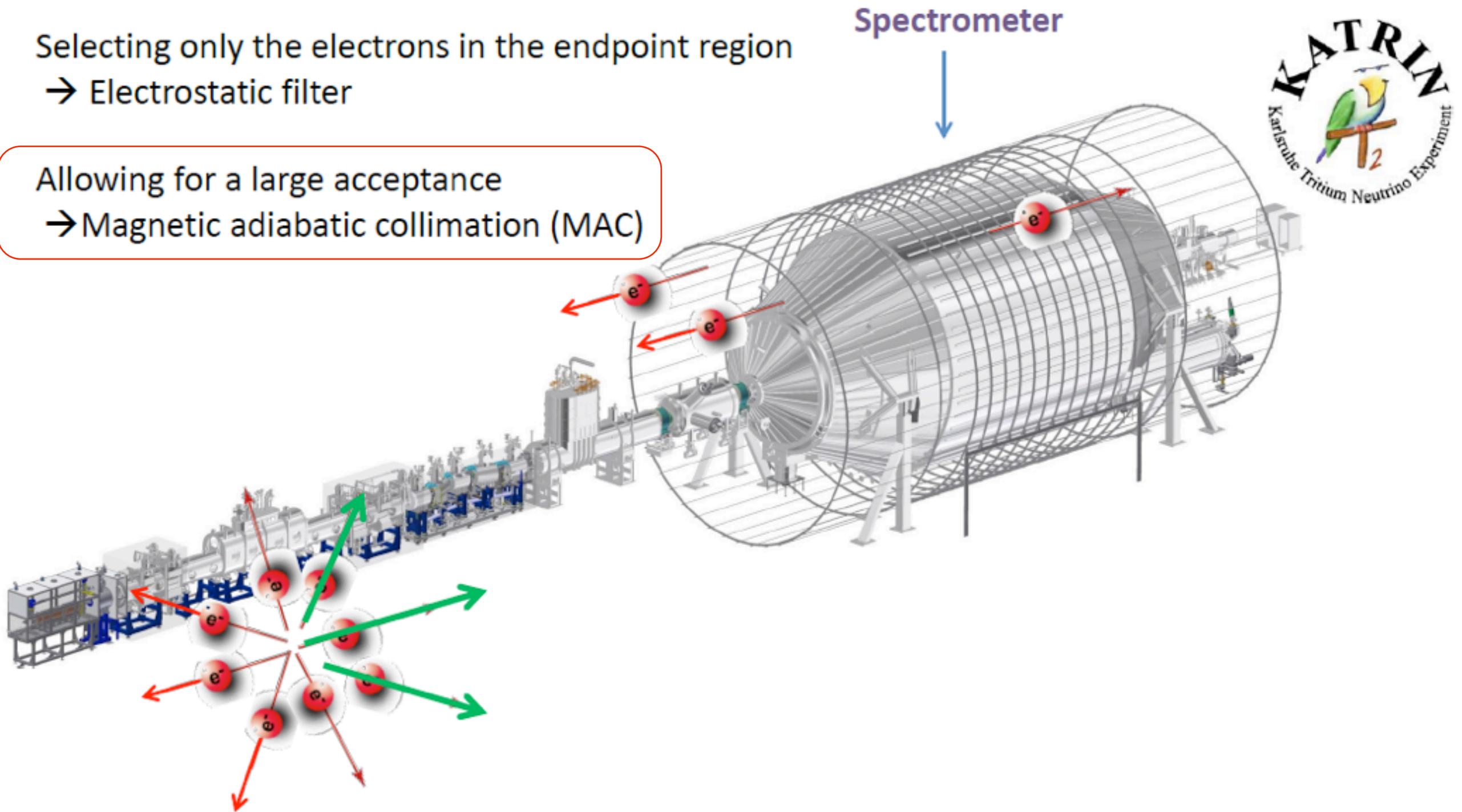
The KATRIN experiment

Selecting only the electrons in the endpoint region

→ Electrostatic filter

Allowing for a large acceptance

→ Magnetic adiabatic collimation (MAC)



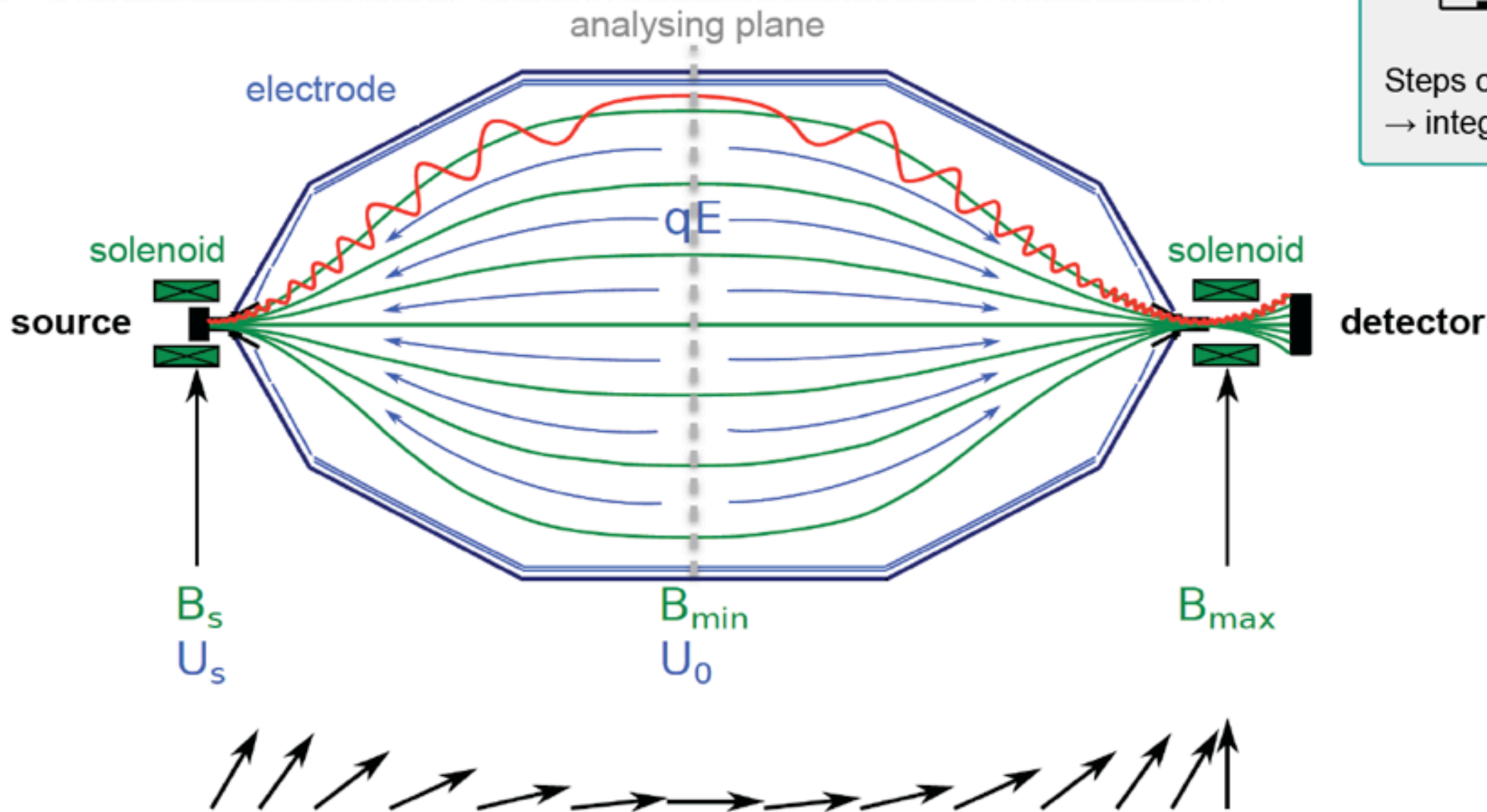
MAC-E filter principle allows for
< 1 eV energy cut off

High-resolution β spectrometer

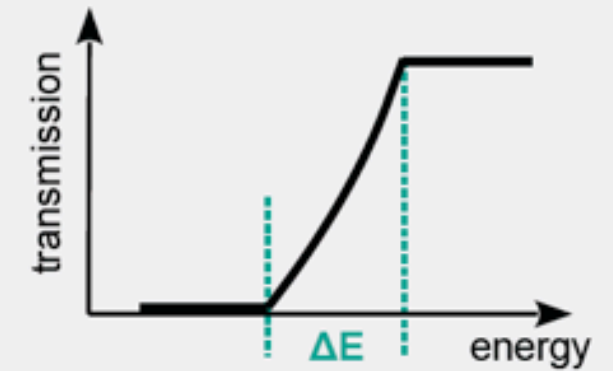
Magnetic Adiabatic Collimation & Electrostatic Filter

- integrating electrostatic filter ($E_{\text{kin}} > eU_0$)
- “clean” (analytic) response function
- $\Delta E < 1$ eV at 18.6 keV

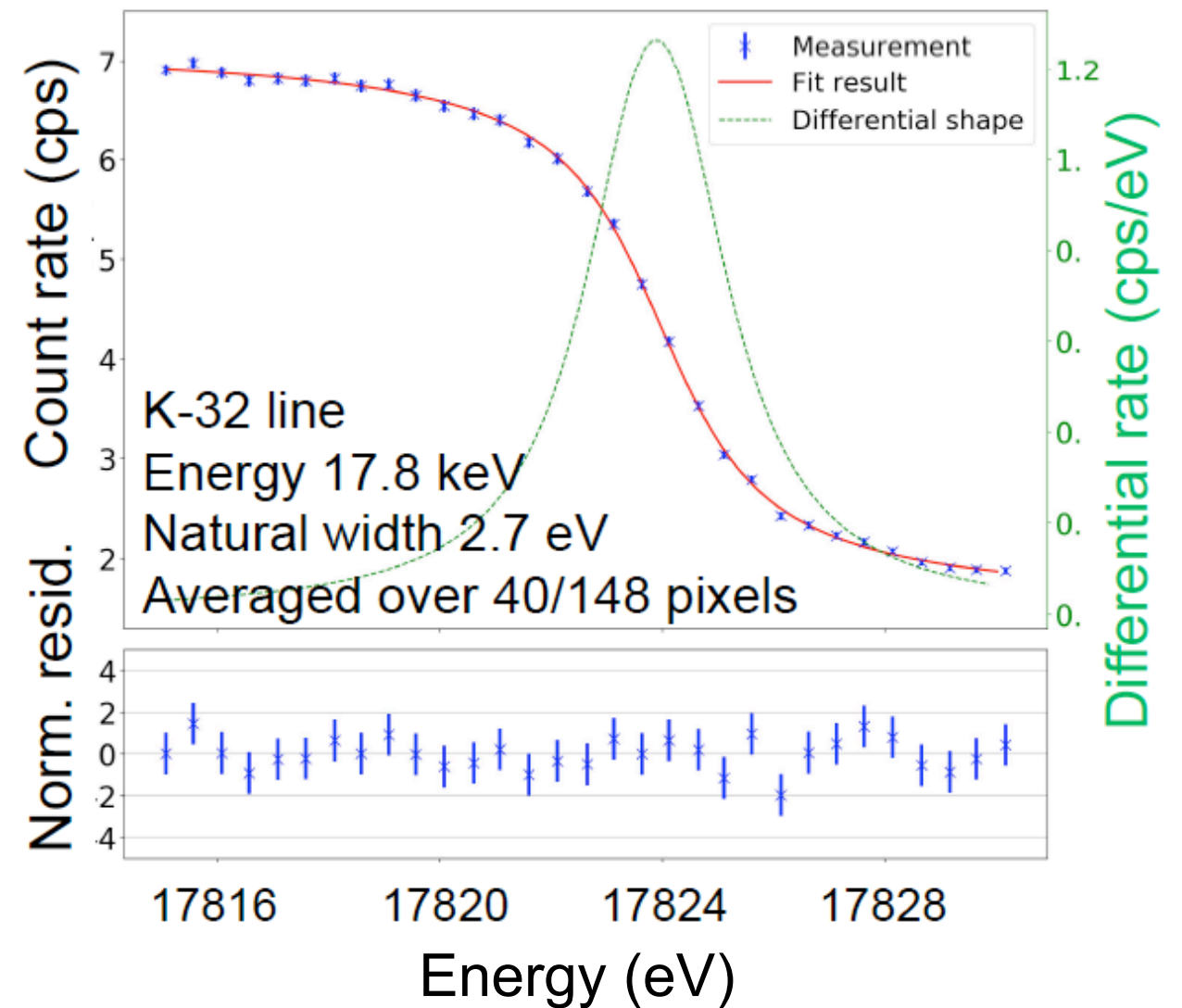
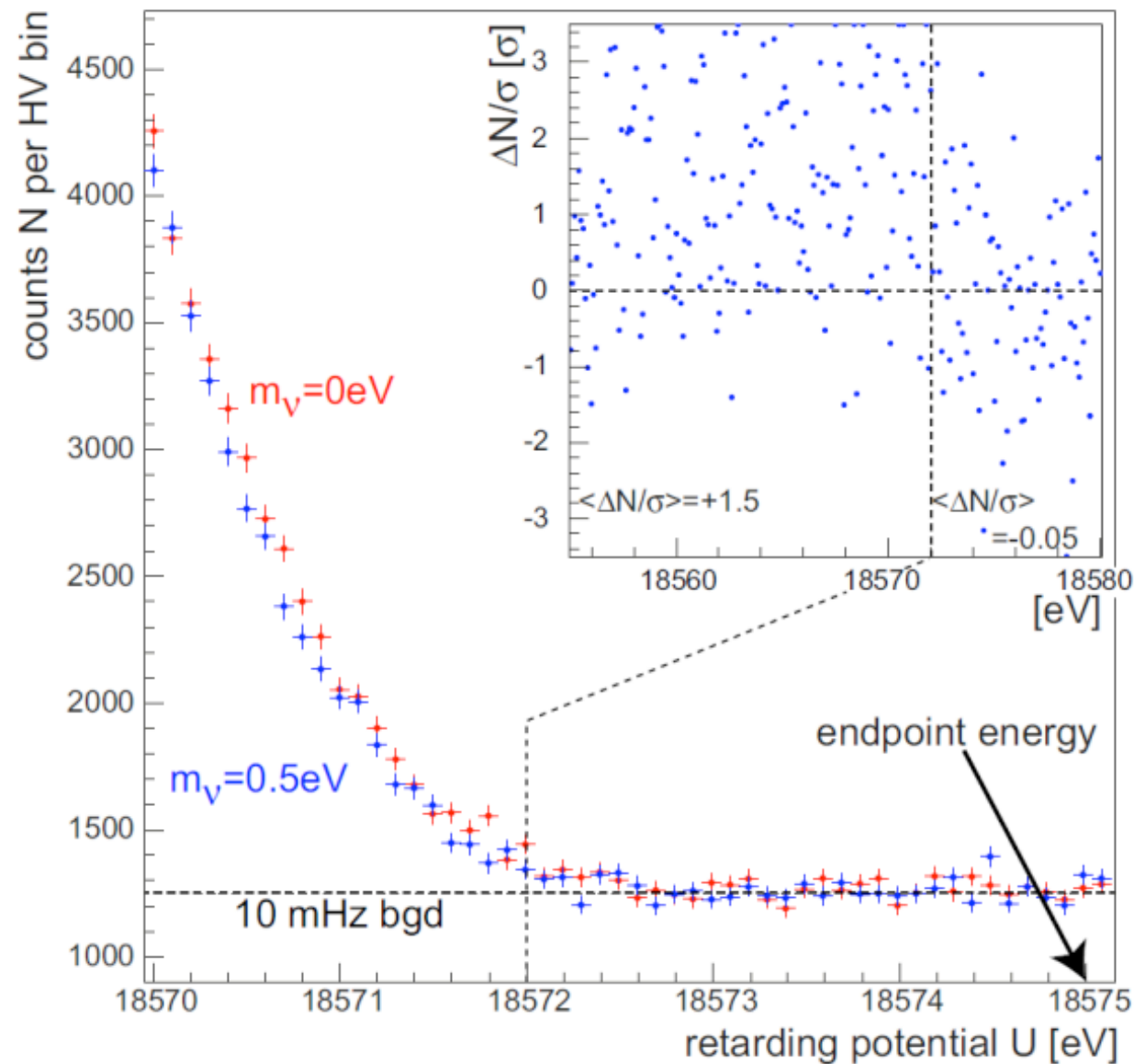
$$\frac{\Delta E}{E} = \frac{B_{\text{min}}}{B_{\text{max}}}$$



Sharp high-pass filter:



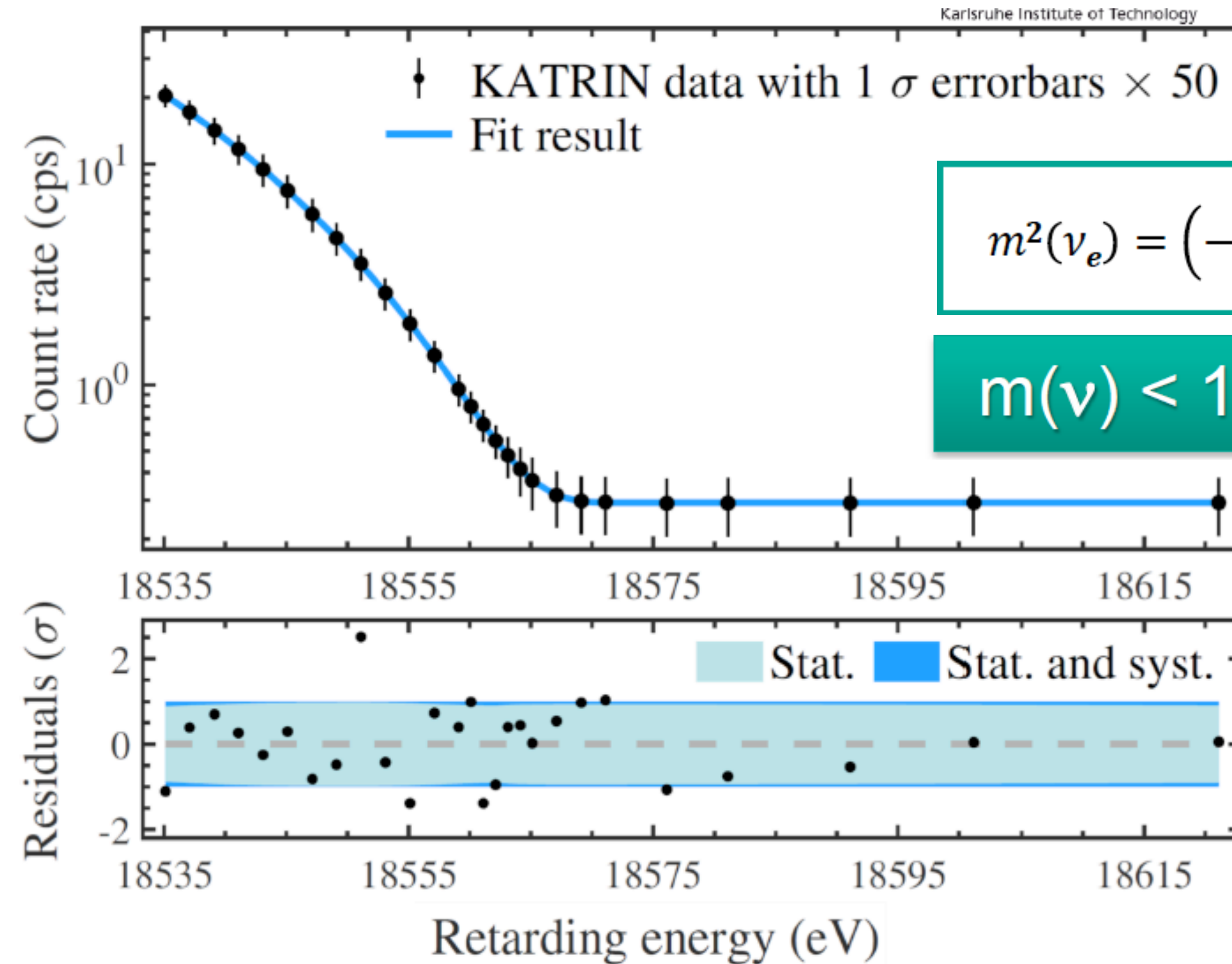
Steps of filter potential
→ integrated β spectrum



“Calibration”: example with a real
July 2017 pre-run with ^{83}Kr de-
excitation lines

- The larger the spectrometer, the smaller the gradient of the e- momentum
- **Integrated** e- spectrum (threshold effect)
- Will measure $N(e^-)$ vs electric potential applied
- Measurement up to 30 eV below end-point (Q-value)

First KATRIN result



$$m^2(\nu_e) = \left(-1.0^{+0.9}_{-1.1} \right) \text{eV}^2 \text{ (90\% CL)}$$

$$m(\nu) < 1.1 \text{ eV (90\% CL)}$$

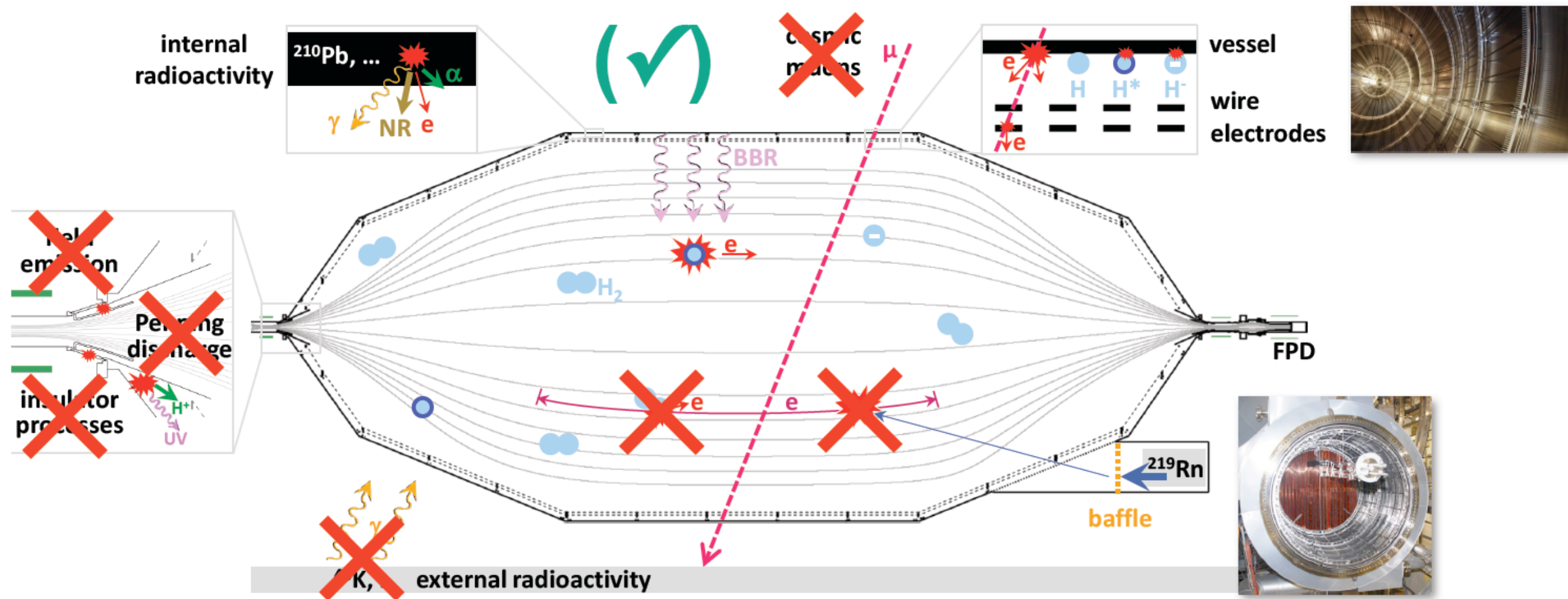
- 2 million events in
in 90-eV-wide interval
(522 h of scanning)
- excellent goodness-of-fit
 $\chi^2 = 21.4$ for 23 d.o.f.
(p-value = 0.56)

$$E_0 = (18573.7 \pm 0.1) \text{ eV} \Rightarrow \text{Q-value} : (18575.2 \pm 0.5) \text{ eV} \quad \text{Q-value } [\Delta M(^3\text{H}, ^3\text{He})]: (18575.72 \pm 0.07) \text{ eV}$$

Main sources of background:

- electrons produced by ionization in the residual gas: **veto system** in place
- electrons from interactions of cosmic rays: **veto system** in place
- γ -rays from natural radioactivity emanating from material surrounding the detector and from the detector itself: **this is still open** (^{210}Pb on spectrometer walls)

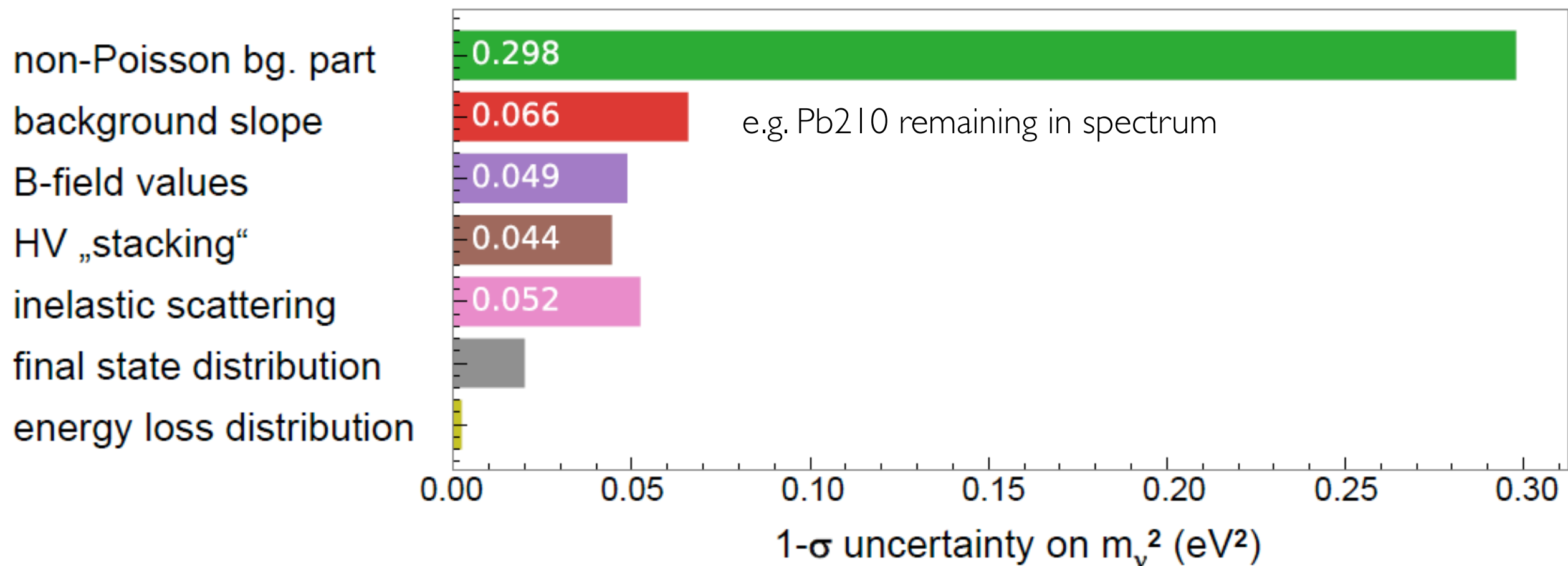
Backgrounds vary over a large range of energies, β -electrons concentrated.
Rely on accurate E determination to separate and reject bkg



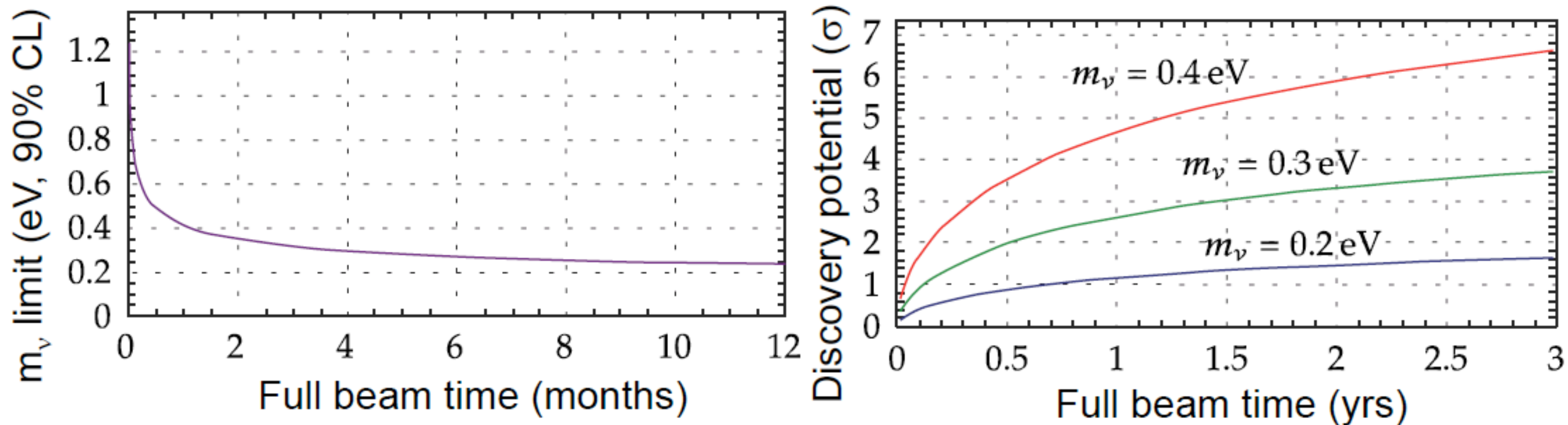
Systematic uncertainties

■ well-understood systematics budget σ_{syst} based on only 4 weeks of data

- total statistical uncertainty budget $\sigma_{\text{stat}} = 0.97 \text{ eV}^2$
 - total systematic uncertainty budget $\sigma_{\text{syst}} = 0.32 \text{ eV}^2$
- improves on Mainz/Troitsk by
- factor 2**
factor 6



- ◆ Full sensitivity ($\sigma_{\text{syst}} = \sigma_{\text{stat}}$) after 3 beam years (~ 5 calendar years)



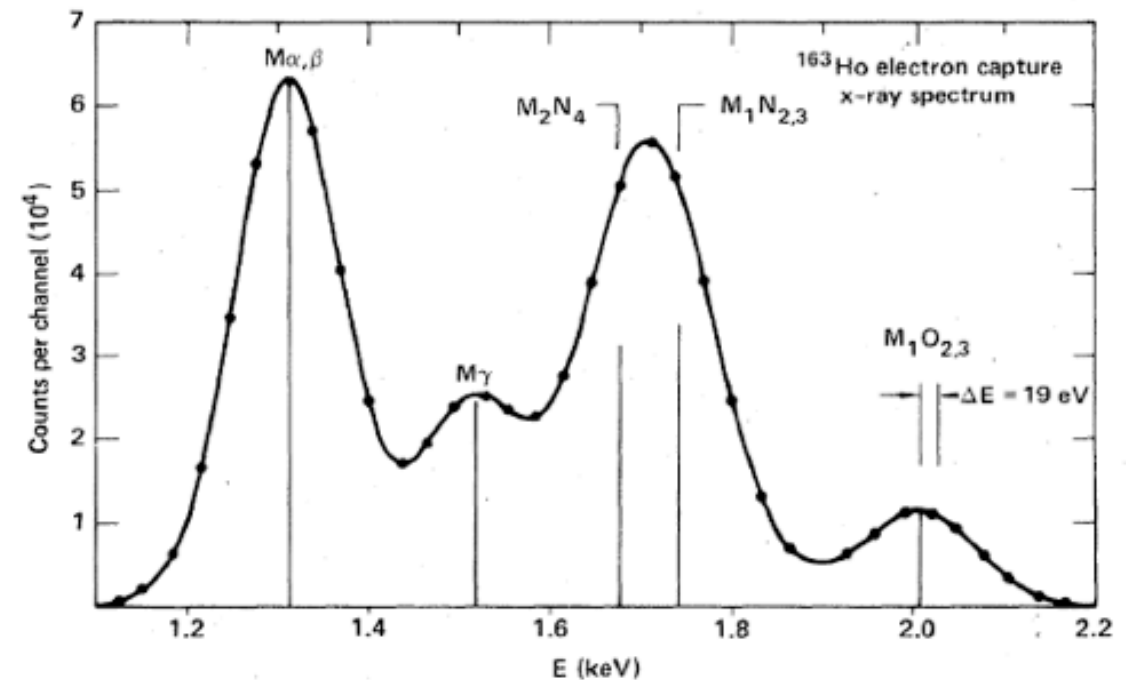
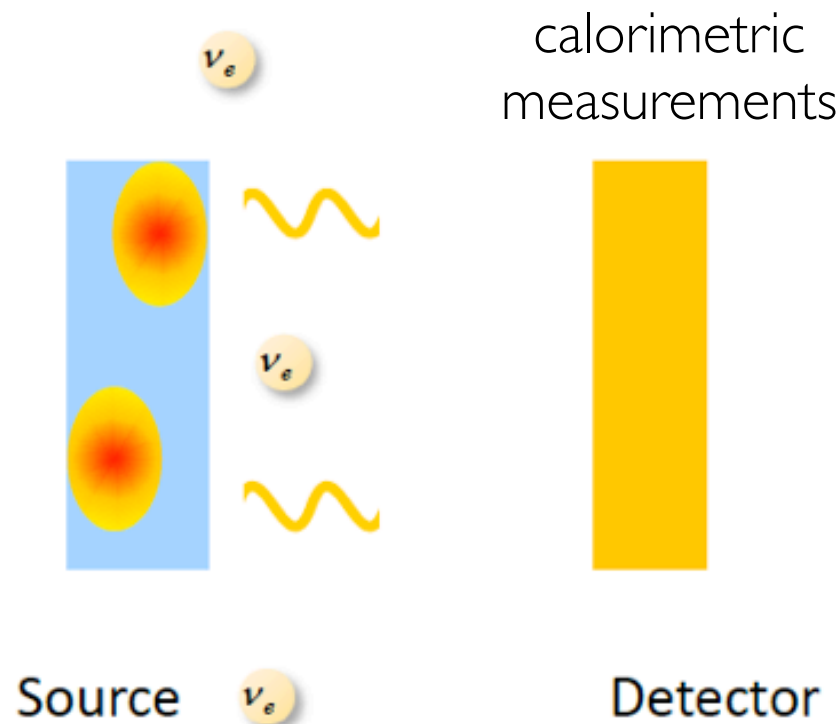
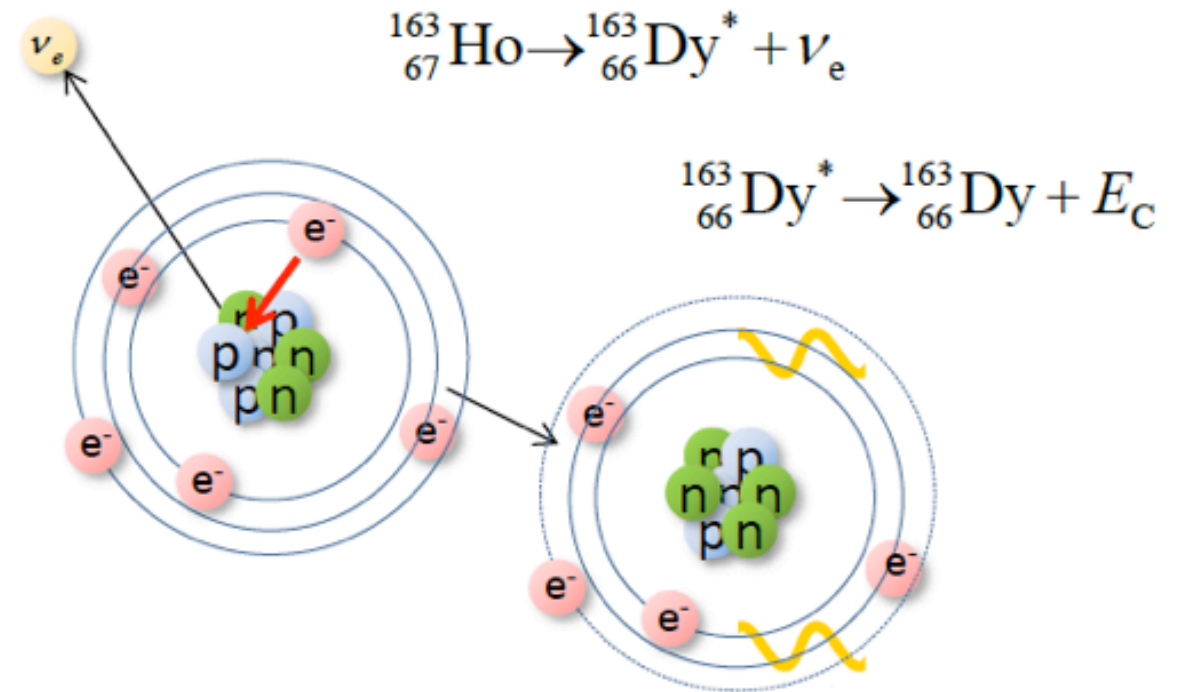
*G. Drexlin et al., Adv. High Energy Phys. **2013** (2013) 293986*

Excluding masses down to **0.24 eV** possible after 3 years of full beam

Electron capture in ^{163}Ho

Atomic de-excitation:

- X-ray emission
- Auger electrons
- Coster-Kronig transitions



Volume 118B, number 4, 5, 6

PHYSICS LETTERS

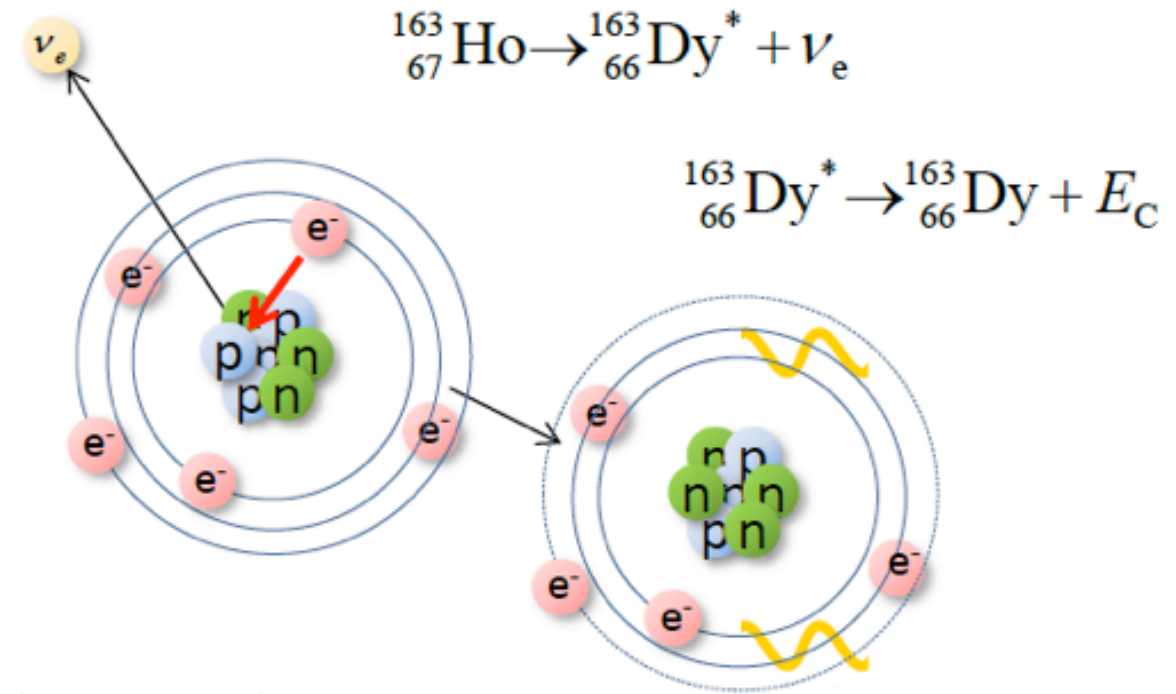
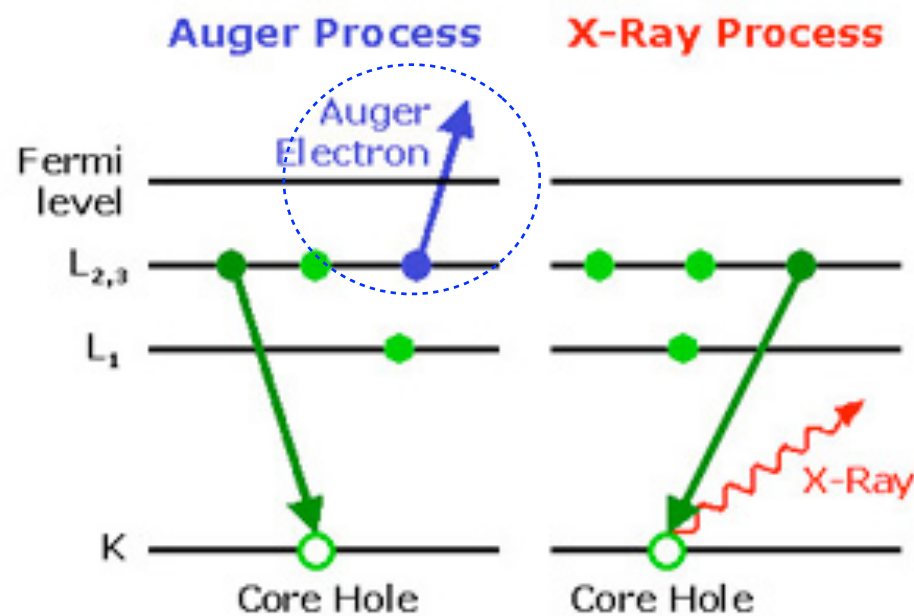
9 December 1982

CALORIMETRIC MEASUREMENTS OF ^{163}Ho DECAY AS TOOLS TO DETERMINE THE ELECTRON NEUTRINO MASS

A. DE RÚJULA and M. LUSIGNOLI ¹
 CERN, Geneva, Switzerland

Atomic de-excitation:

- **X-ray emission**
- Auger electrons
- Coster-Kronig transitions

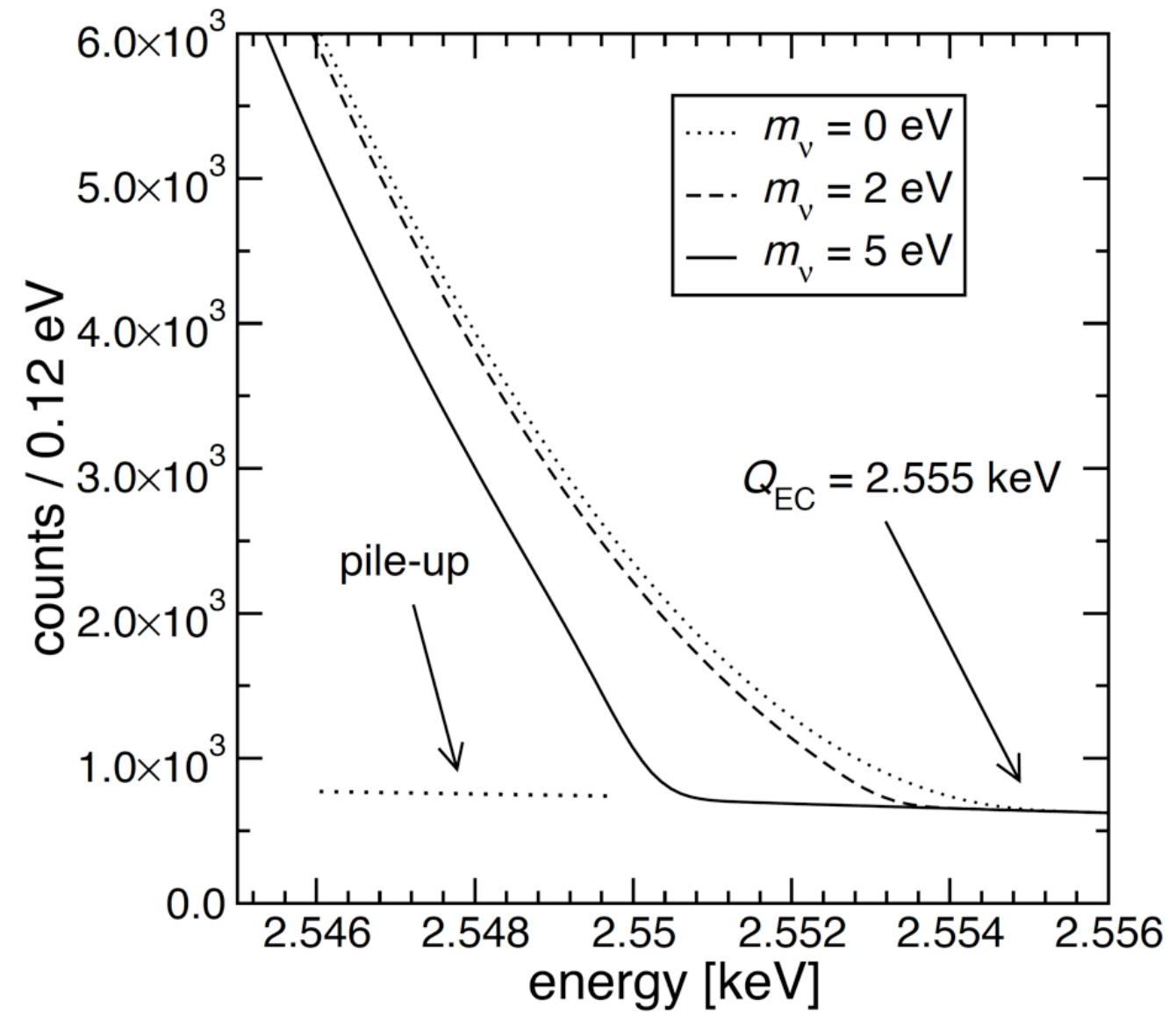
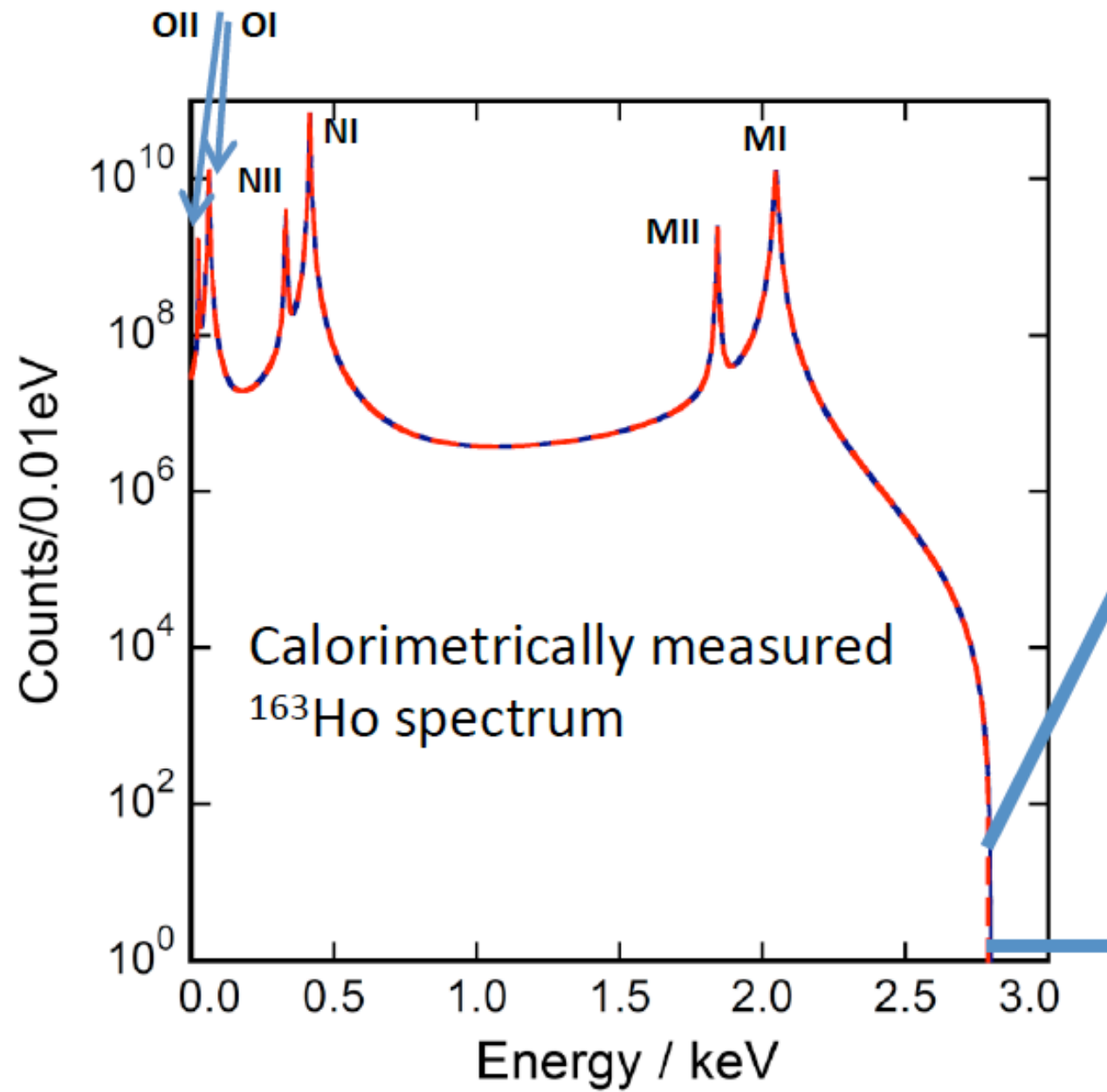


- $\tau_{1/2} \cong 4570 \text{ years}$ ($2 \cdot 10^{11}$ atoms for 1 Bq)

- $Q_{EC} = (2.833 \pm 0.030^{\text{stat}} \pm 0.015^{\text{syst}}) \text{ keV}$

S. Eliseev et al., *Phys. Rev. Lett.* **115** (2015) 062501

- Q_{EC} function of $m(\mathbf{v}) \Rightarrow$ measurement of $E(e)$ sensitive at end-point
- One sees Auger electron and measures $E(e)$ inclusively, with source = detector
 - no risk of loss or of mis-modelling energy at source
- E freed by de-exciting ^{163}Dy has \sim lowest known “**Q value**”: 2.8 keV
- **problem**: lifetime! need smart format of detector to maximize statistics



$$\frac{d\lambda_{EC}}{dE_c} = \frac{G_{\beta}^2}{4\pi^2} (Q - E_c) \sqrt{(Q - E_c)^2 - m_{\nu}^2} \times$$

$$\sum_i n_i C_i \beta_i^2 B_i \frac{\Gamma_i}{2\pi} \frac{1}{(E_c - E_i)^2 + \Gamma_i^2/4},$$

Equivalent of beta-decay but with B-W peaks corresponding to energy levels

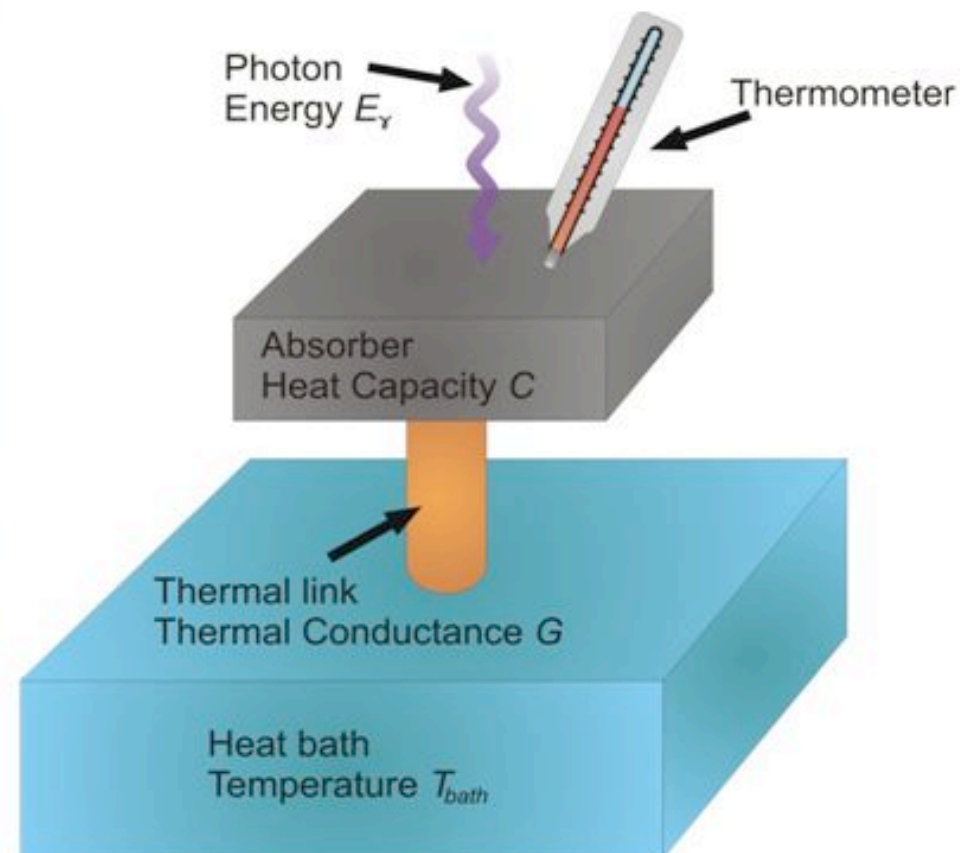
Microcalorimetry

- Small, segmented devices needed for high E resolution (and to avoid two events overlapping in time in same reading element)

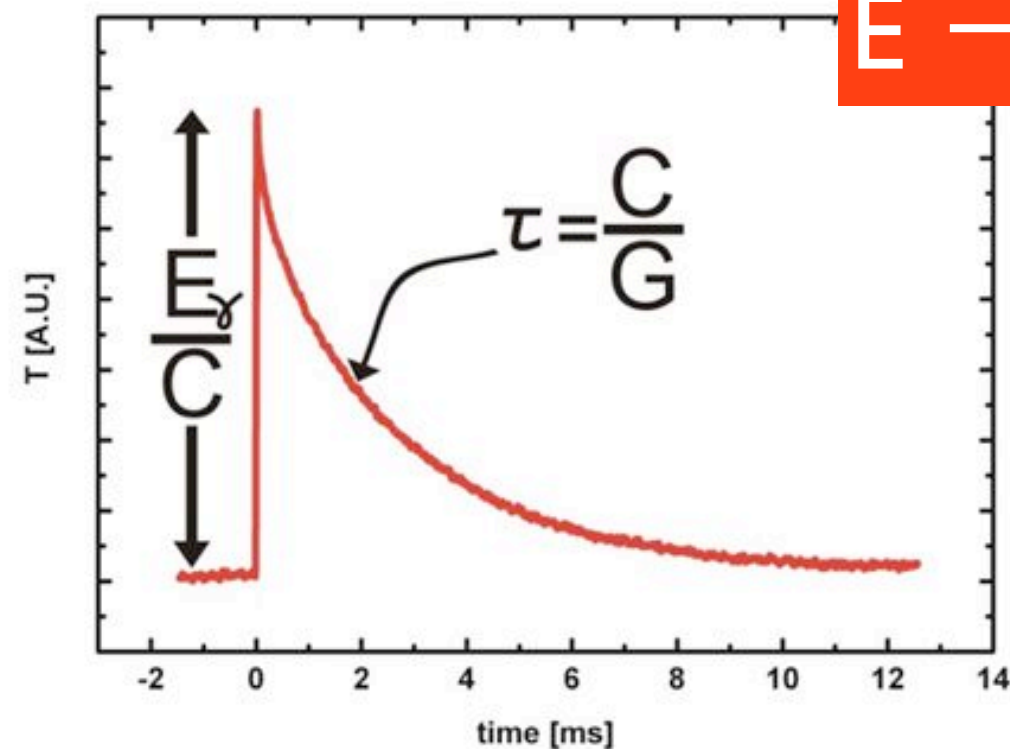
Transition-Edge Sensor (TES)



- TES as a calorimeter
 - Measures the energy of incident radiation

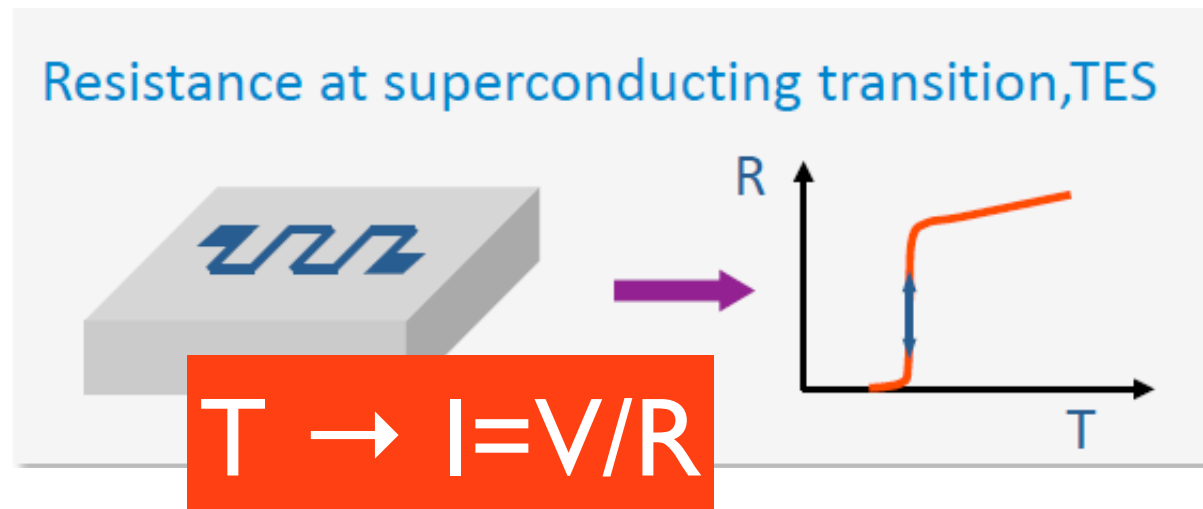


Schematics of a calorimeter

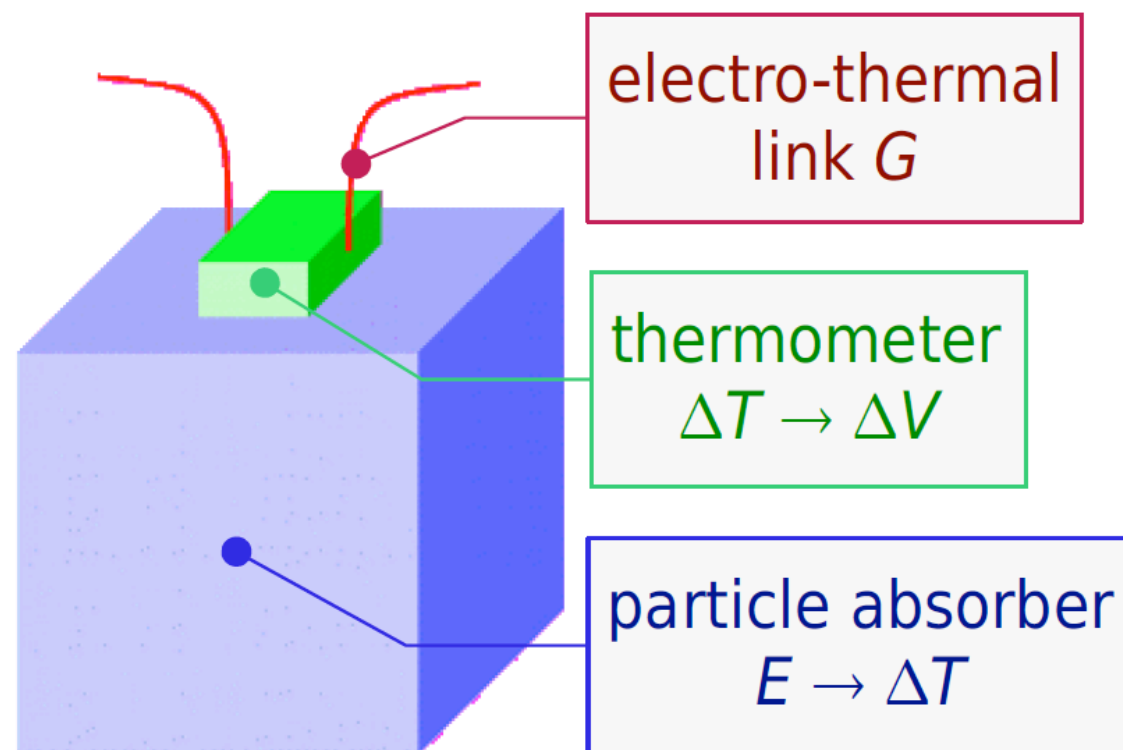
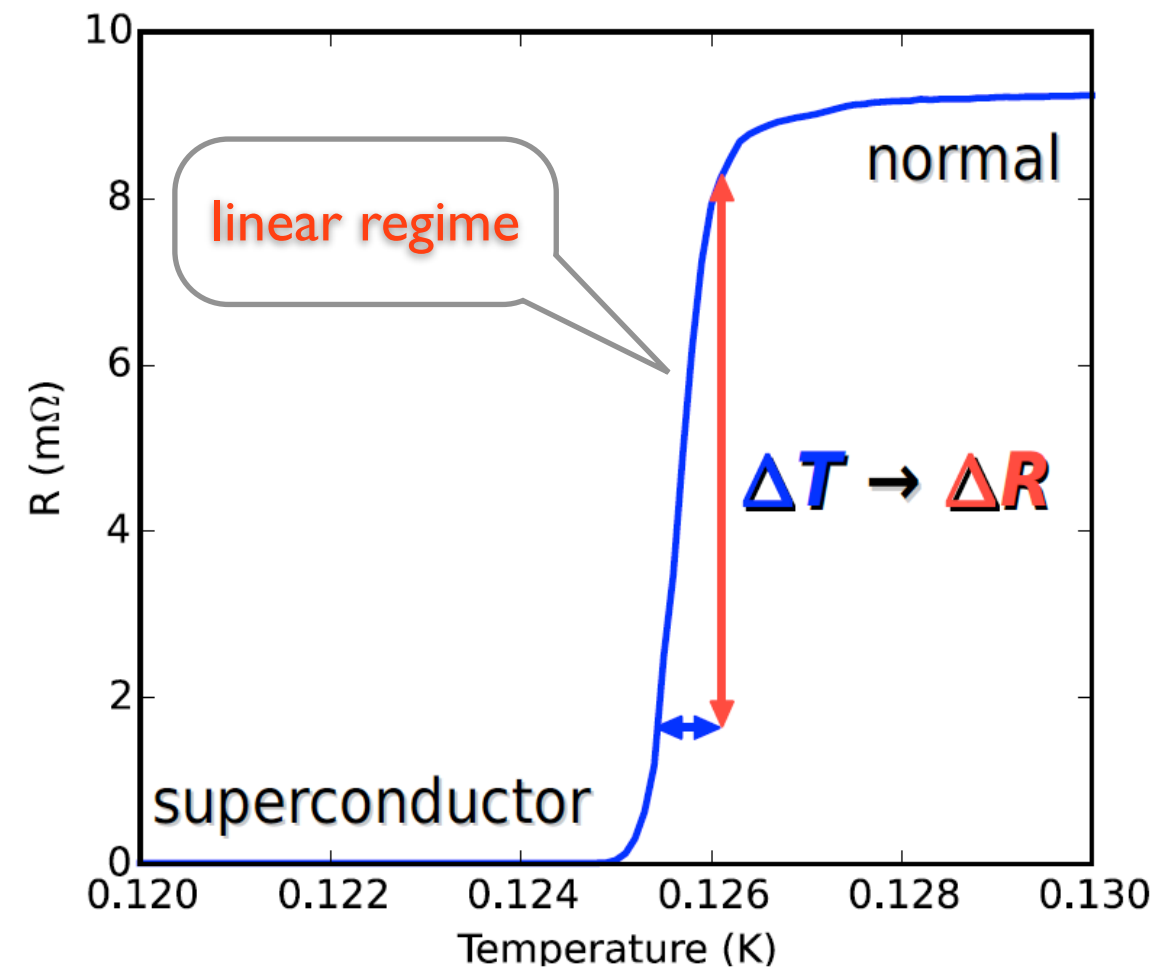


Typical pulse from a calorimeter

E → T



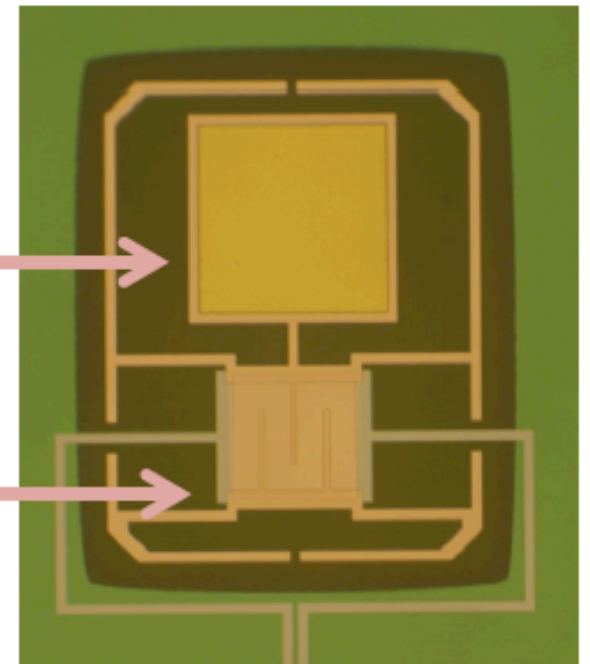
- Exploit super-conducting property to rapidly (but about linearly) change R with T



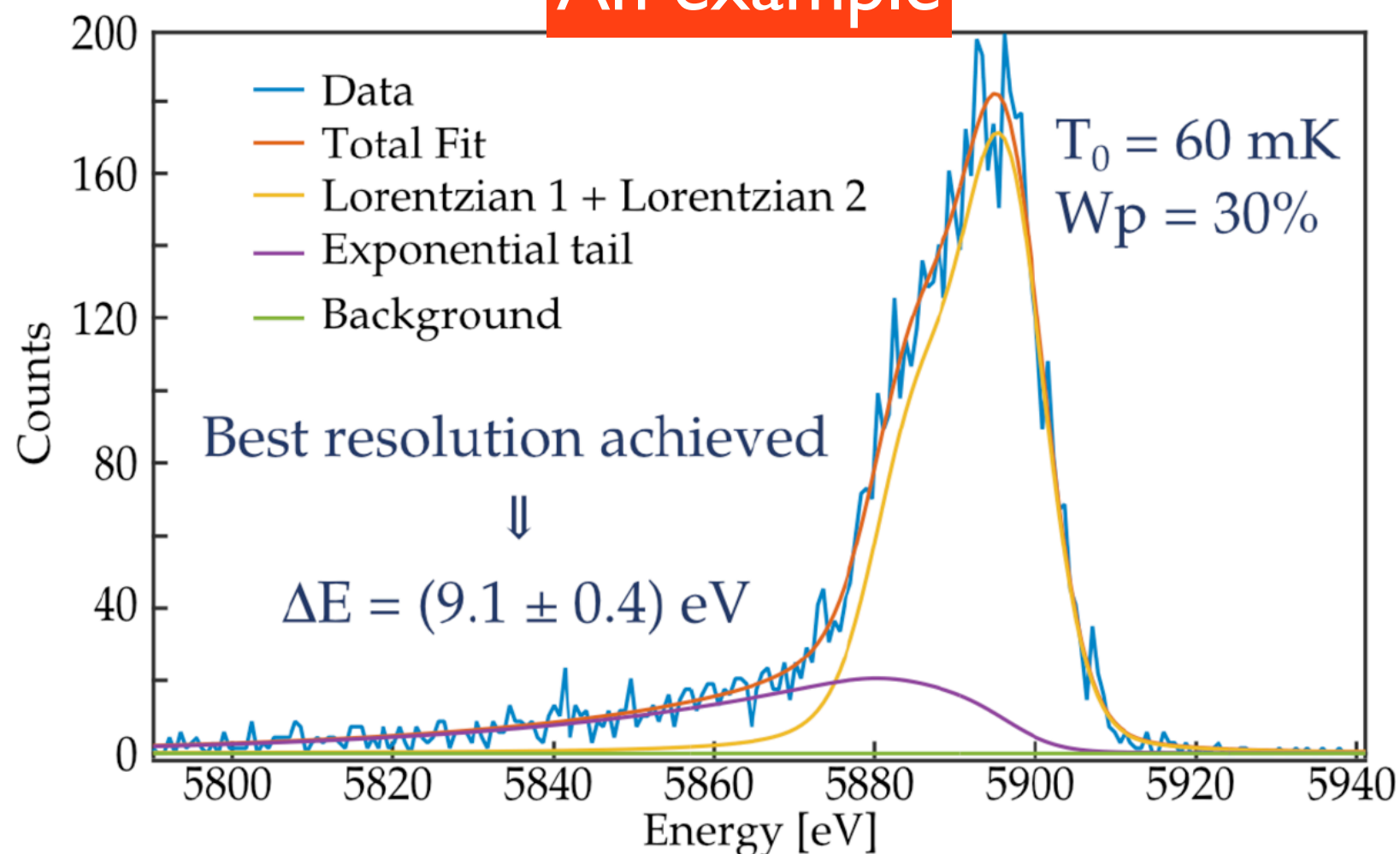
- Use film of material undergoing transition at roughly ^{163}Ho Q (2-3 keV)
 - linear with $E_c \Leftrightarrow T$
 - generates current read-out
- Electro-thermic feedback compensates increase of I from T
 - forces TES to stay around linear regime

Absorber: Bi-Au or Au + 6.5×10^{13} ^{163}Ho per detector \rightarrow **300 dec/sec**
 ^{163}Ho ion implanted in absorber using dedicated facility at Genoa University

Transition Edge Sensor: MoCu or MoAu superconducting films



An example



$$\Delta E \simeq 2.35 \sqrt{4kT E_{\text{max}}}$$

- $Q = 2.5 \text{ keV}$
- operating at $< 150 \text{ mK}$ heat capacity
- gives $\Delta E \sim 0.8 \text{ eV FWHM}$
- HOLMES claims $\Delta E = 1 \text{ eV}$

Pile-up

- TES have a relaxation time of \sim several ms
 - Two decays can happen close in time within the same TES element and not be discriminated
- ➡ bias on the E_c measured by summing two processes

spectrum is given by the two event pile-up probability $f_{pp} = \tau_R A_{EC}$, where τ_R is the time resolution and A_{EC} is the EC activity in each detector. This kind of statis-

Statistics in the end point region

- $N_{ev} > 10^{14} \rightarrow A \approx 1 \text{ MBq}$

Unresolved pile-up ($f_{pu} \sim a \cdot \tau_r$)

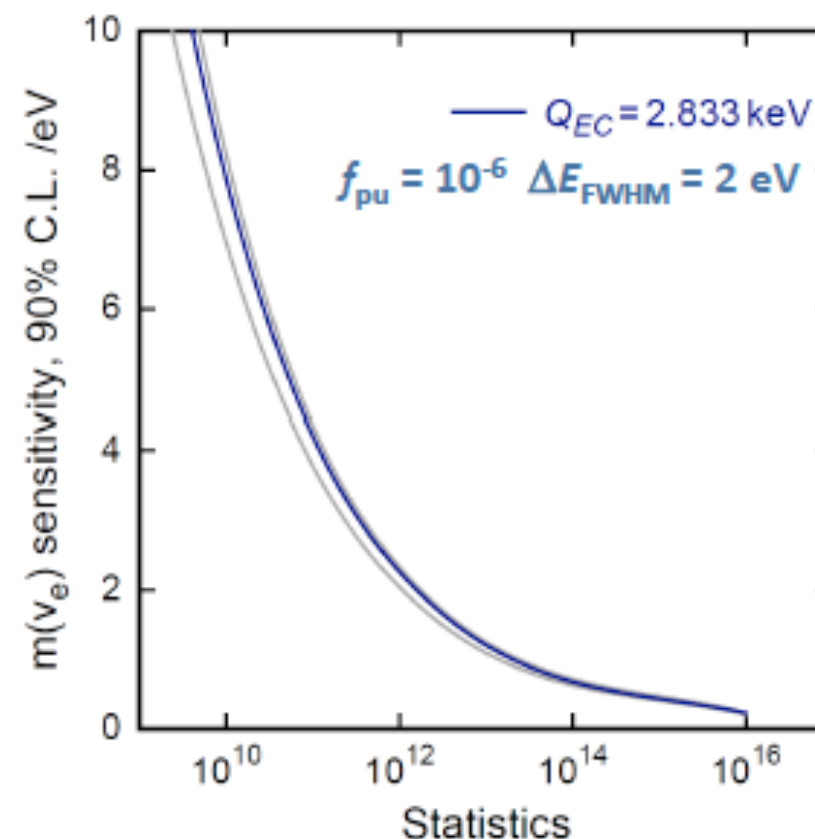
- $f_{pu} < 10^{-5}$ requirement
- $\tau_r < 1 \mu s \rightarrow a \sim 10 \text{ Bq}$
- 10^5 pixels

Precision characterization of the endpoint region

- $\Delta E_{FWHM} < 3 \text{ eV}$

Background level

- $< 10^{-5} \text{ events/eV/det/day}$



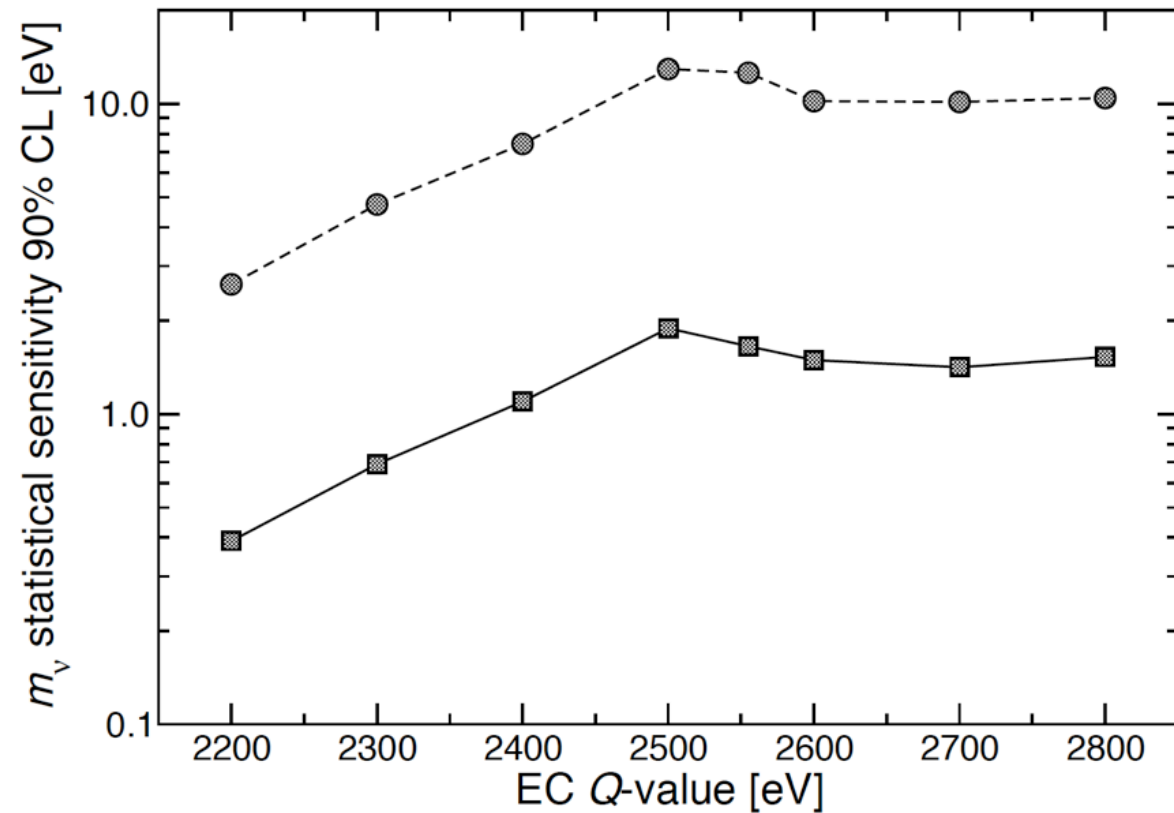


Fig. 4 Monte Carlo estimate of HOLMES neutrino mass statistical sensitivity for $N_{ev} = 3 \times 10^{13}$ (lower curve) or 10^{10} (upper curve) and with $f_{pp} = 3 \times 10^{-4}$, $\Delta E_{FWHM} = 1$ eV, and no background.

Effect of statistics

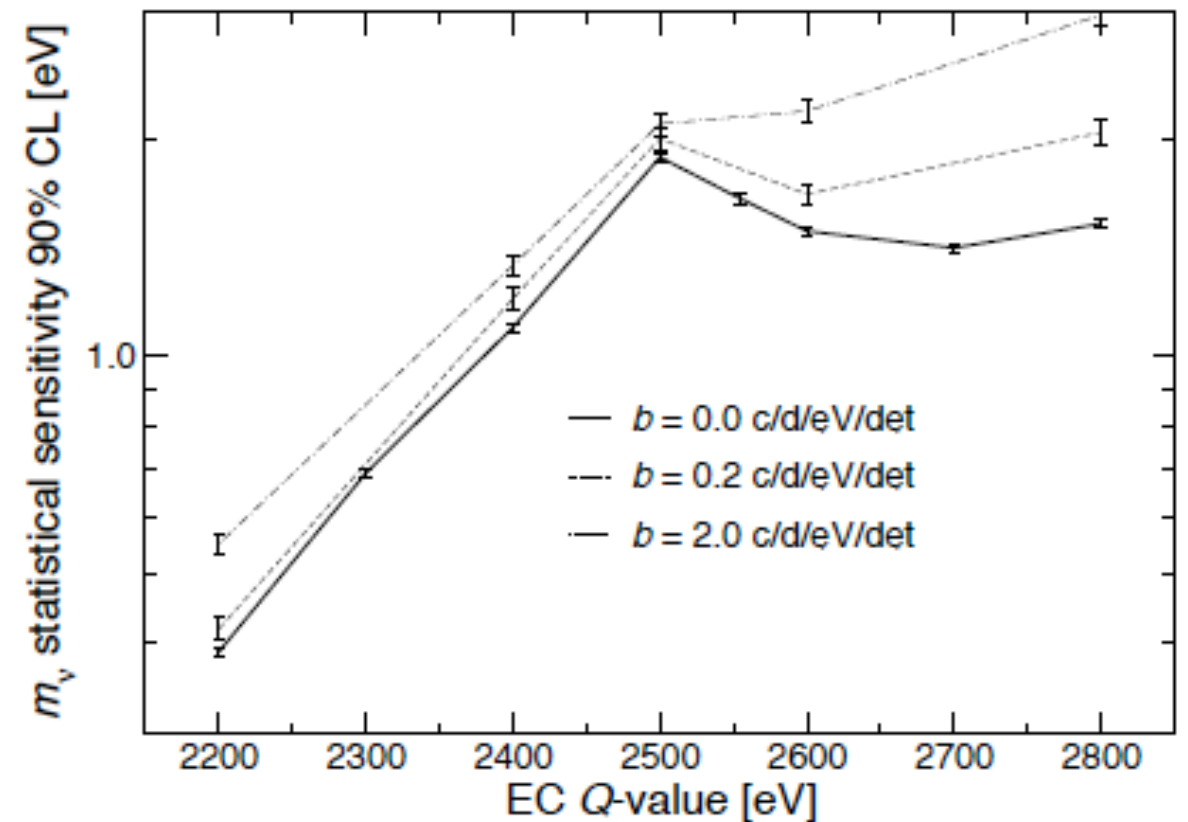
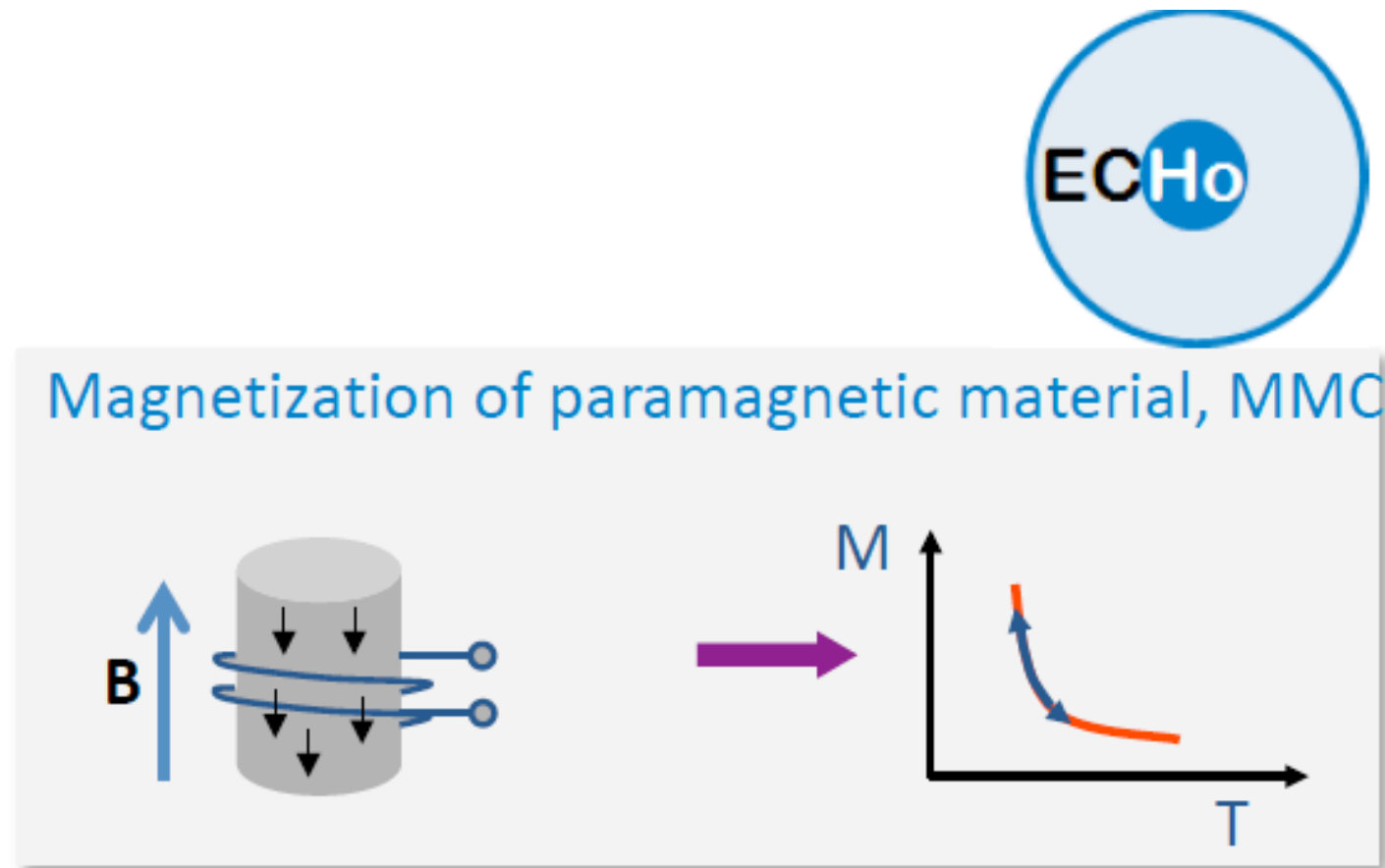


Fig. 9 Monte Carlo estimates of the effect of various background levels on HOLMES baseline statistical sensitivity.

Effect of bkg

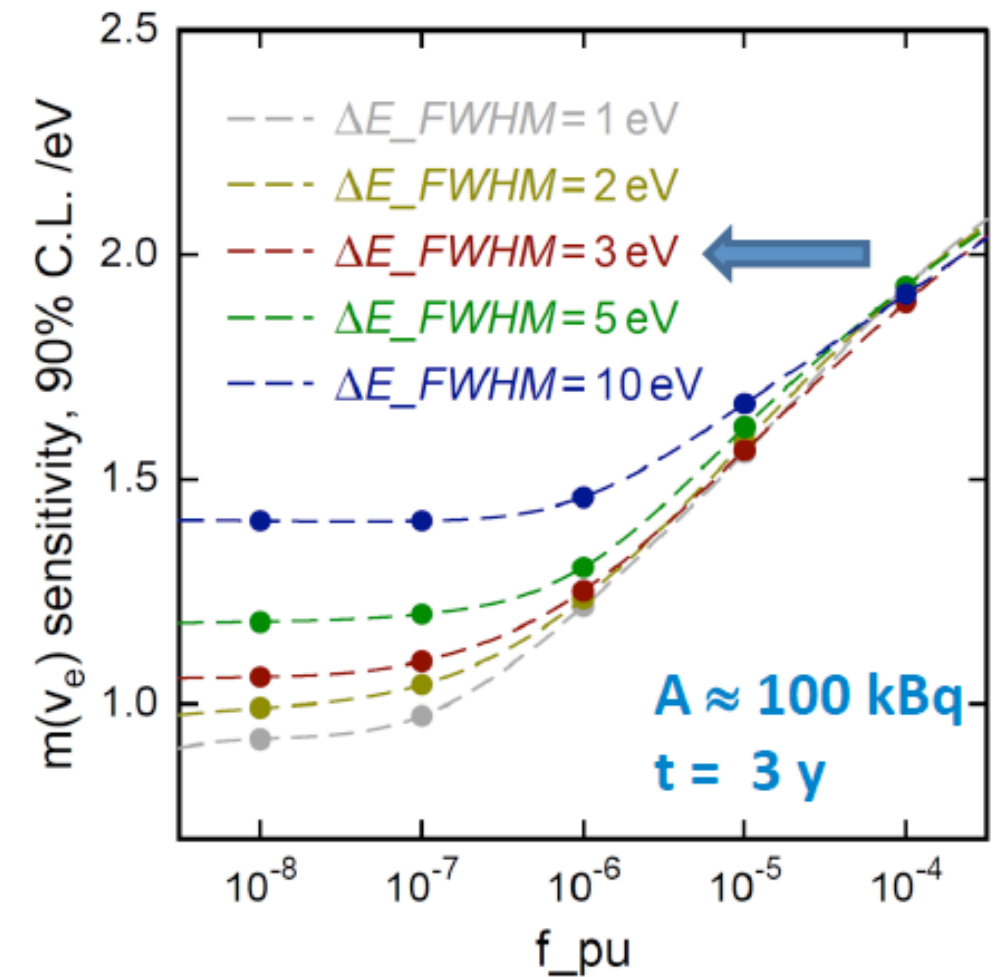
Overall this technique expected to currently attain
 $\sim 0.2\text{-}0.4$ eV neutrino mass sensitivity
 \Rightarrow competitive with spectrometers

Alternative observable: the ECHo experiment



A. Fleischmann, C. Enss and G. M. Seidel,
Topics in Applied Physics 99 (2005) 63

ECHo-100k (2018 – 2021)

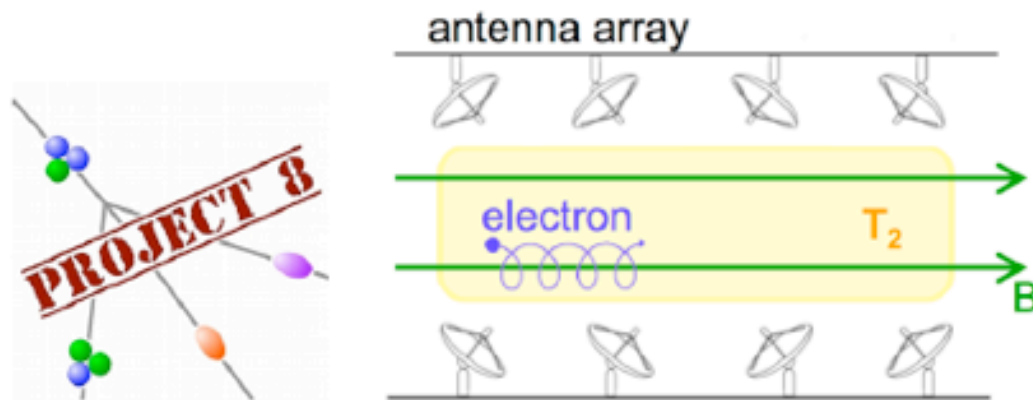


Activity per pixel 10 Bq
Number of detectors 12000
Readout: microwave SQUID multiplexing

Broadly same challenges and figures of merit to attain sensitivity

PROJECT 8

Alternative to KATRIN/
spectroscopy



- Enclosed volume filled with **tritium molecular gas**
- Add a **magnetic field** →
Decay electrons spiral around field lines
- Add **antennas** to detect the cyclotron radiation

Cyclotron Radiation Emission Spectroscopy (CRES)

- **Non-destructive** measurement of electron energy

$$\omega_{\gamma} = \frac{\omega_0}{\gamma} = \frac{eB}{K + m_e}$$

@ 1 Tesla

$\omega(18 \text{ keV}) \sim 26 \text{ GHz}$

$P(18 \text{ keV}) = 1.2 \text{ fW}$

$$Q = M_{3\text{H}} - M_{3\text{He}} - m_e = 18.58 \text{ keV}$$

B. Monreal & J. Formaggio PRD 80 (2009) 051301

Cyclotron Radiation Emission Spectroscopy (CRES)

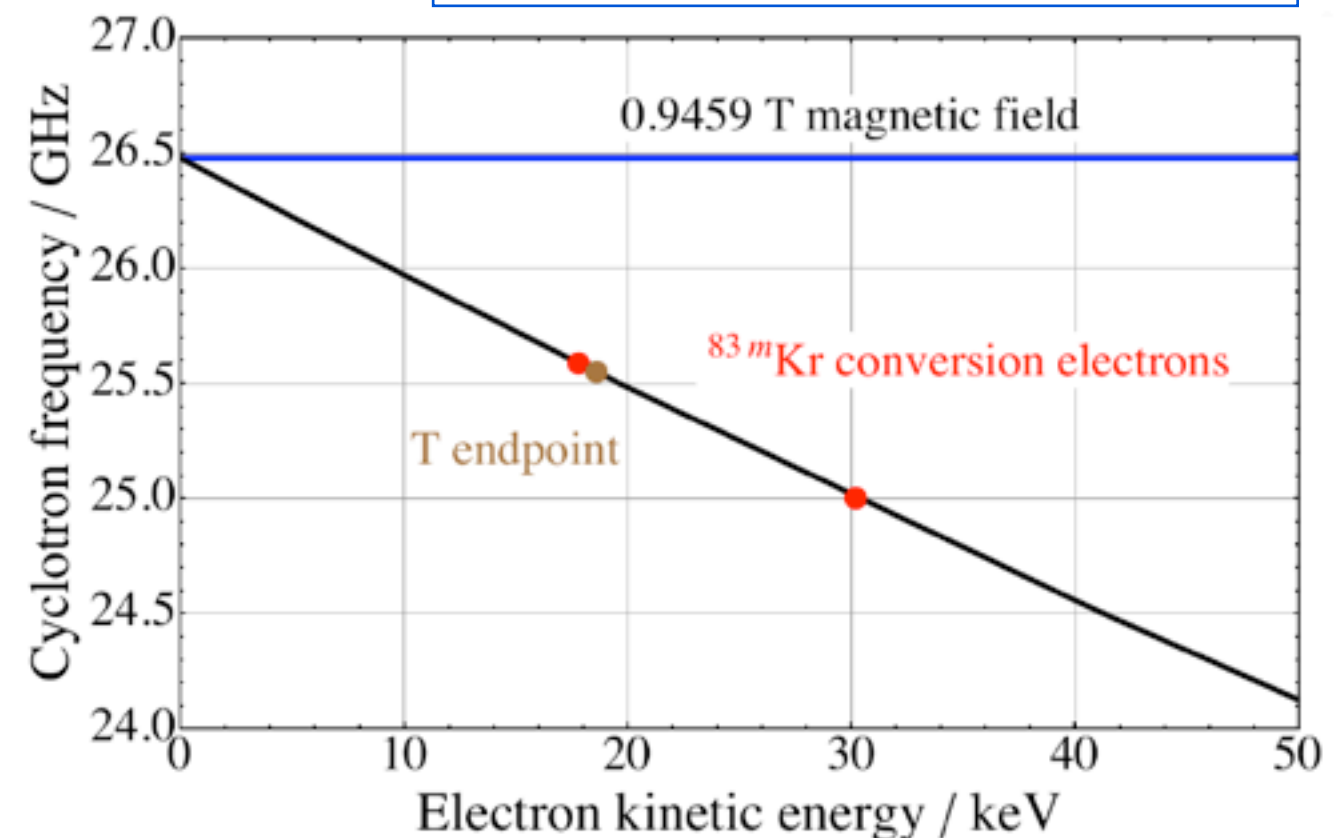
PROJECT 8

$$Q = M_{3\text{H}} - M_{3\text{He}} - m_e = 18.58 \text{ keV}$$

The electron cyclotron frequency is related to the electron kinetic energy

The cyclotron frequency is encoded in cyclotron radiation

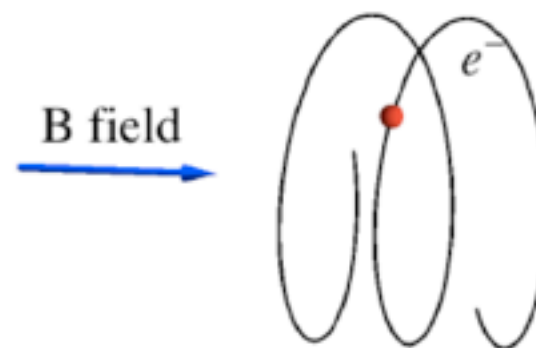
Frequency is something we can measure very precisely – eV resolution demonstrated, sub-eV resolution expected



Cyclotron motion:

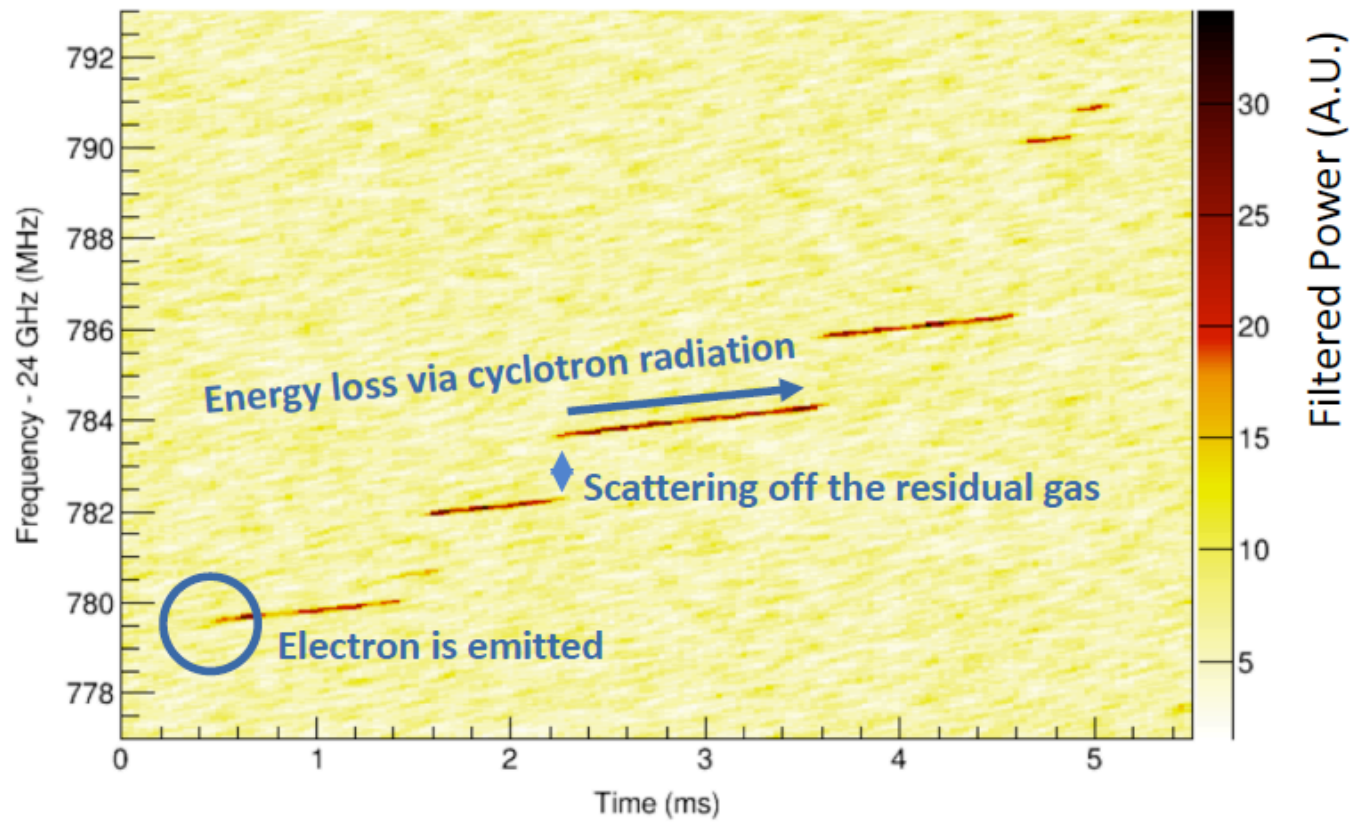
$$f_{\gamma} = \frac{f_c}{\gamma} B = \frac{1}{2\pi} \frac{eB}{m_e + E_{\text{kin}}/c^2}$$

$$f_c = 27\,992.491\,10(6) \text{ MHz T}^{-1}$$



Project 8 Electron Event with Energy 18 keV

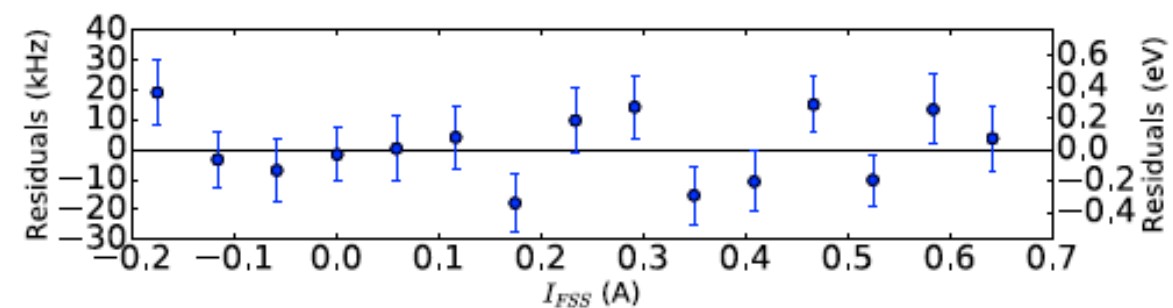
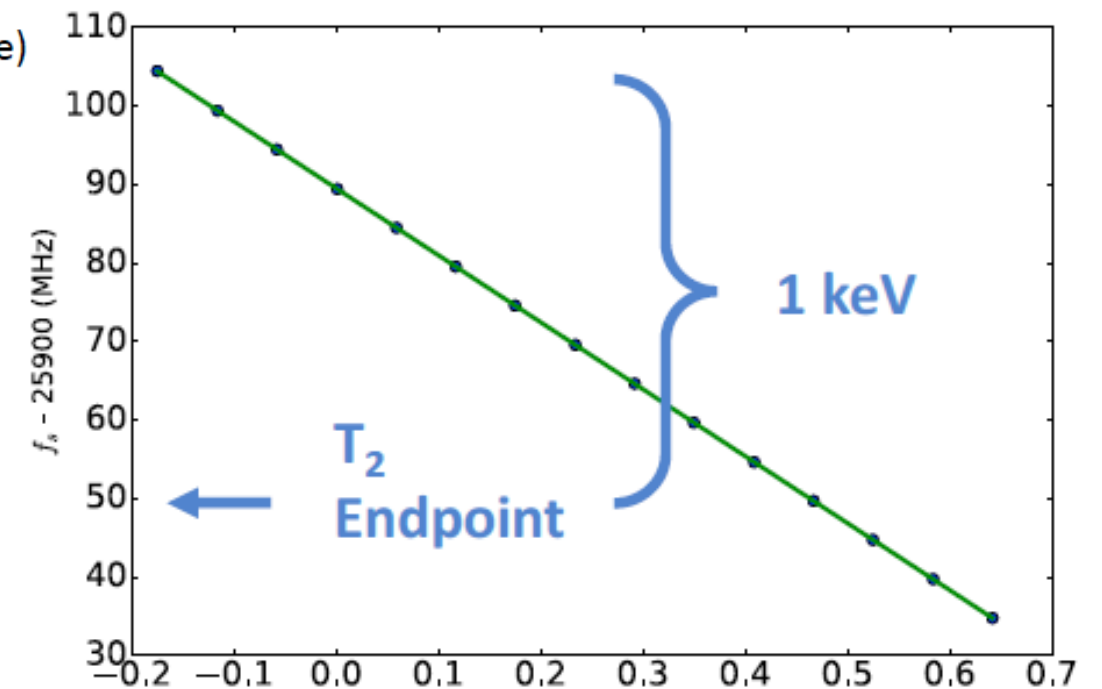
<https://zenodo.org/record/1286954#.XEiHGvx7mi4>



Frequency increases as energy is lost due to radiation (continuous) and collisions (discrete)

Cyclotron motion:

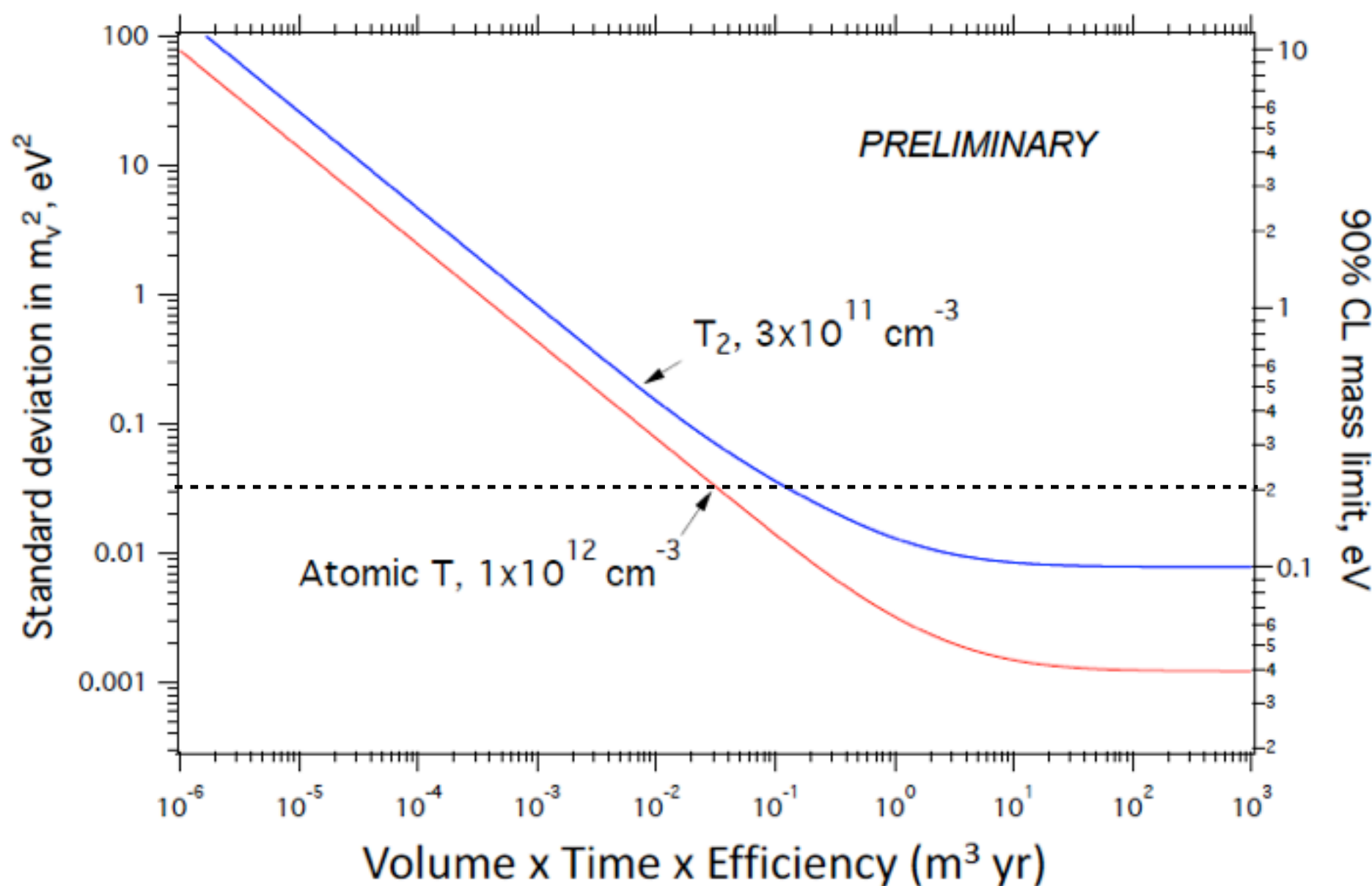
$$f_{\gamma} = \frac{f_c}{\gamma} B = \frac{1}{2\pi} \frac{eB}{m_e + E_{\text{kin}}/c^2}$$



Linearity test completed, good to 0.2 eV
Efficiency data being taken right now

Project 8 Projected Capabilities with Atomic Tritium

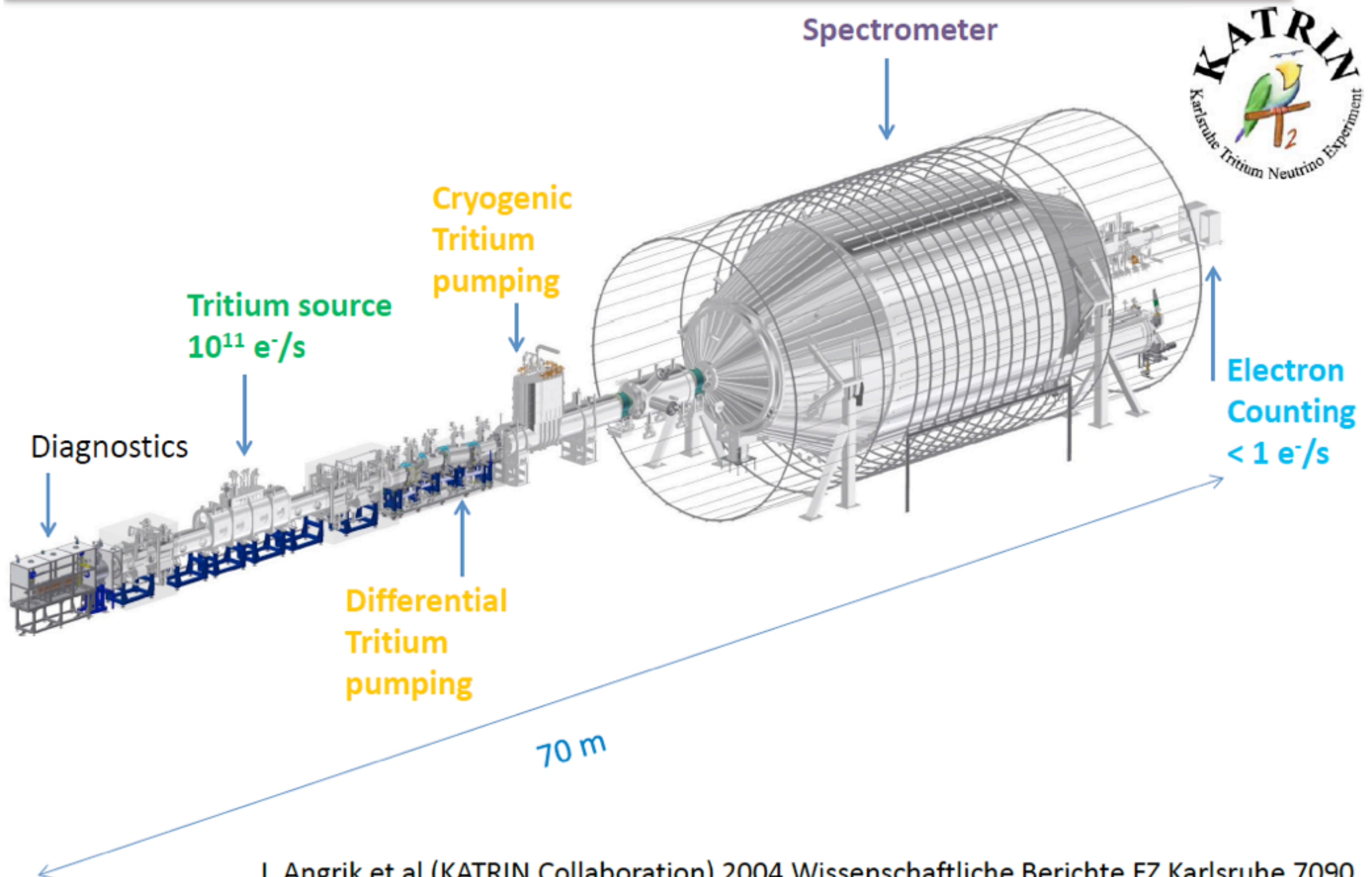
PROJECT 8



Atomic tritium should allow us sensitivity to a 40 meV mass scale with 10-100 m^3 -years exposure

Back up

The KATRIN experiment



J. Angrik et al (KATRIN Collaboration) 2004 Wissenschaftliche Berichte FZ Karlsruhe 7090

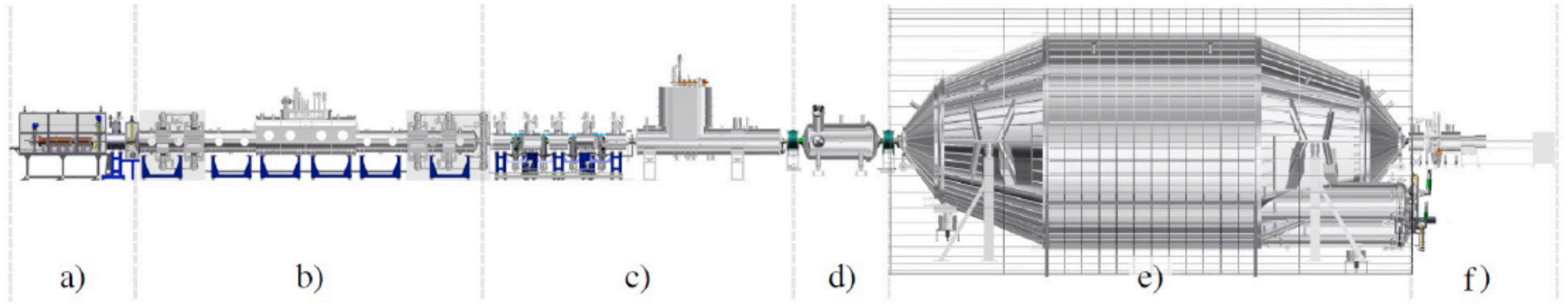
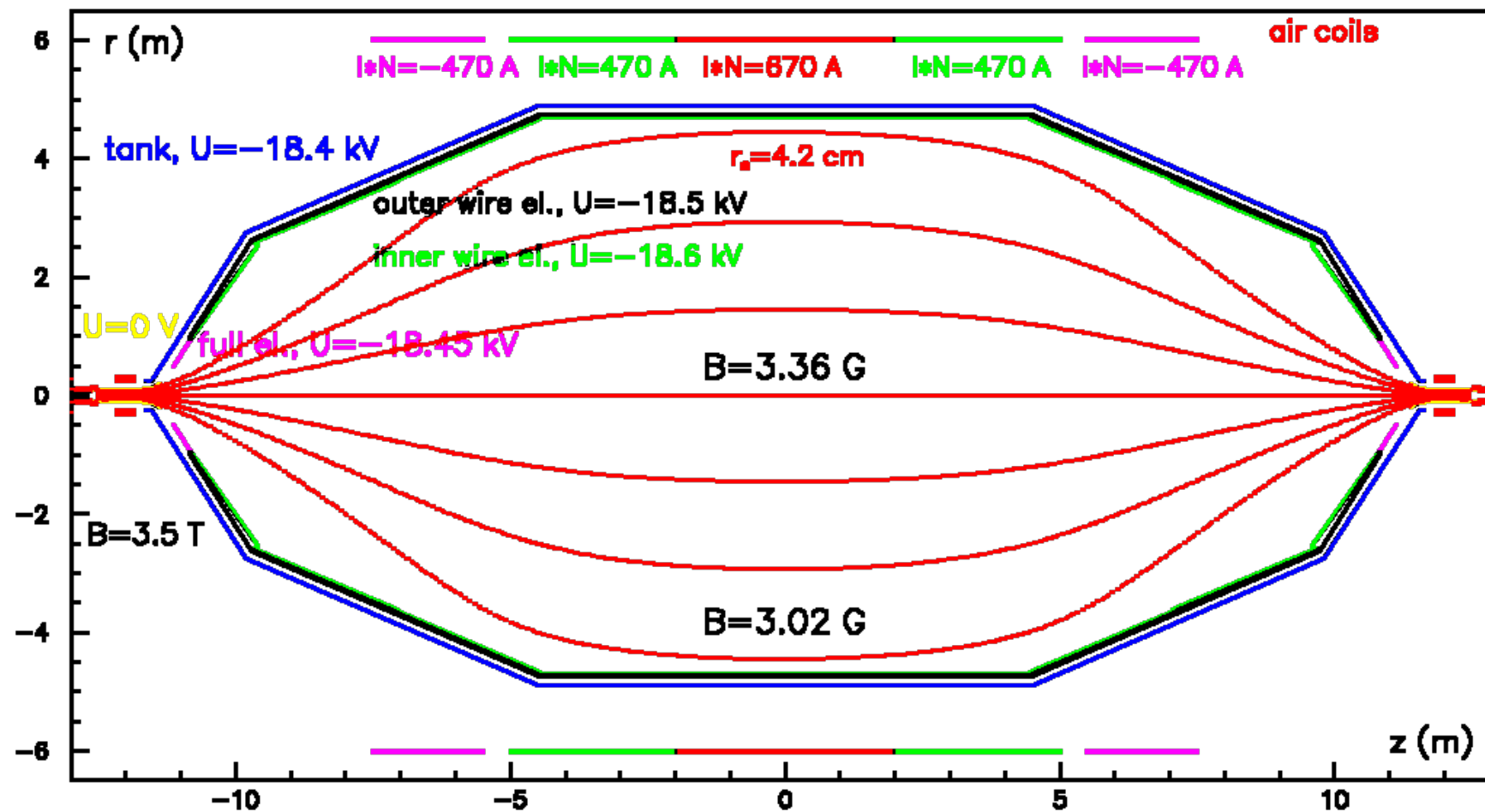


FIG. 1. The major components of the KATRIN beam line consist of a) the Rear Section for diagnostics, b) the windowless gaseous tritium source WGTS, c) the pumping section with the DPS and CPS cryostats, and a tandem set-up of two MAC-E-filters: d) the smaller pre-spectrometer and e) the larger main spectrometer with its surrounding aircoil system. This system transmits only the highest-energy β -decay electrons onto f) the solid-state detector where they are counted.



- \sim constant along B lines
- spectrometer acts as an **integrating** high-energy pass filter by virtue of E field

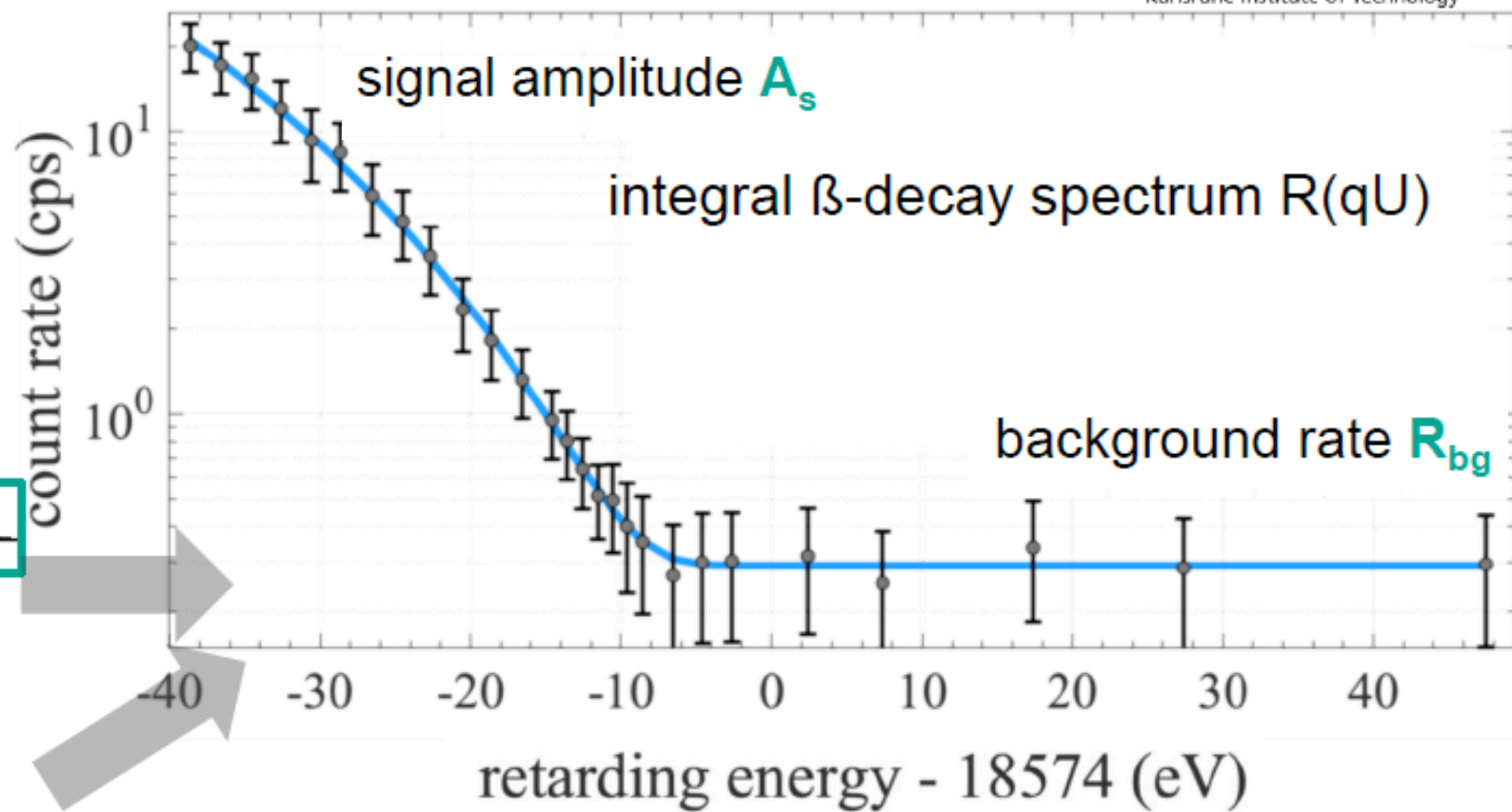
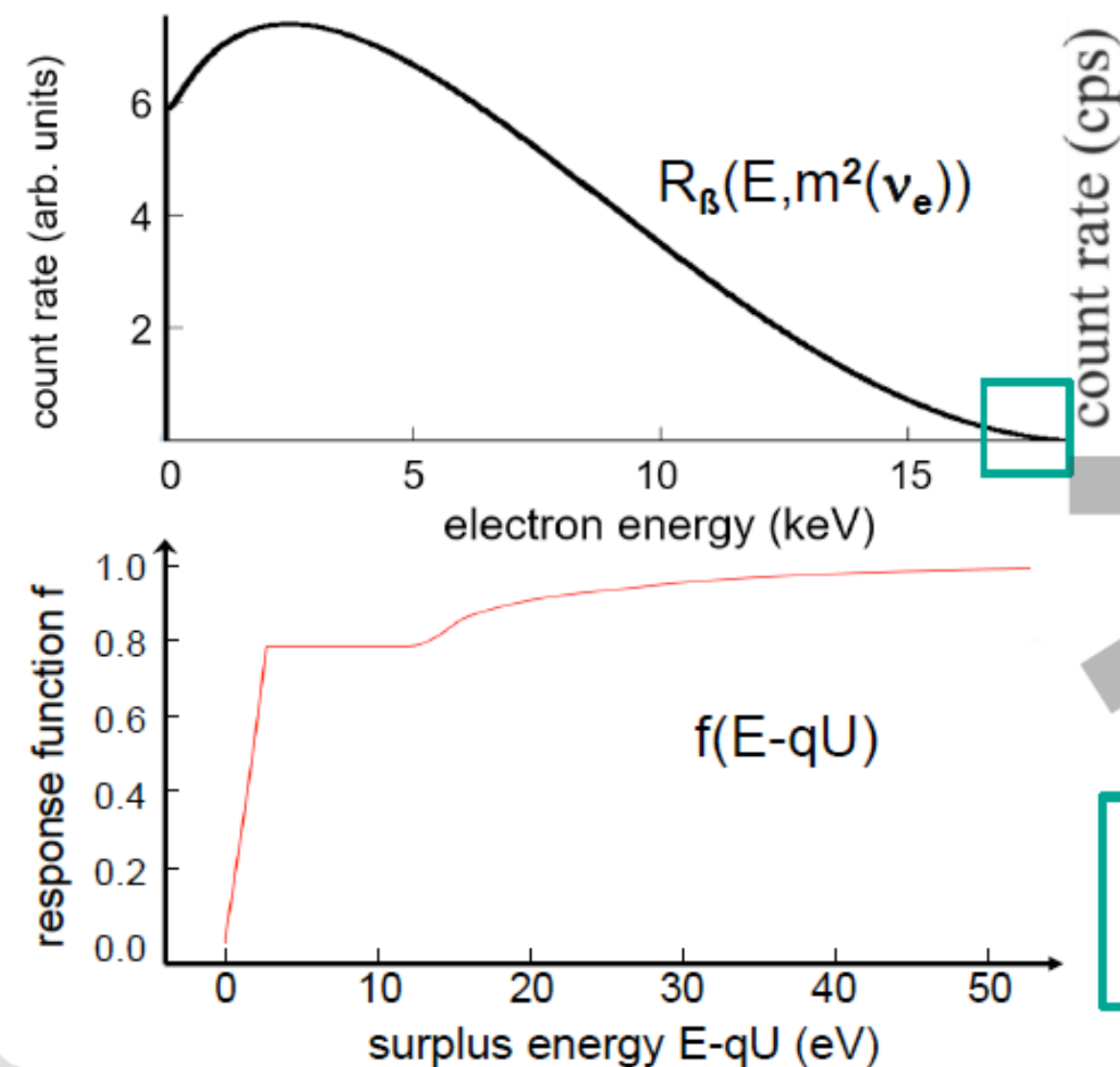


high source activity: $2.45 \cdot 10^{10}$ Bq allowed to collect data for 780h in April 10 – May, 13 2019

lead to first $m_{\nu, \text{eff}}$ limit in 2019

modelling of experimental data

■ β -spectrum \otimes response function



$$R(qU) = A_s \cdot N_T \int_{qU}^{E_0} R_{\beta}(E, m^2(\nu_e)) \cdot f(E - qU) dE + R_{bg}$$

analysis chain & ν -mass result

■ two independent analysis methods

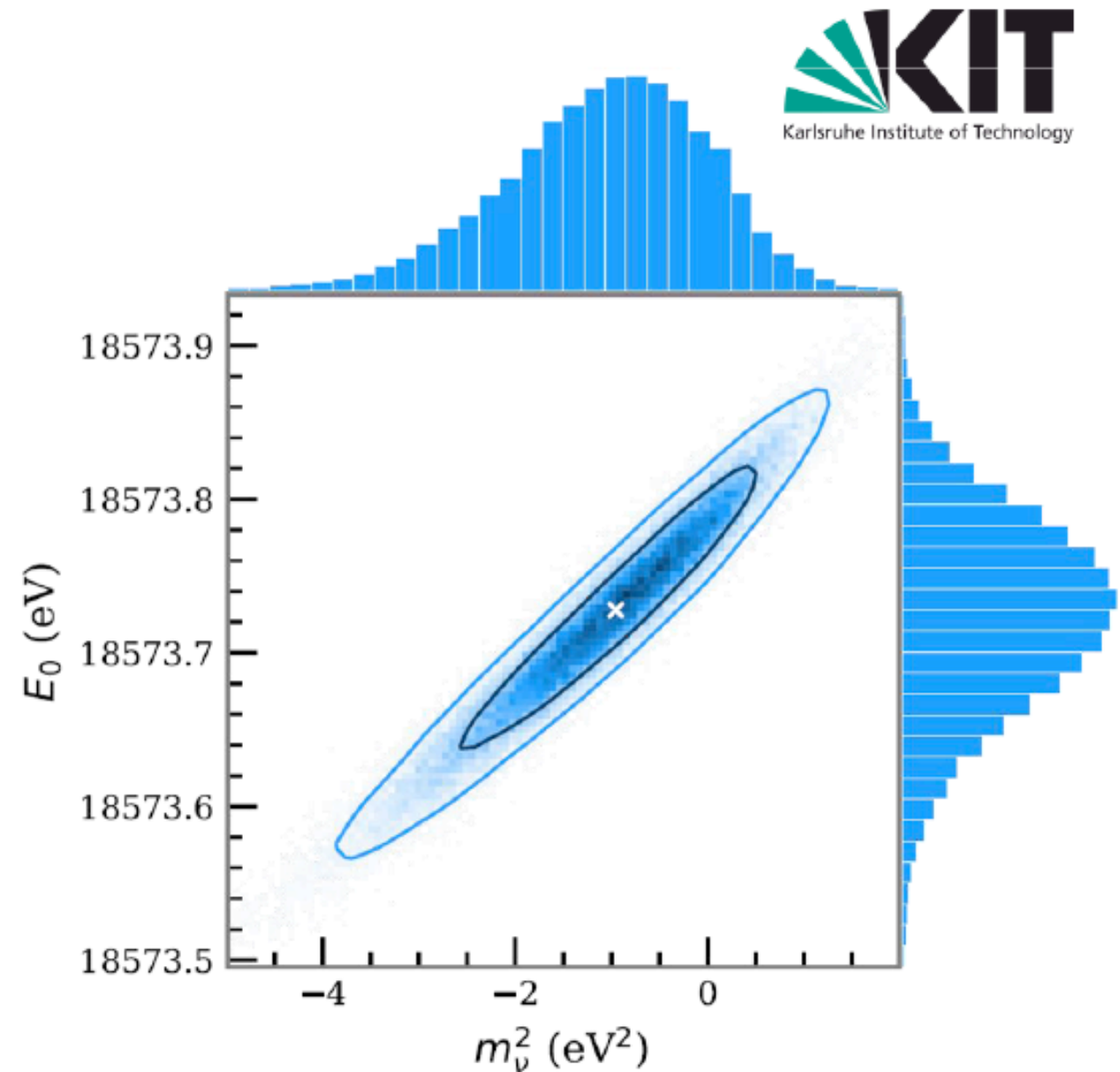
to propagate uncertainties & infer parameters

- **Covariance matrix:**
covariance matrix + χ^2 -estimator
- **MC propagation:**
 10^5 MC samples + likelihood ($-2 \ln \mathcal{L}$)
- both methods agree to a few percent

■ ν -mass and E_0 : best fit results

$$m^2(\nu_e) = \left(-1.0^{+0.9}_{-1.1} \right) \text{eV}^2 \text{ (90\% CL)}$$

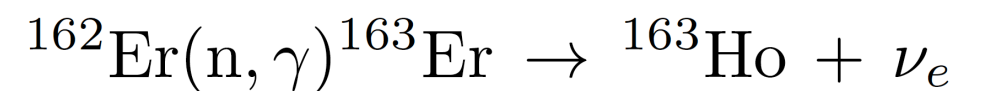
$$E_0 = (18573.7 \pm 0.1) \text{ eV} \Rightarrow \text{Q-value} : (18575.2 \pm 0.5) \text{ eV} \quad \text{Q-value } [\Delta M(^3\text{H}, ^3\text{He})]: (18575.72 \pm 0.07) \text{ eV}$$



Main issues

- Measuring the energy with micro-calorimeters with high resolution
- Estimate doubles=overlaps and their bias on Q end-point
- Keep background under control

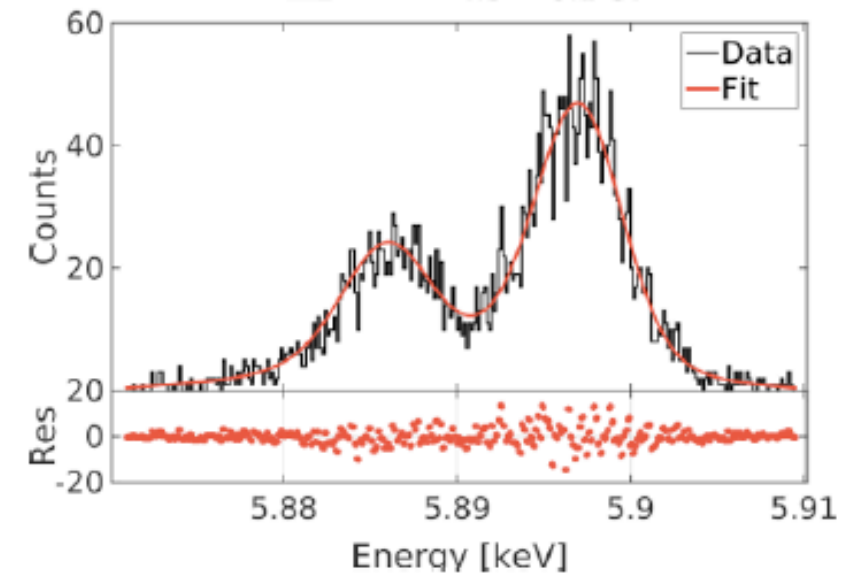
Er161 3.21 h 3/2- EC	Er162 0+ 0.14	Er163 75.0 m 5/2- EC	Er164 0+ 1.61	Er165 10.36 h 5/2- EC	Er166 0+ 33.6
Ho160 25.6 m 5+ EC *	Ho161 2.48 h 7/2- EC *	Ho162 15.0 m 1+ EC *	Ho163 1.70 y 1/2- EC	Ho164 29 m 1+ EC,β- *	Ho165 2.2- 100
Dy159 144.4 d 3/2- EC	Dy160 0+ 2.34	Dy161 5/2+ 18.9	Dy162 0+ 25.5	Dy163 5/2- 24.9	Dy164 0+ 28.2
Tb158 180 y 3- EC,β- *	Tb159 3/2+ 100	Tb160 72.3 d 3- β-	Tb161 6.88 d 3/2+ β-	Tb162 7.60 m 1- β-	Tb163 19.5 m 3/2+ β-



- ^{163}Ho source mostly from neutron irradiation of ^{163}Er
- decays quickly ($\tau \sim 75$ min) and large x-sec: effective process
- but mind radioactive impurities from other elements emitting below 5 keV!

Source production and purification:

130 MBq available for tests and experiments

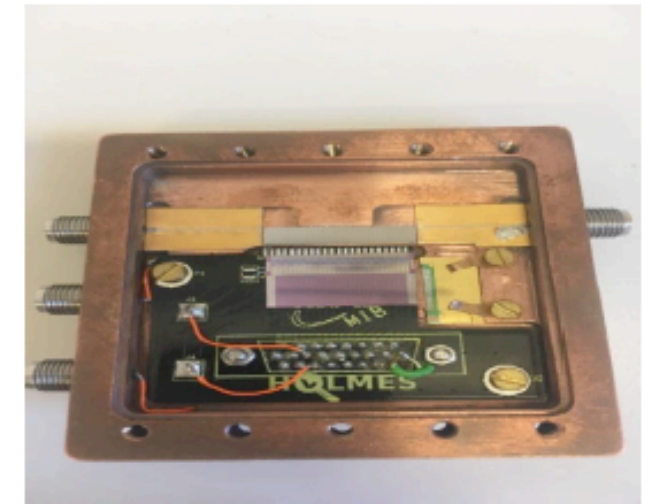


Detector arrays characterization:

very good single pixel performance

operating microwave SQUID multiplexing

next challenge → load TES arrays with ^{163}Ho

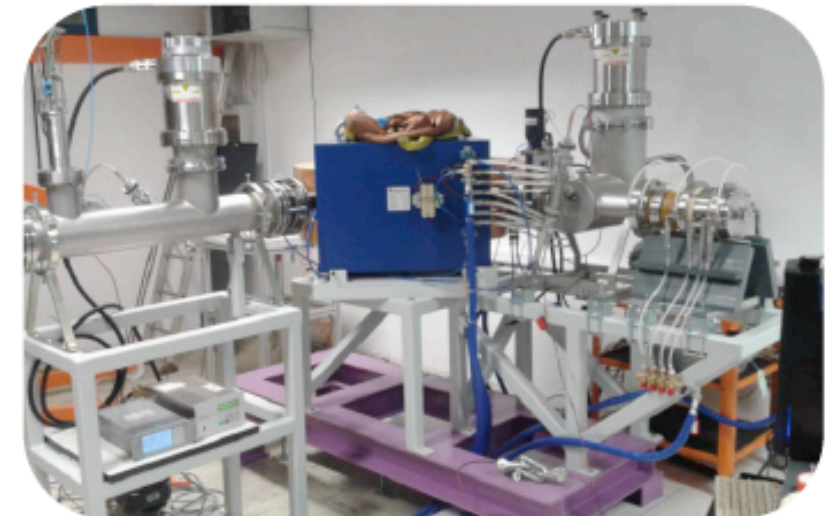


Dedicated mass separator:

facility installed

tests of the ion source on-going

commissioning on-going

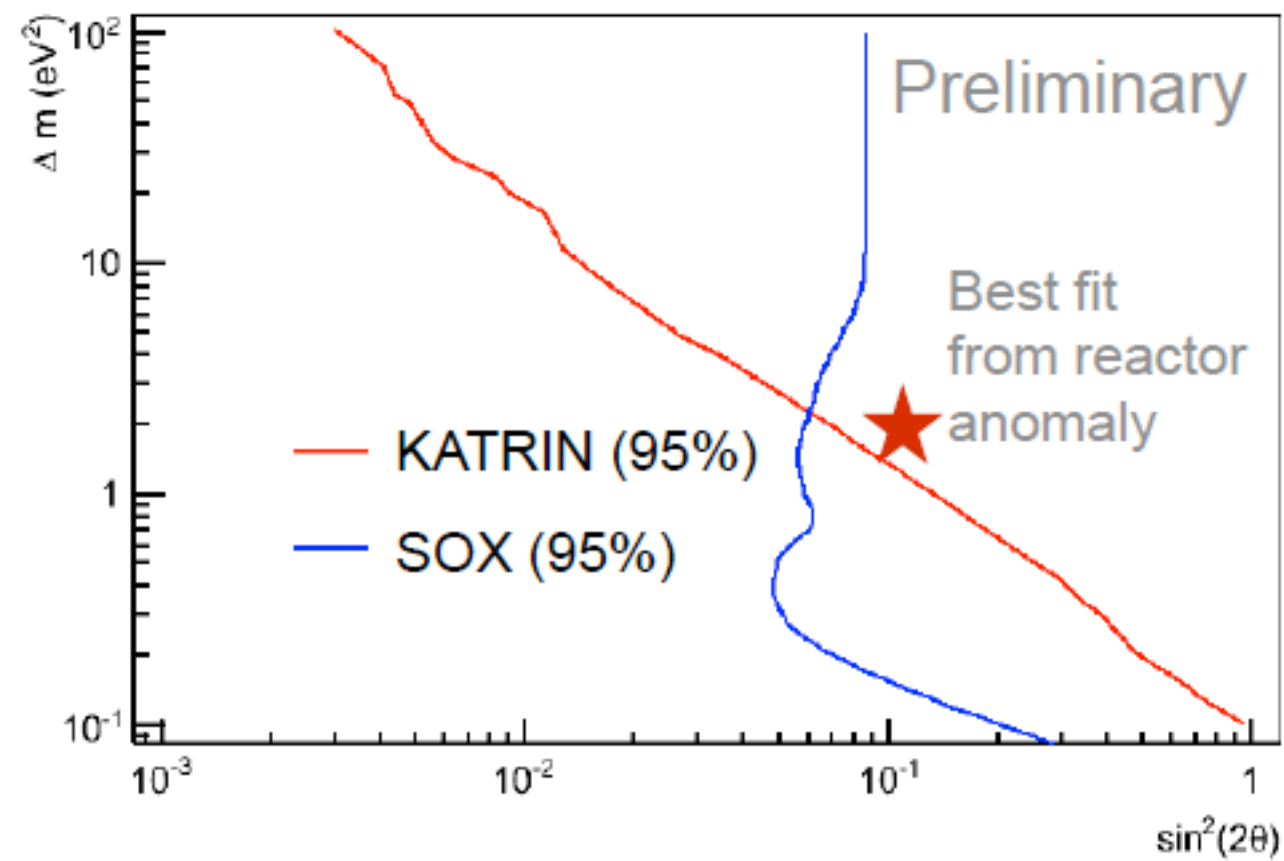


- full scale (starting 2019):
 - 1000 channels,
 - $t_M = 3$ years (3×10^{13} events)
 - $m(\nu_e) < 1$ eV

Project 8 Goals

- Demonstrate that CRES can be used to measure the tritium endpoint in a small prototype
(right now, “Phase II”)
- Scale to a large-volume system that has sufficient statistics to contribute to the global neutrino mass effort and serve as a intermediate step for an atomic experiment
(near future, “Phase III”)
- Transition to an atomic tritium measurement and make the most sensitive measurement of the neutrino mass possible
(future, “Phase IV”)

eV-scale sterile neutrinos

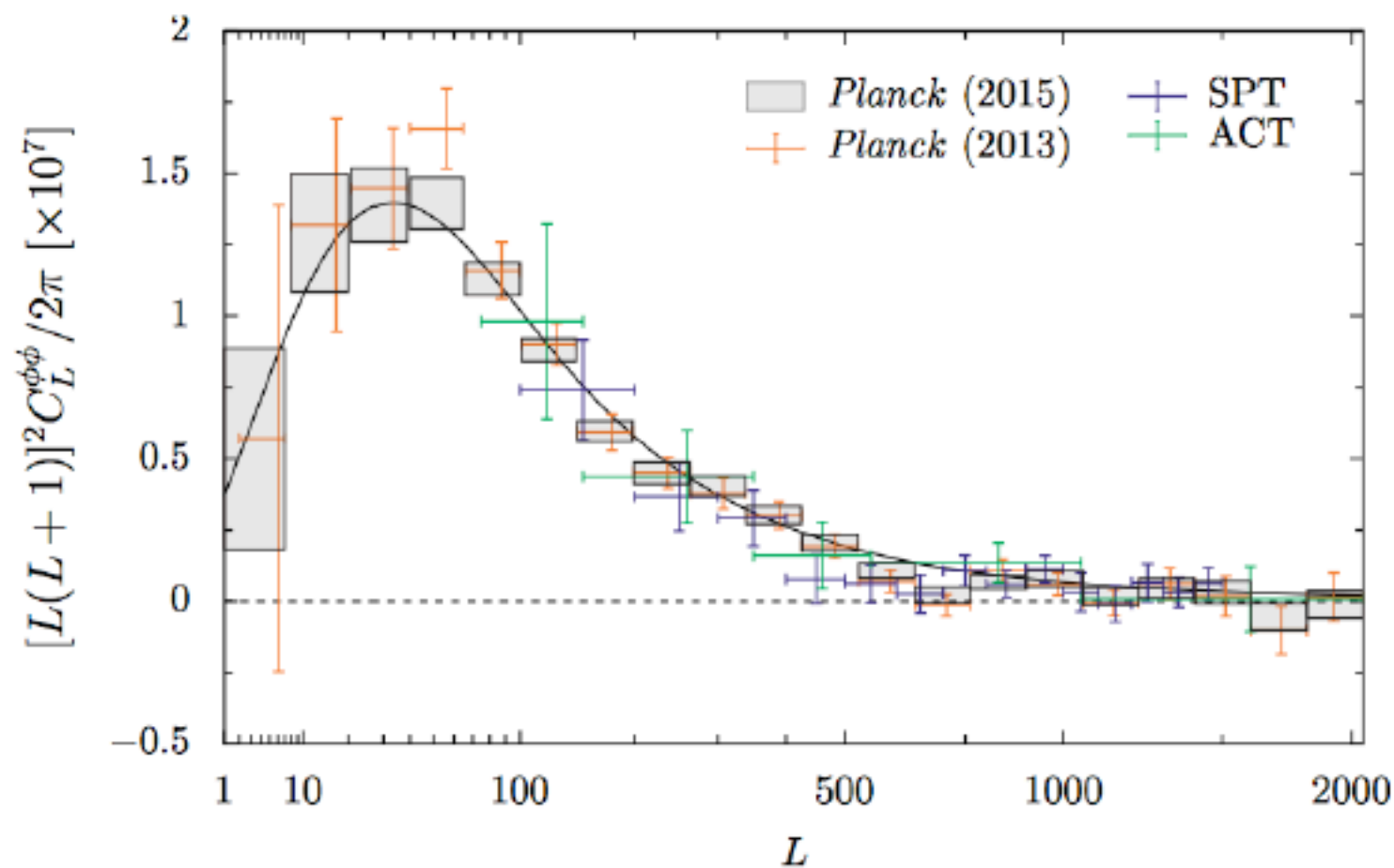
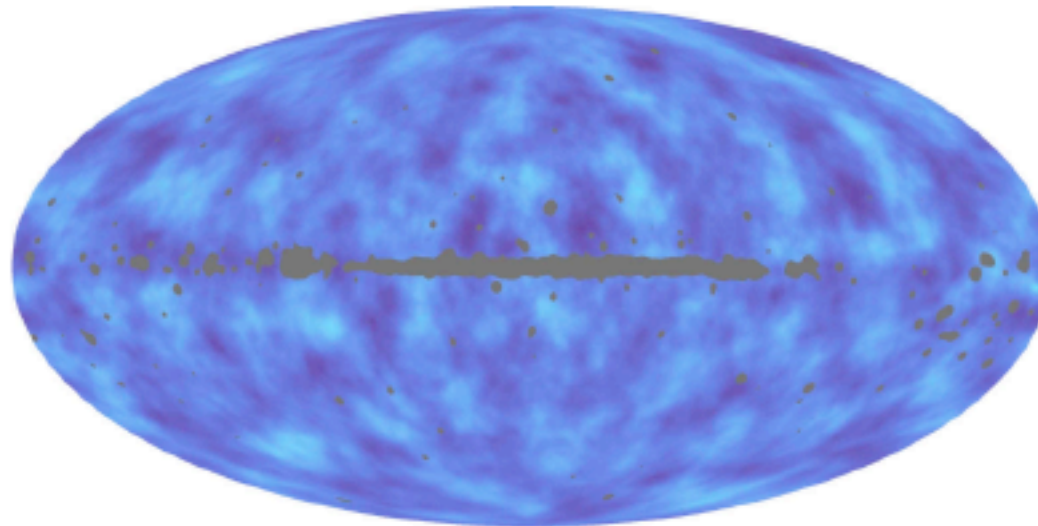


KATRIN **as is** probes the favored parameter space for light sterile neutrinos and is complementary to oscillation experiments

SOX at Borexino

first proposed (AFAIK...):
Phys.Rev. D73 (2006)
045021

CMB lensing potential



LARGE SCALE STRUCTURES

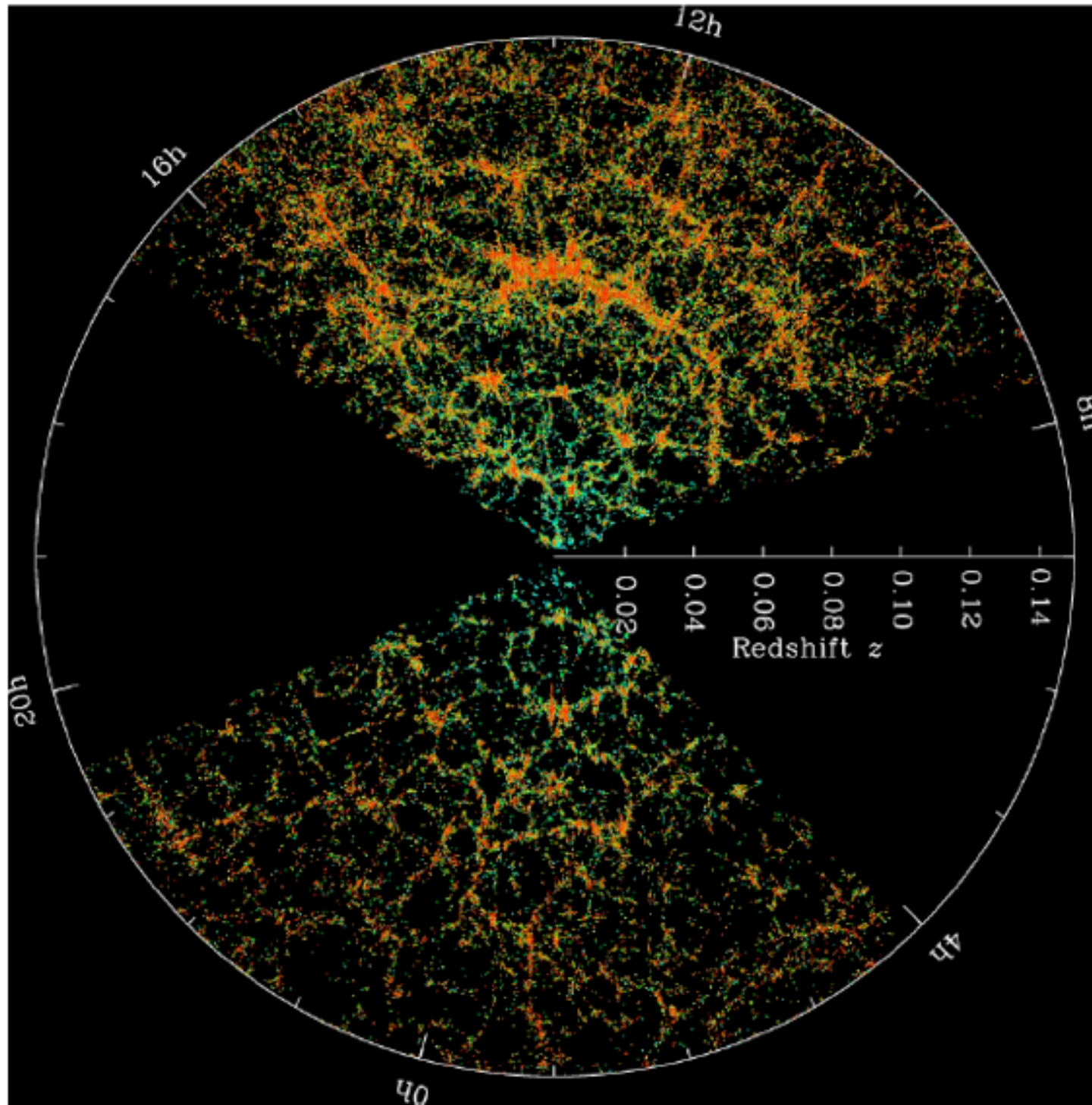
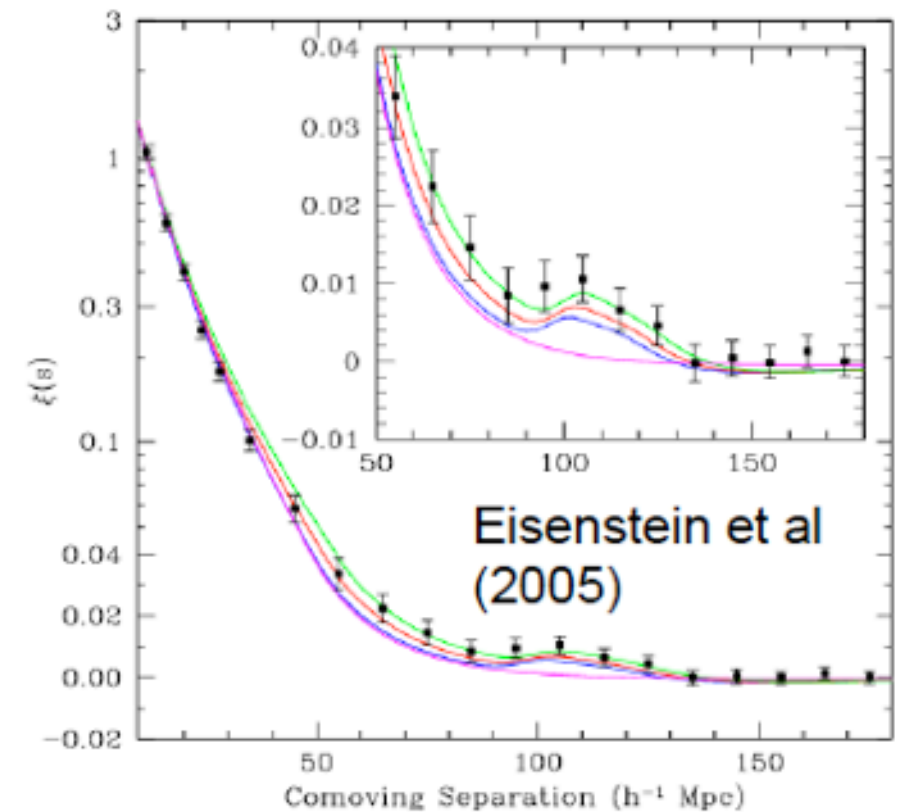
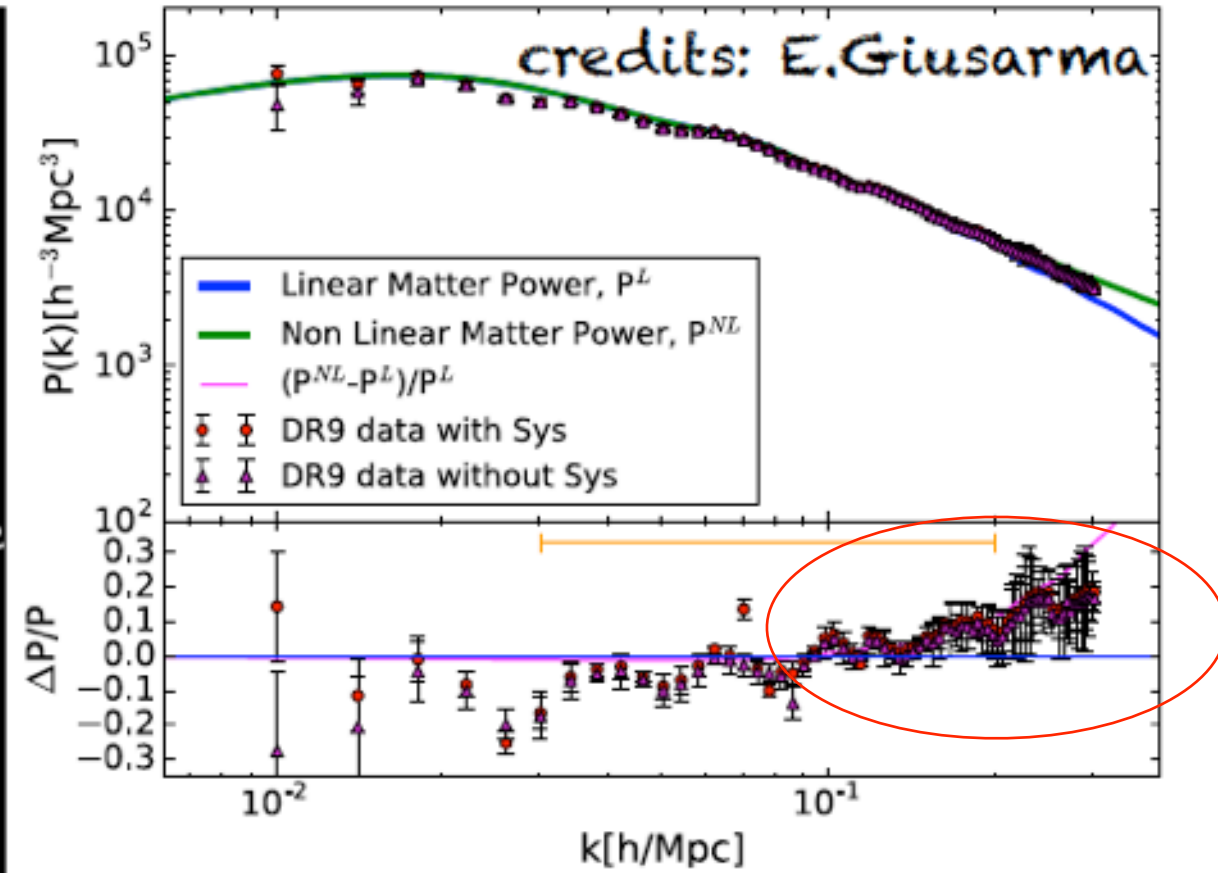


Image Credit: M. Blanton and the Sloan Digital Sky Survey.

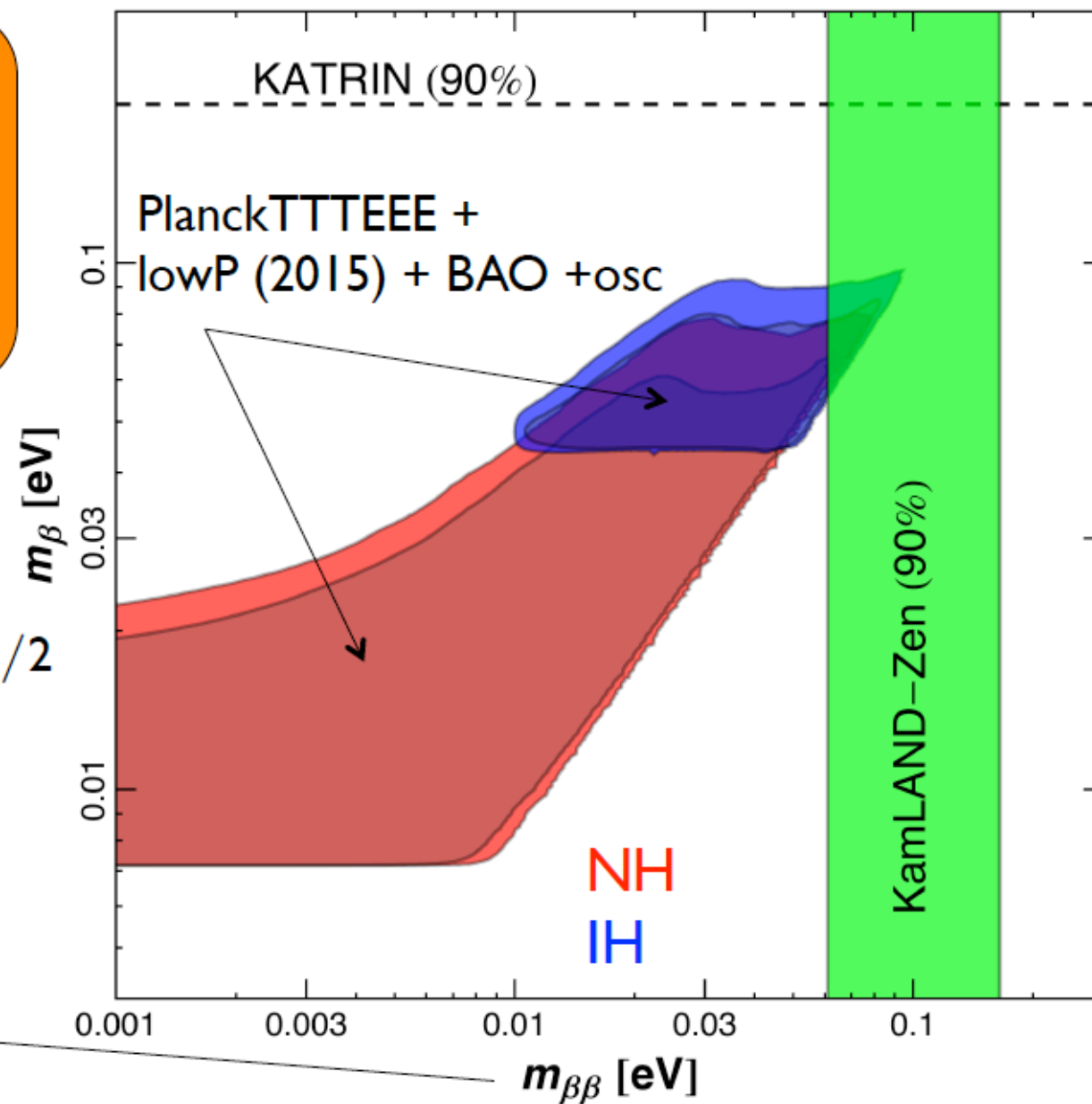


95% constraints on total mass	<i>Planck</i> TT	<i>Planck</i> TTTEEE
+lowP	<0.72 eV	<0.49 eV
+lowP+lensing	<0.68 eV	<0.59 eV
+lowP+BAO	<0.21 eV	<0.17 eV
+lowP+ext	<0.20 eV	<0.15 eV
+lowP+lensing+ext	<0.23 eV	<0.19 eV

Cosmology constraints can be combined with data from oscillation experiments

$$m_{\beta} \equiv \left[\sum |U_{ei}|^2 m_i^2 \right]^{1/2}$$

$$m_{\beta\beta} \equiv \left| \sum U_{ei}^2 m_i \right|$$



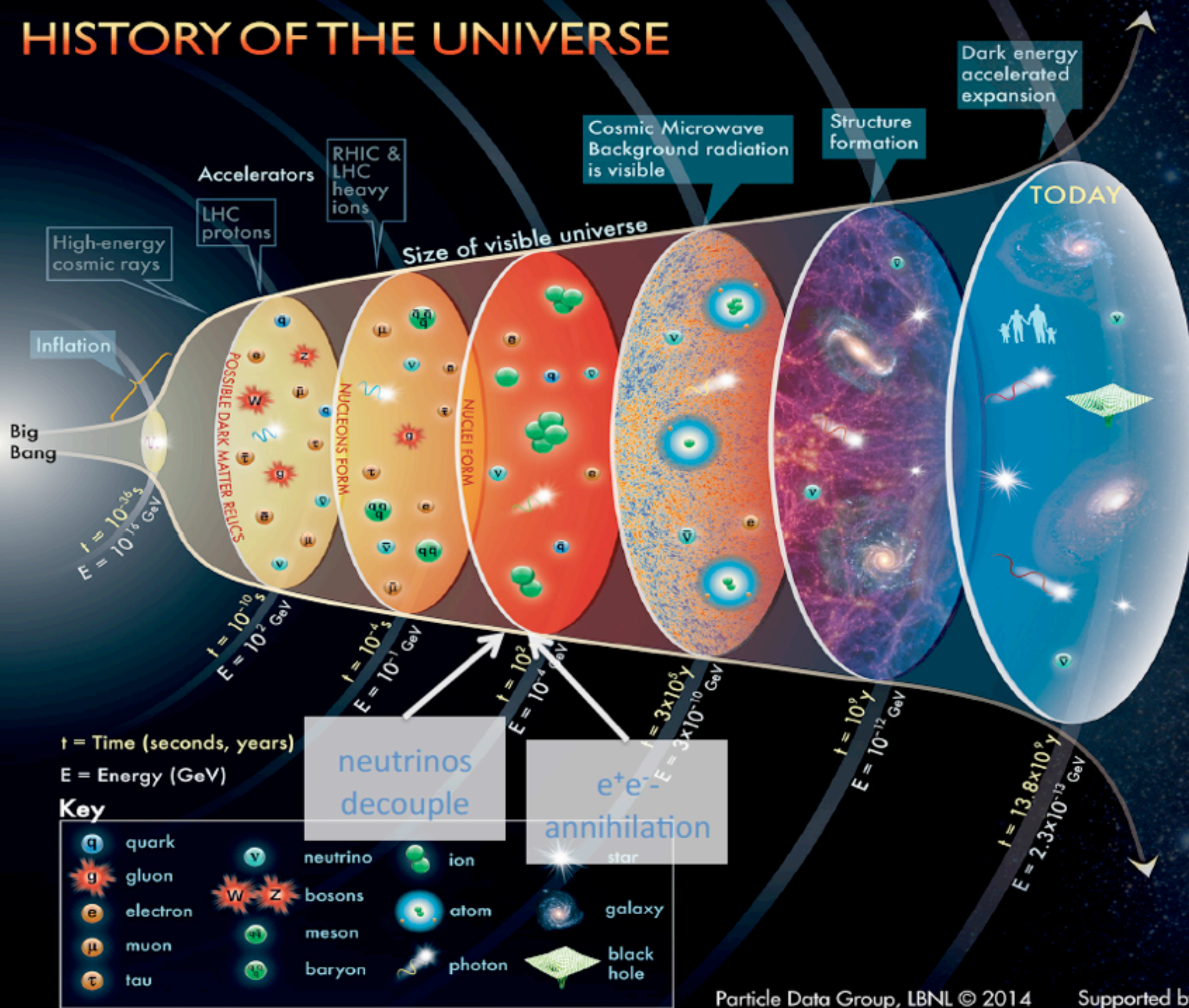
Cosmological constraints

(for more see e.g. seminar by Lattanzi at
Roma Tre, 10th Jan 2017)

- cosmological observations

$$\sum m_\nu \equiv \sum_i m_i \quad (0.2 - 0.7 \text{ eV @ 95\%CL})$$

HISTORY OF THE UNIVERSE



Particle Data Group, LBNL © 2014

Supported by DOE

The Cosmic Neutrino Background - Properties

At freeze out the neutrinos had a thermal velocity distribution.

Since then the neutrinos have continued to move along geodesics with a velocity which has red-shifted as a result of the expansion of the universe.

This geodesic movement is called *free streaming*.

These free-streaming neutrinos make up the *cosmic neutrino background*.

- Below $T \sim 1$ MeV, neutrino free stream keeping an equilibrium spectrum:

$$f_{\nu}(p) = \frac{1}{e^{p/T} + 1}$$

- Today $T_{\nu} = 1.9$ K and $n_{\nu} = 113$ part/cm³ per species

Constraints from the Neutrino Background

In standard cosmologies, the cosmological neutrino background only interacts gravitationally after freeze-out and *all cosmological bounds on neutrino masses arise from gravitational interactions of the cosmic neutrino background.*

The gravitational interaction depends on the sum of the gravity from all of the neutrinos, which is proportional to the sum of the masses once the neutrinos have become nonrelativistic.

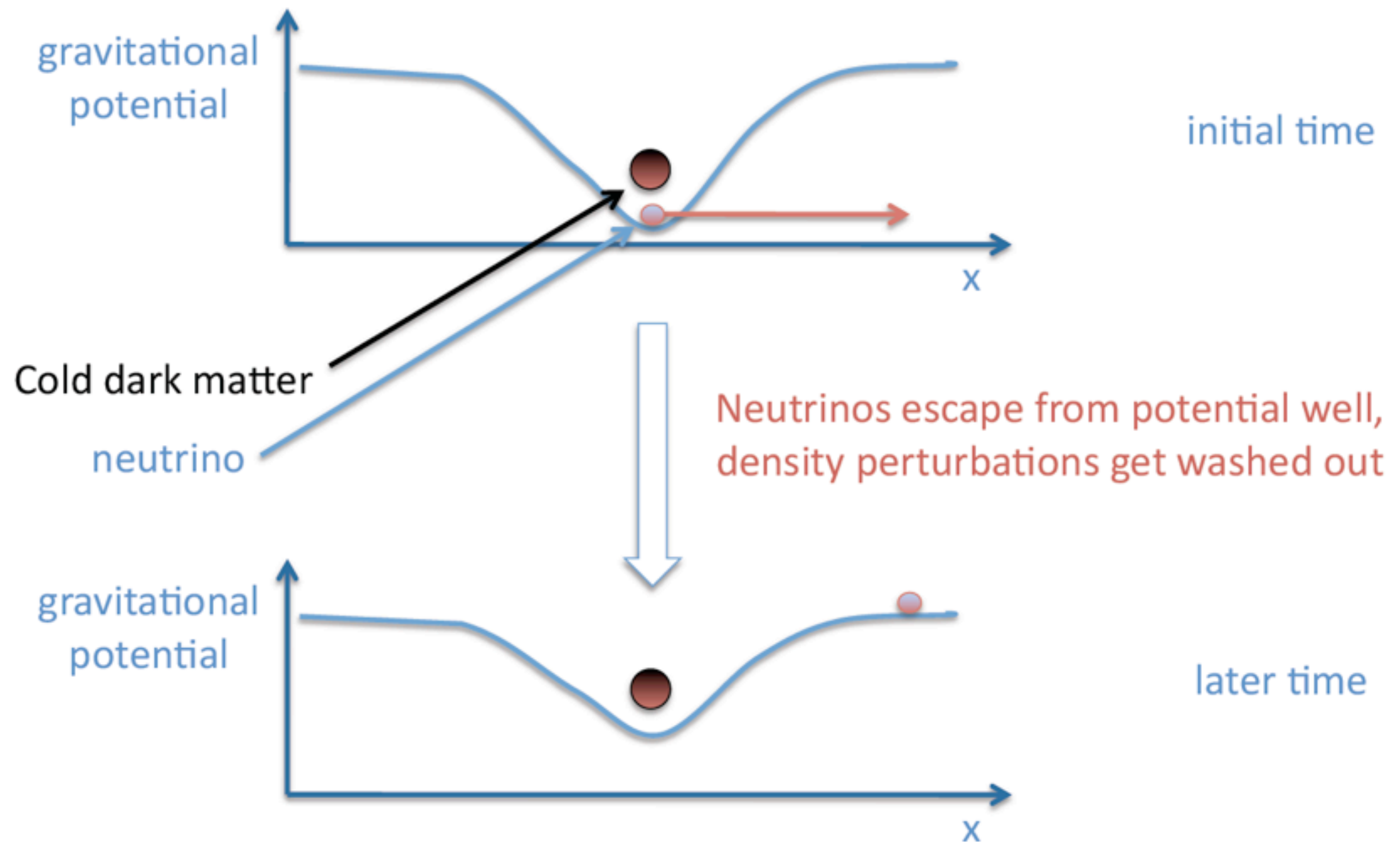
This is why cosmology constrains the sum of the masses.

➡ Effects:

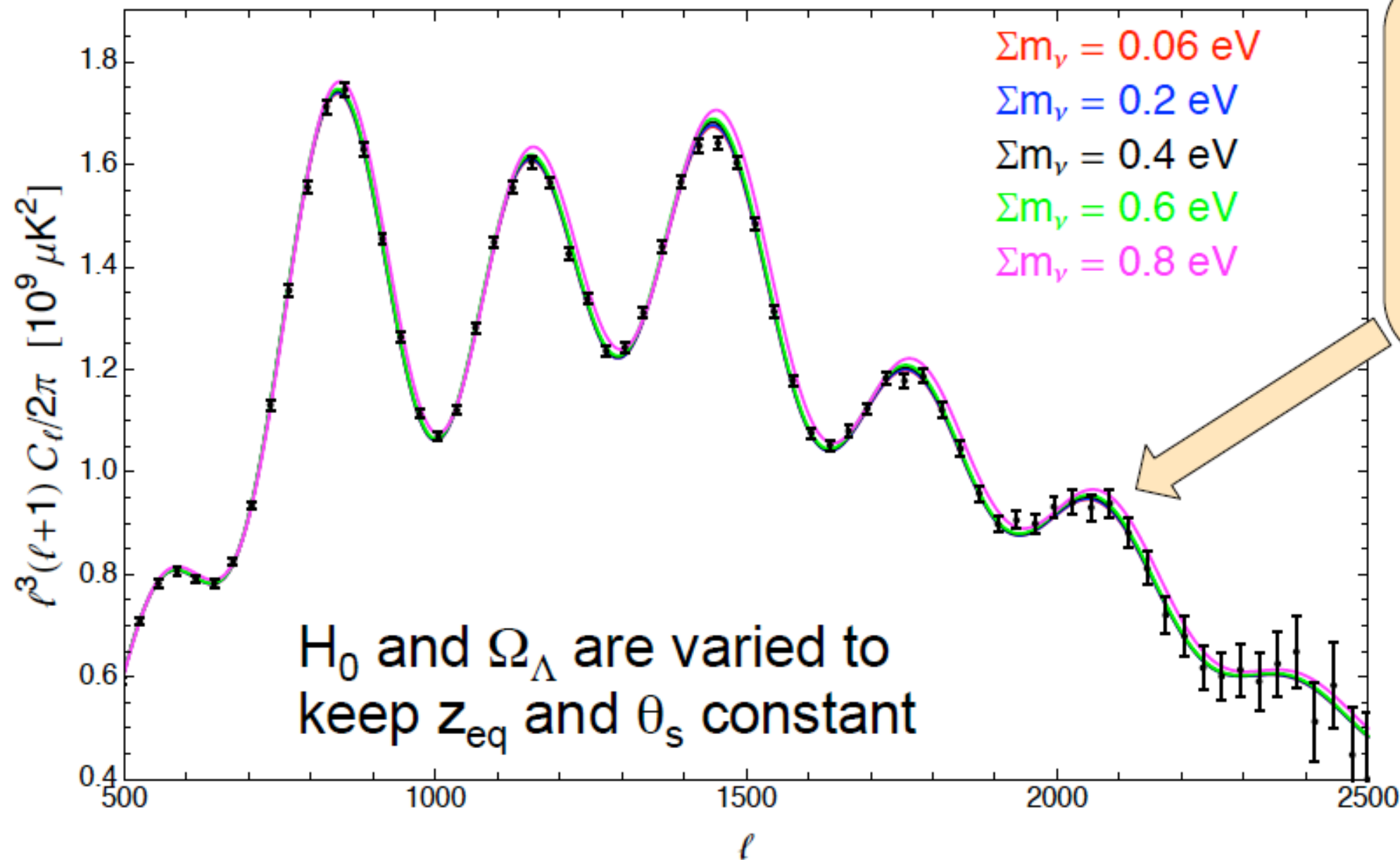
- I) They contribute to the recent expansion of the universe identically to dark matter.
- II) Since freeze out they free stream a distance called the *free-streaming length*. This disrupts structure formation on scales below the free-streaming length.

Free streaming

*Velocity dispersion **large** wrt size of potential well*



HOW HEAVY?



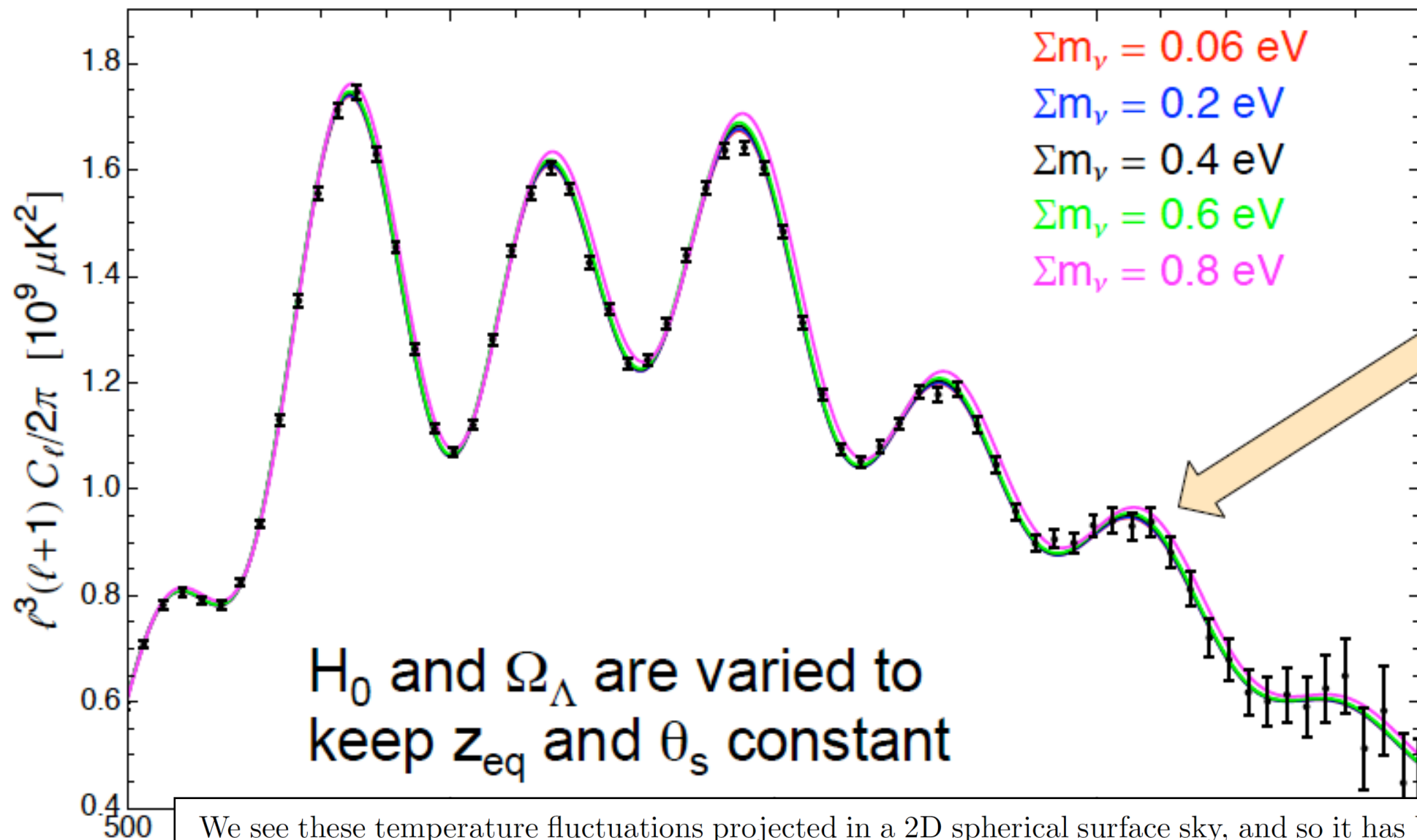
Net effect
is to
decrease
lensing

Perturbations: free streaming, damping of small-scale perturbations

- proportional to the neutrino energy density
- the effect is larger for larger masses

Model-dependent: interplay with Λ_{CDM} , H_0

HOW HEAVY?



Net effect
is to
decrease
lensing

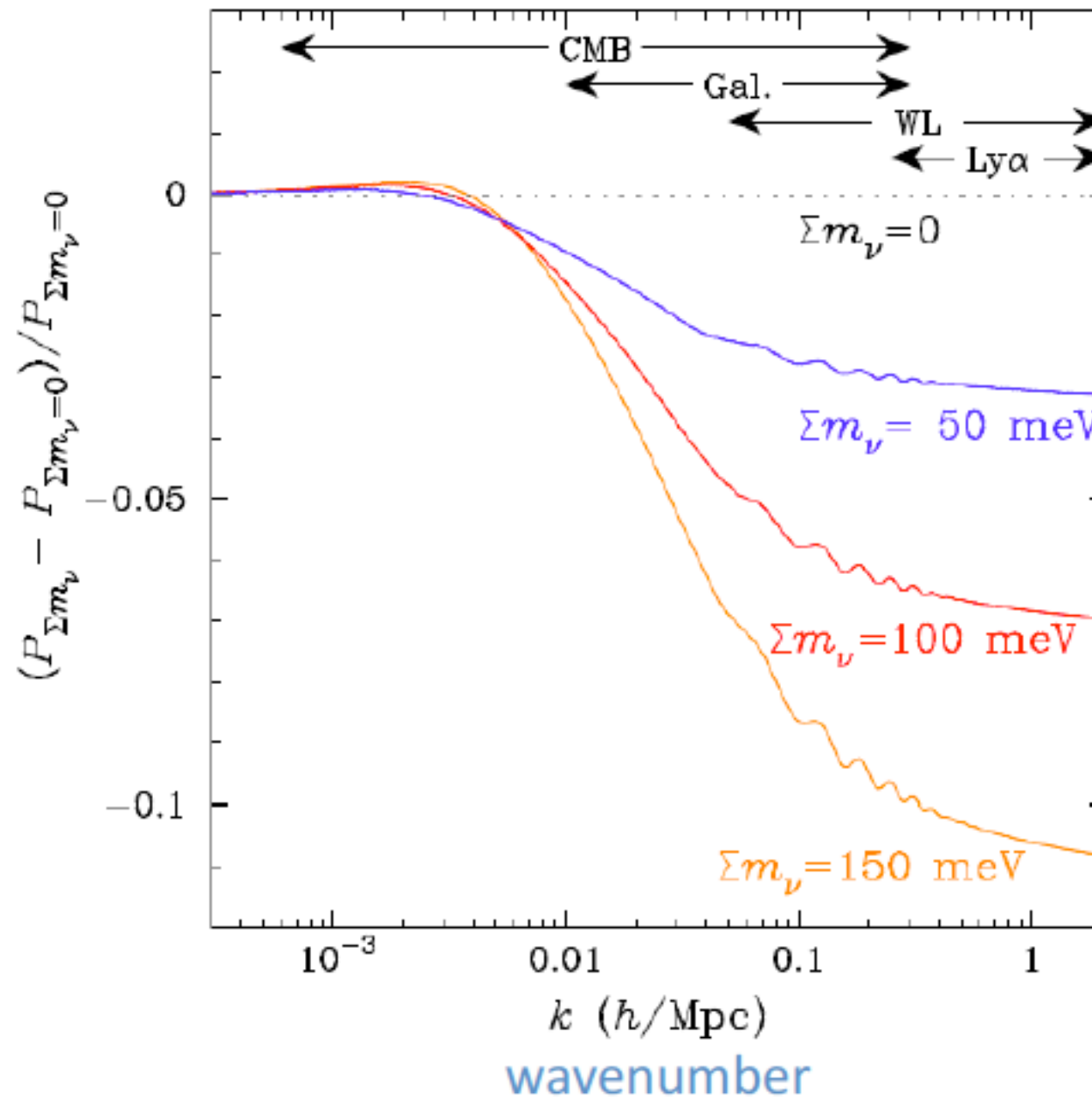
We see these temperature fluctuations projected in a 2D spherical surface sky, and so it has become common in the literature to expand the temperature field using spherical harmonics. The spherical harmonics form a complete orthonormal set on the unit sphere and are defined as

$$Y_{lm} = \sqrt{\frac{2\ell+1}{4\pi} \frac{(\ell-m)!}{(\ell+m)!}} P_\ell^m(\cos\theta) e^{im\phi} \quad (2)$$

where the indices $\ell = 0, \dots, \infty$ and $-\ell \leq m \leq \ell$ and P_ℓ^m are the Legendre polynomials. ℓ is called the multipole and represents a given angular scale in the sky α , given approximately by $\alpha = \pi/\ell$ (in degrees).

Matter power spectrum with massive neutrinos (at low redshifts)

Suppression of the matter power spectrum
wrt massless neutrino case



$$\Delta \mathcal{P} / \mathcal{P} \approx 8 \frac{\omega_\nu}{\omega_m}$$

ratio of density of ν to matter (=non-relativistic particles) in the present universe

[Figure from Abazajian+ 2013]

FUTURE PROSPECTS FROM THE LAB

The absolute mass scale can be measured through:
(numbers on the right are **forecast for future sensitivities**)

- tritium beta decay

$$m_{\beta} \equiv \left[\sum |U_{ei}|^2 m_i^2 \right]^{1/2} \quad (200 \text{ meV @ 68\%CL})$$

(Katrin)

- neutrinoless double beta decay

$$m_{\beta\beta} \equiv \left| \sum U_{ei}^2 m_i \right| \quad (8 - 20 \text{ meV @ 90\%CL})$$

(nEXO, 5-year exposure)

- cosmological observations

$$\sum m_{\nu} \equiv \sum_i m_i \quad (16 - 45 \text{ meV @ 68\%CL})$$

(CORE, CORE+LSS)

Mass scale: experimental tools / 1



three complementary tools available

→ low temperature detectors play key role

(E. Fiorini and T. Niinikoski, Nucl. Instrum. and Meth. 224, p.83 (1984))



tool	Cosmology CMB+LSS+...	Neutrinoless Double Beta decay	Beta decay end-point
observable	$m_{\Sigma} = \sum_k m_{\nu_k}$	$m_{\beta\beta} = \sum_k m_{\nu_k} U_{ek}^2 $	$m_{\beta} = (\sum_k m_{\nu_k}^2 U_{ek} ^2)^{1/2}$
present sensitivity	≈ 0.1 eV	≈ 0.1 eV	2 eV
future sensitivity	0.05 eV	0.05 eV	0.2 eV
model dependency	yes ☹️	yes ☹️	no 😊
systematics	large ☹️	yes 😐	large ☹️

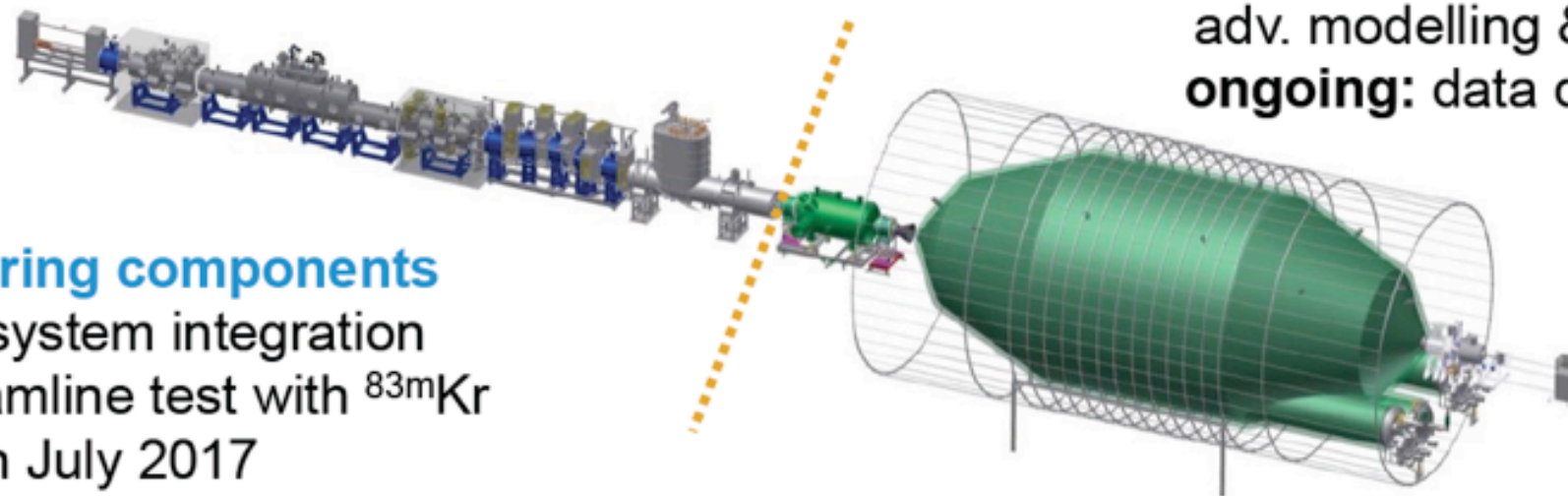
Summary & outlook

- ▶ β decay allows model-independent, **direct** access to neutrino mass scale
- ▶ KATRIN will exhaust degenerate mass regime: **200 meV** (90% CL for 5 yrs of running); reaching sub-eV sensitivity with first few weeks of data
- ▶ Interesting physics potential beyond m_ν : eV and keV scale sterile ν , RH currents, LIV, ...

Preparing KATRIN for neutrino-mass measurements:

Tritium-bearing components

- now: final system integration
- overall beamline test with ^{83m}Kr achieved in July 2017
- **next**: inactive commissioning with D_2 , then $\text{D}_2(\text{T}_2)$



Analysis chain

adv. modelling & analysis framework
ongoing: data quality filters, blinding

Spectrometer & detector section

2 successful commissioning phases already done
ongoing: background investigations

→ **First tritium runs starting in 2018, inauguration ceremony: 11 June 2018**