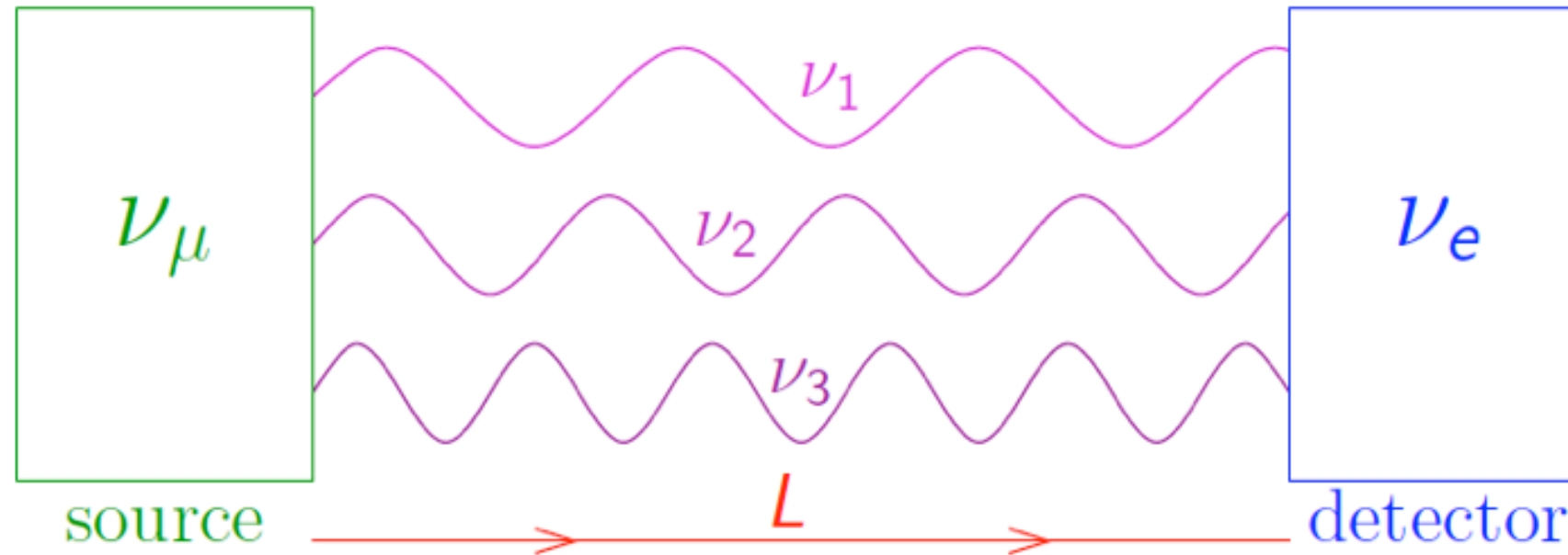


Lecture 4: LBL/accelerators

PhD Cycle XXXIV

Neutrino Oscillations

$$|\nu(t=0)\rangle = |\nu_\mu\rangle = U_{\mu 1} |\nu_1\rangle + U_{\mu 2} |\nu_2\rangle + U_{\mu 3} |\nu_3\rangle$$



$$|\nu(t > 0)\rangle = U_{\mu 1} e^{-iE_1 t} |\nu_1\rangle + U_{\mu 2} e^{-iE_2 t} |\nu_2\rangle + U_{\mu 3} e^{-iE_3 t} |\nu_3\rangle \neq |\nu_\mu\rangle$$

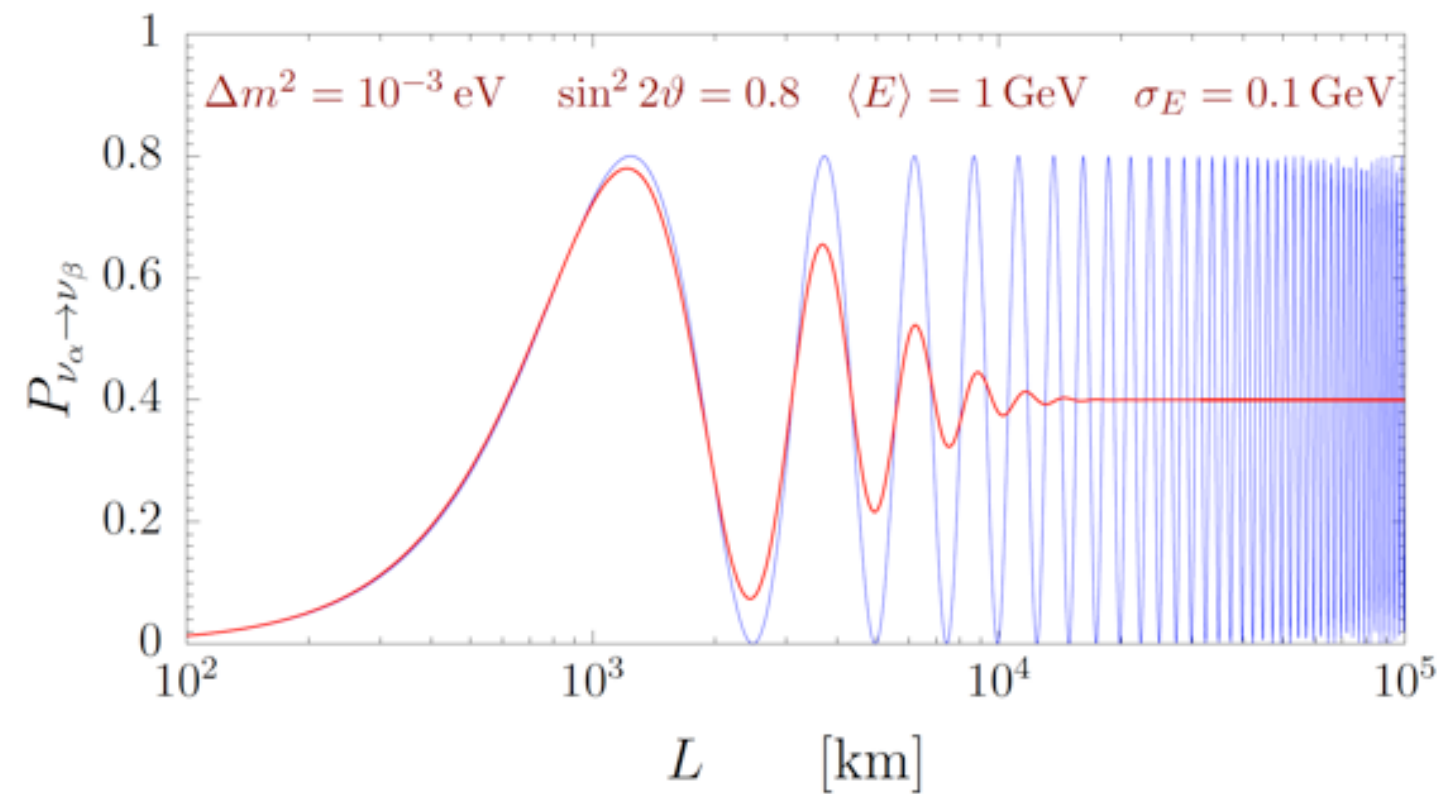
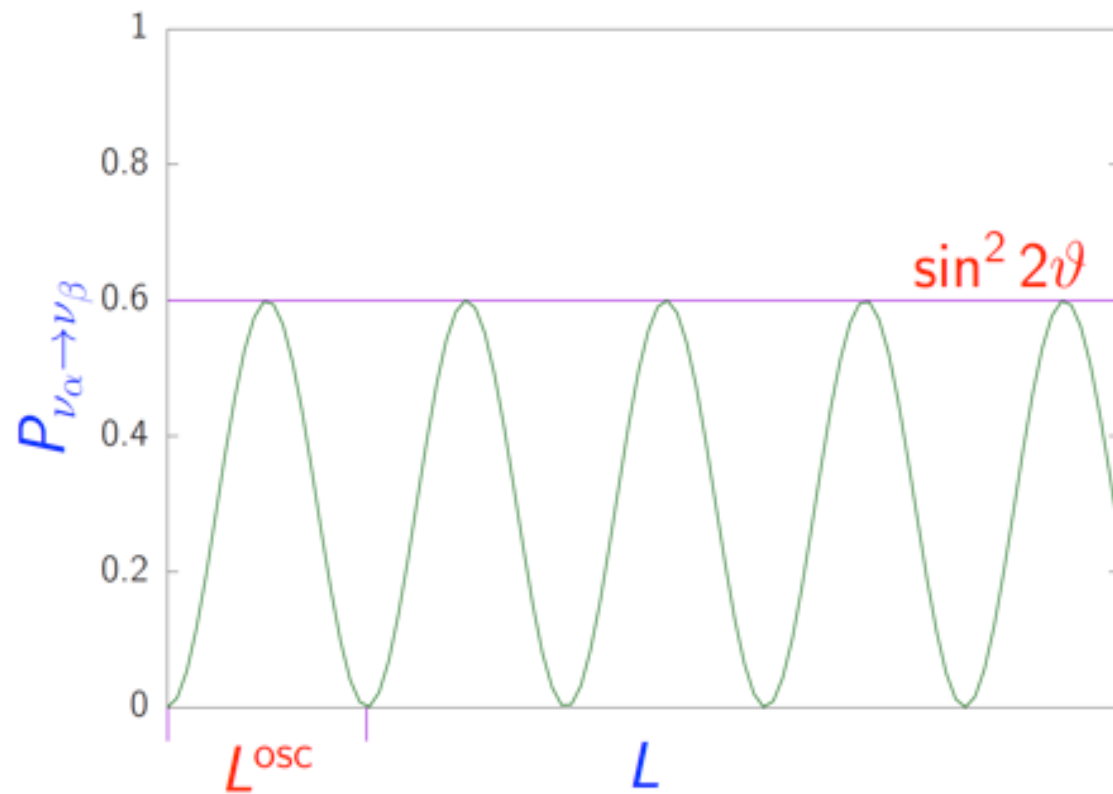
$$E_k^2 = p^2 + m_k^2$$

$$P_{\nu_\mu \rightarrow \nu_e}(t > 0) = |\langle \nu_e | \nu(t > 0) \rangle|^2 \sim \sum_{k>j} \text{Re}[U_{ek} U_{\mu k}^* U_{ej}^* U_{\mu j}] \sin^2 \left(\frac{\Delta m_{kj}^2 L}{4E} \right)$$

transition probabilities depend on U and $\Delta m_{kj}^2 \equiv m_k^2 - m_j^2$

$$\begin{array}{cccc} \nu_e \rightarrow \nu_\mu & \nu_e \rightarrow \nu_\tau & \nu_\mu \rightarrow \nu_e & \nu_\mu \rightarrow \nu_\tau \\ \bar{\nu}_e \rightarrow \bar{\nu}_\mu & \bar{\nu}_e \rightarrow \bar{\nu}_\tau & \bar{\nu}_\mu \rightarrow \bar{\nu}_e & \bar{\nu}_\mu \rightarrow \bar{\nu}_\tau \end{array}$$

2 ν -mixing: $P_{\nu_\alpha \rightarrow \nu_\beta} = \sin^2 2\vartheta \sin^2 \left(\frac{\Delta m^2 L}{4E} \right) \Rightarrow \boxed{L^{\text{osc}} = \frac{4\pi E}{\Delta m^2}}$



Tiny neutrino masses lead to observable macroscopic oscillation distances!

{	$10 \frac{\text{m}}{\text{MeV}} \left(\frac{\text{km}}{\text{GeV}} \right)$	short-baseline experiments	$\Delta m^2 \gtrsim 10^{-1} \text{ eV}^2$
	$10^3 \frac{\text{m}}{\text{MeV}} \left(\frac{\text{km}}{\text{GeV}} \right)$	long-baseline experiments	$\Delta m^2 \gtrsim 10^{-3} \text{ eV}^2$
	$10^4 \frac{\text{km}}{\text{GeV}}$	atmospheric neutrino experiments	$\Delta m^2 \gtrsim 10^{-4} \text{ eV}^2$
	$10^{11} \frac{\text{m}}{\text{MeV}}$	solar neutrino experiments	$\Delta m^2 \gtrsim 10^{-11} \text{ eV}^2$

Neutrino oscillations are the optimal tool to reveal tiny neutrino masses!

SOURCE	Flavour	Distance	Energy	Min Δm^2
Sun	ν_e	$\sim 1.5 \times 10^8 \text{ km}$	0.2 – 15 MeV	$\sim 10^{-11} \text{ eV}^2$
CR	$\nu_\mu, \bar{\nu}_\mu, \nu_e, \bar{\nu}_e$	10 km – 13000 km	0.2 GeV – 100 GeV	$\sim 10^{-4} \text{ eV}^2$
Reactors	$\bar{\nu}_e$	20 m – 250 km	$\langle E \rangle \approx 3 \text{ MeV}$	$\sim 10^{-1} - 10^{-6} \text{ eV}^2$
Accelerators	$\nu_\mu, \bar{\nu}_\mu, \nu_e, \bar{\nu}_e$	15 m – 730 km	20 MeV – 100 GeV	$\sim 10^{-3} - 10 \text{ eV}^2$

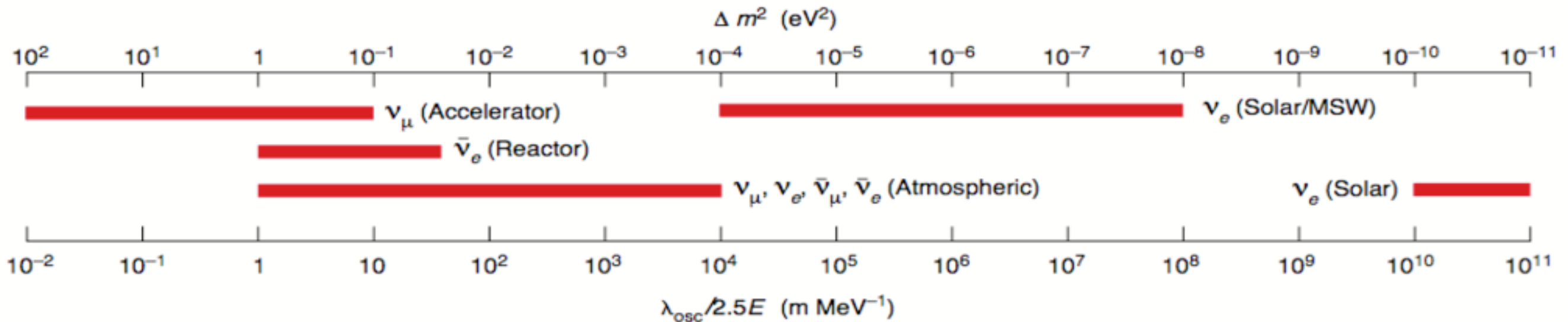


Figure 15. Accessible Ranges of Δm^2

Neutrino energies are specific to the source, and source-to-detector distances also vary with the source. The ratio of these two variables determines the range of values for Δm^2 that neutrino oscillation experiments can measure using each source. These ranges are labeled with the source and the neutrinos produced by that source. Two ranges are given for solar-neutrino experiments. One assumes that the MSW effect enhances oscillations, in which case, the range of Δm^2 is determined in part by the electron density of matter in the Sun. The other assumes no matter enhancement.

Three-Neutrino Mixing Paradigm

Standard Parameterization of Mixing Matrix

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta_{13}} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta_{13}} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & e^{i\lambda_{21}} & 0 \\ 0 & 0 & e^{i\lambda_{31}} \end{pmatrix}$$

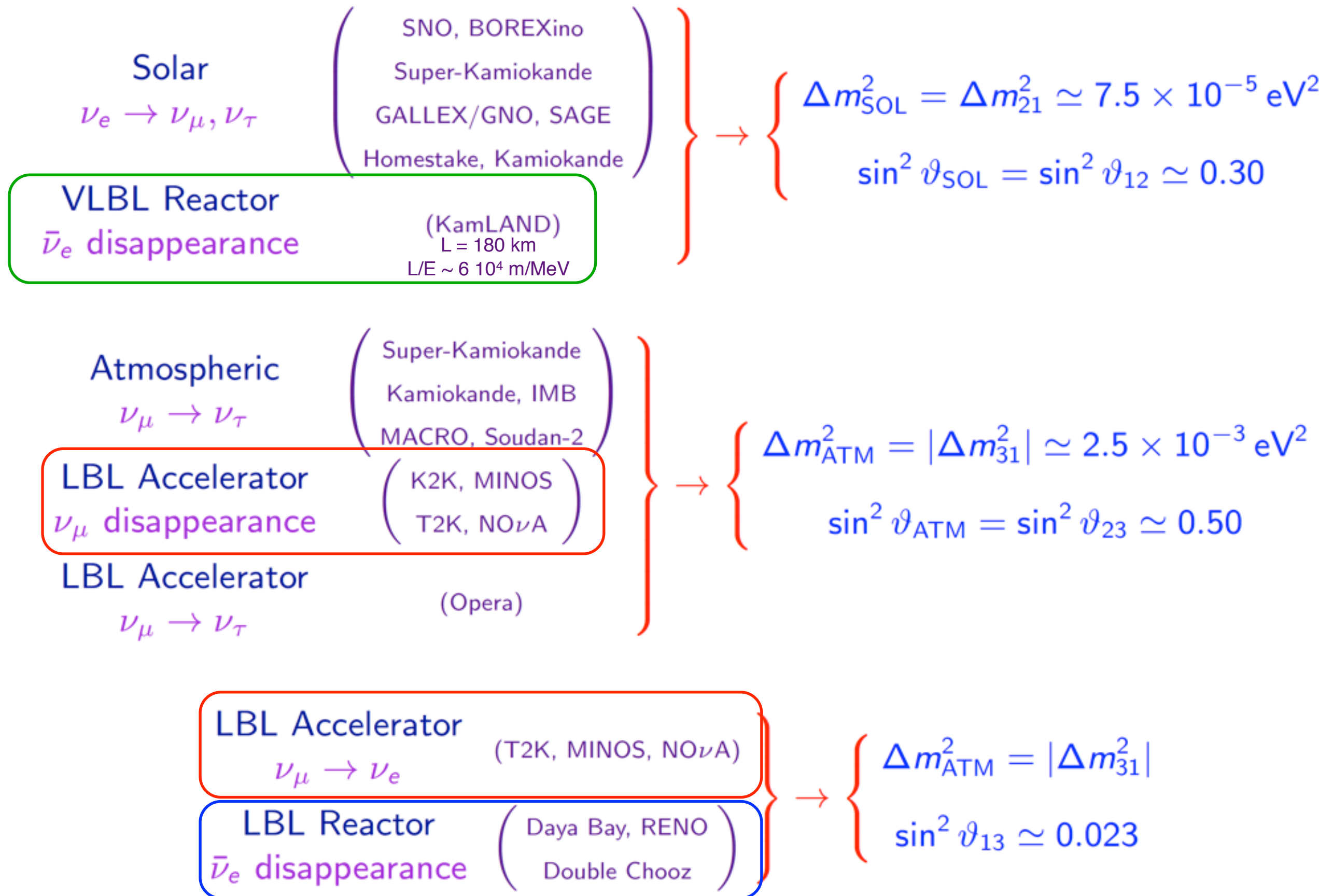
$$= \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta_{13}} \\ -s_{12}c_{23}-c_{12}s_{23}s_{13}e^{i\delta_{13}} & c_{12}c_{23}-s_{12}s_{23}s_{13}e^{i\delta_{13}} & s_{23}c_{13} \\ s_{12}s_{23}-c_{12}c_{23}s_{13}e^{i\delta_{13}} & -c_{12}s_{23}-s_{12}c_{23}s_{13}e^{i\delta_{13}} & c_{23}c_{13} \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & e^{i\lambda_{21}} & 0 \\ 0 & 0 & e^{i\lambda_{31}} \end{pmatrix}$$

$$c_{ab} \equiv \cos \vartheta_{ab} \quad s_{ab} \equiv \sin \vartheta_{ab} \quad 0 \leq \vartheta_{ab} \leq \frac{\pi}{2} \quad 0 \leq \delta_{13}, \lambda_{21}, \lambda_{31} < 2\pi$$

$$\text{OSCILLATION PARAMETERS} \quad \left\{ \begin{array}{l} 3 \text{ Mixing Angles: } \vartheta_{12}, \vartheta_{23}, \vartheta_{13} \\ 1 \text{ CPV Dirac Phase: } \delta_{13} \\ 2 \text{ independent } \Delta m_{kj}^2 \equiv m_k^2 - m_j^2: \Delta m_{21}^2, \Delta m_{31}^2 \end{array} \right.$$

2 CPV Majorana Phases: $\lambda_{21}, \lambda_{31} \iff |\Delta L| = 2$ processes

Experimental Evidences of Neutrino Oscillations



Experimental knowledge (2018)

<https://globalfit.astroparticles.es/>

parameter	best fit $\pm 1\sigma$	3σ range	
Δm_{21}^2 [10^{-5}eV^2]	$7.55^{+0.20}_{-0.16}$	7.05–8.14	2.4%
$ \Delta m_{31}^2 $ [10^{-3}eV^2] (NO)	2.50 ± 0.03	2.41–2.60	
$ \Delta m_{31}^2 $ [10^{-3}eV^2] (IO)	$2.42^{+0.03}_{-0.04}$	2.31–2.51	1.3%
$\sin^2 \theta_{12}/10^{-1}$	$3.20^{+0.20}_{-0.16}$	2.73–3.79	5.5%
$\sin^2 \theta_{23}/10^{-1}$ (NO)	$5.47^{+0.20}_{-0.30}$	4.45–5.99	4.7%
$\sin^2 \theta_{23}/10^{-1}$ (IO)	$5.51^{+0.18}_{-0.30}$	4.53–5.98	4.4%
$\sin^2 \theta_{13}/10^{-2}$ (NO)	$2.160^{+0.083}_{-0.069}$	1.96–2.41	
$\sin^2 \theta_{13}/10^{-2}$ (IO)	$2.220^{+0.074}_{-0.076}$	1.99–2.44	3.5%
δ/π (NO)	$1.32^{+0.21}_{-0.15}$	0.87–1.94	10%
δ/π (IO)	$1.56^{+0.13}_{-0.15}$	1.12–1.94	9%

relative 1σ uncertainty

de Salas et al, PLB782 (2018) 633

Open Problems

- ▶ $\vartheta_{23} \stackrel{<}{\stackrel{>}{\approx}} 45^\circ$?
 - ▶ T2K (Japan), NO ν A (USA), ...
- ▶ CP violation ? $\delta_{13} \approx 3\pi/2$?
 - ▶ T2K (Japan), NO ν A (USA), DUNE (USA), HyperK (Japan), ...
- ▶ Mass Ordering ?
 - ▶ JUNO (China), RENO-50 (Korea), PINGU (Antarctica), ORCA (EU), INO (India), ...

- Let's devote a couple of our lectures to exploring the reach, strategy and issues of the current experiments at artificial sources

Open Problems

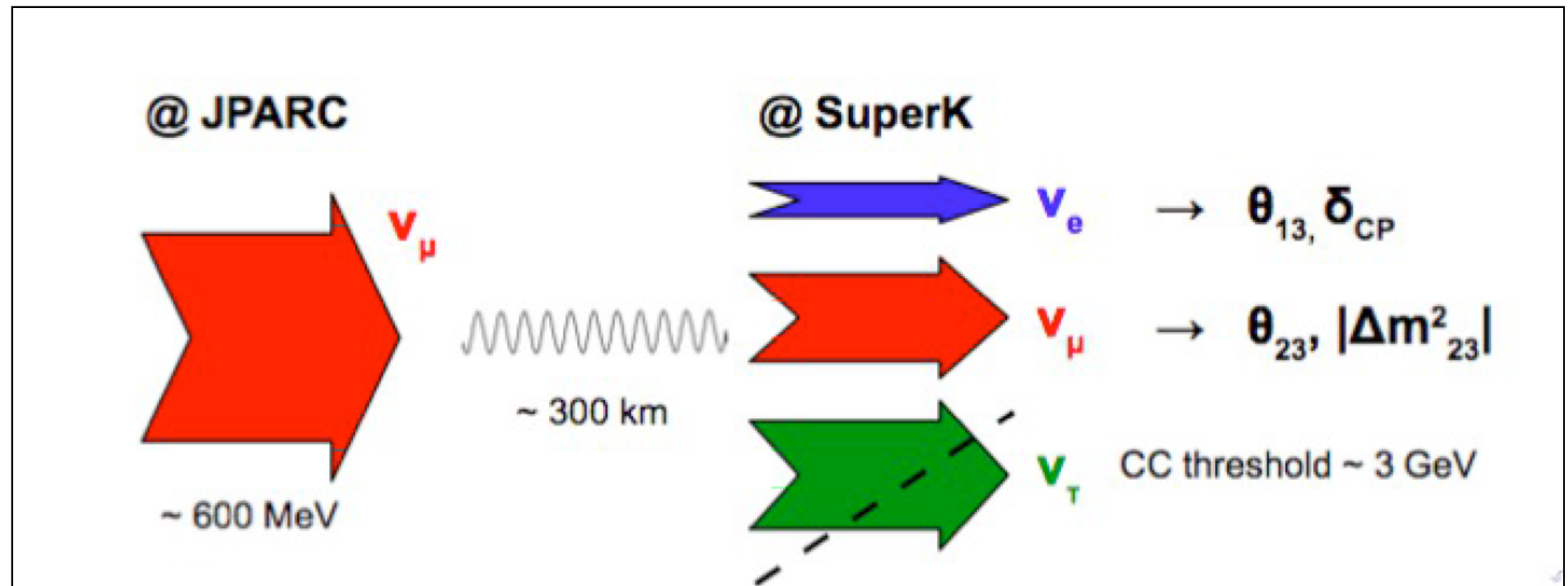
- ▶ $\vartheta_{23} \stackrel{<}{\stackrel{>}{\approx}} 45^\circ$?
 - ▶ T2K (Japan), NO ν A (USA), ...
- ▶ CP violation ? $\delta_{13} \approx 3\pi/2$?
 - ▶ T2K (Japan), NO ν A (USA), DUNE (USA), HyperK (Japan), ...
- ▶ Mass Ordering ?
 - ▶ JUNO (China), RENO-50 (Korea), PINGU (Antarctica), ORCA (EU), INO (India), ...

- Let's devote a couple of our lectures to exploring the reach, strategy and issues of the current experiments at artificial sources

Current expts of ν_e appearance in ν_μ beam

- **T2K** (Tokai-To-Kamioka)
 - J-PARC: 50 GeV proton synchrotron @Tokai (JP)
 - High intensity
 - beam directed towards Super-Kamiokande
 - $L=295$ Km
- **Nova**: Fermilab neutrino beam (NuMI)
 - $L=810$ km
- Both experiments are at an angle with respect to the beam direction (off-axis experiments)

T2K



Neutrino oscillations at LBL

$$P(\nu_\mu \rightarrow \nu_\mu) \simeq 1 - (\cos^4 \theta_{13} \sin^2 2\theta_{23}) \sin^2 \left(\Delta m_{31}^2 \frac{L}{4E} \right)$$

E ~ 0.6 GeV
L ~ 295 km

- Precise measurement of $\sin^2 2\theta_{23}$
- Test of CPT by comparing measured $\nu_\mu \rightarrow \nu_\mu$ with $\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu$

$$P(\nu_\mu \rightarrow \nu_e) \simeq \boxed{\sin^2 2\theta_{13} \times \sin^2 \theta_{23} \times \frac{\sin^2[(1-x)\Delta]}{(1-x)^2}} \quad \text{Phys. Rev. D64 (2001) 053003}$$

Leading term

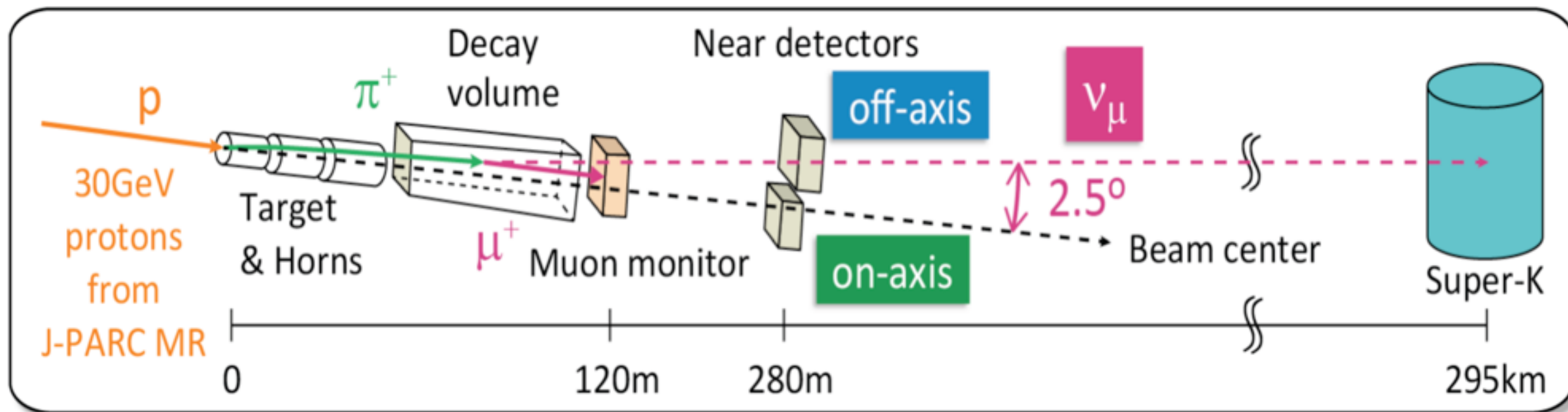
CP violating $\ominus \alpha \boxed{\sin \delta_{CP}} \times \sin^2 2\theta_{12} \sin 2\theta_{13} \sin 2\theta_{23} \times \sin \Delta \frac{\sin[x\Delta]}{x} \frac{\sin[(1-x)\Delta]}{(1-x)}$
 “+” for antineutrino

CP conserving $\alpha \boxed{\cos \delta_{CP}} \times \sin 2\theta_{12} \sin 2\theta_{13} \sin 2\theta_{23} \times \cos \Delta \frac{\sin[x\Delta]}{x} \frac{\sin[(1-x)\Delta]}{(1-x)}$
 $+ O(\alpha^2)$

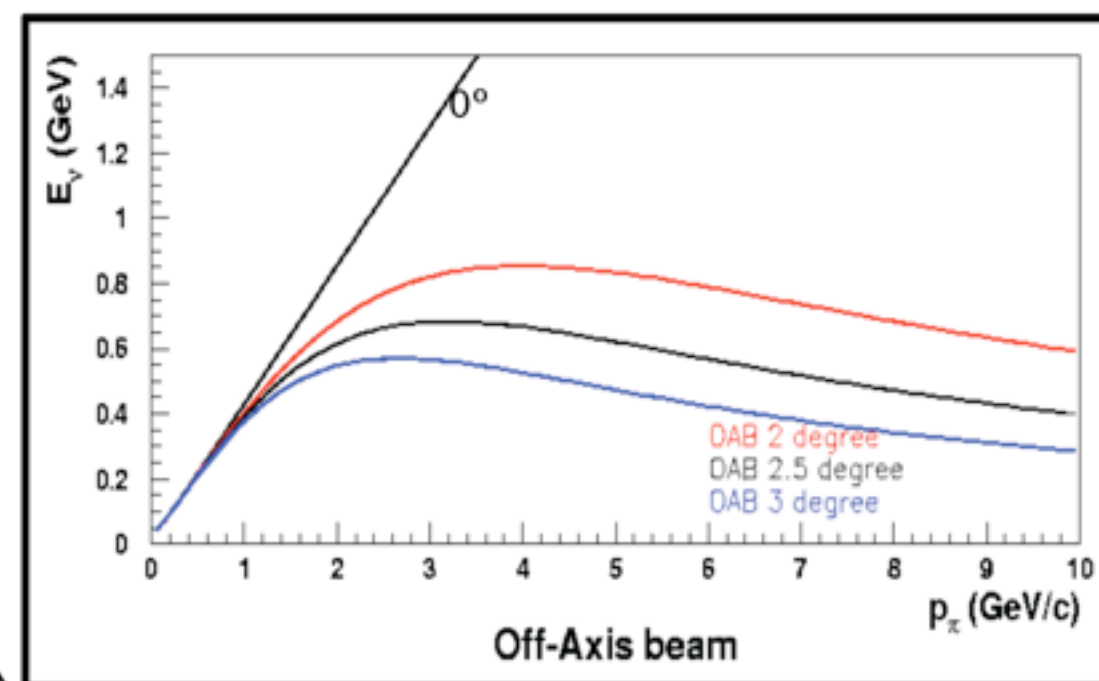
Matter effect $x = \frac{2\sqrt{2}G_F N_e E}{\Delta m_{31}^2} \quad \alpha = \left| \frac{\Delta m_{21}^2}{\Delta m_{31}^2} \right| \sim \frac{1}{30} \quad \Delta = \frac{\Delta m_{31}^2 L}{4E}$

- The leading term defines the octant $\theta_{23} > 45^\circ$ or $\theta_{23} < 45^\circ$
- All mass splittings and mixing angles have been measured to be non-zero:
second order term can violate the CP symmetry if $\sin \delta_{CP} \neq 0$

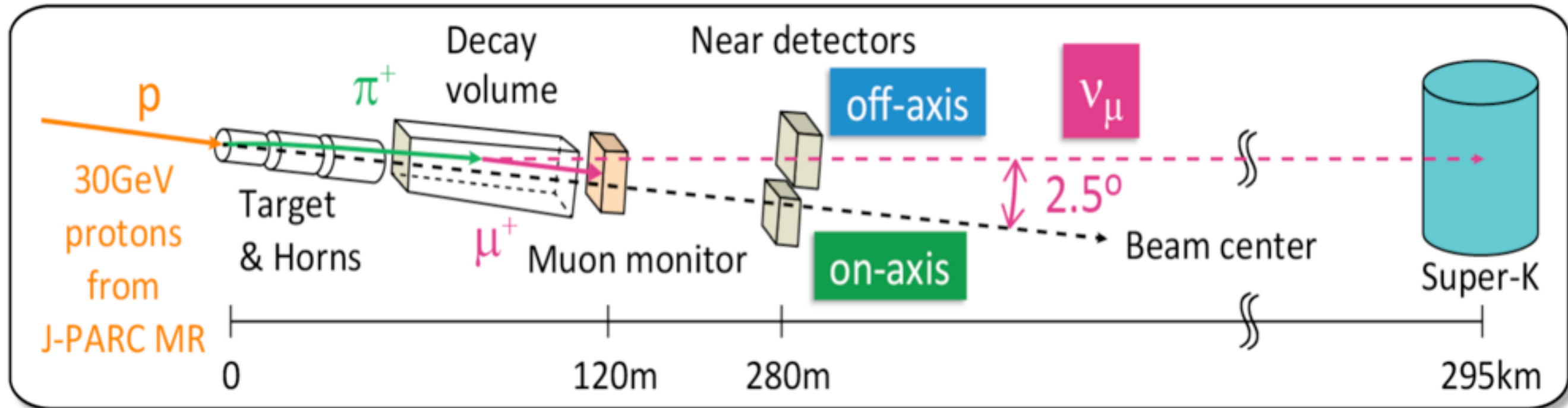
Design principle: the off-axis angle



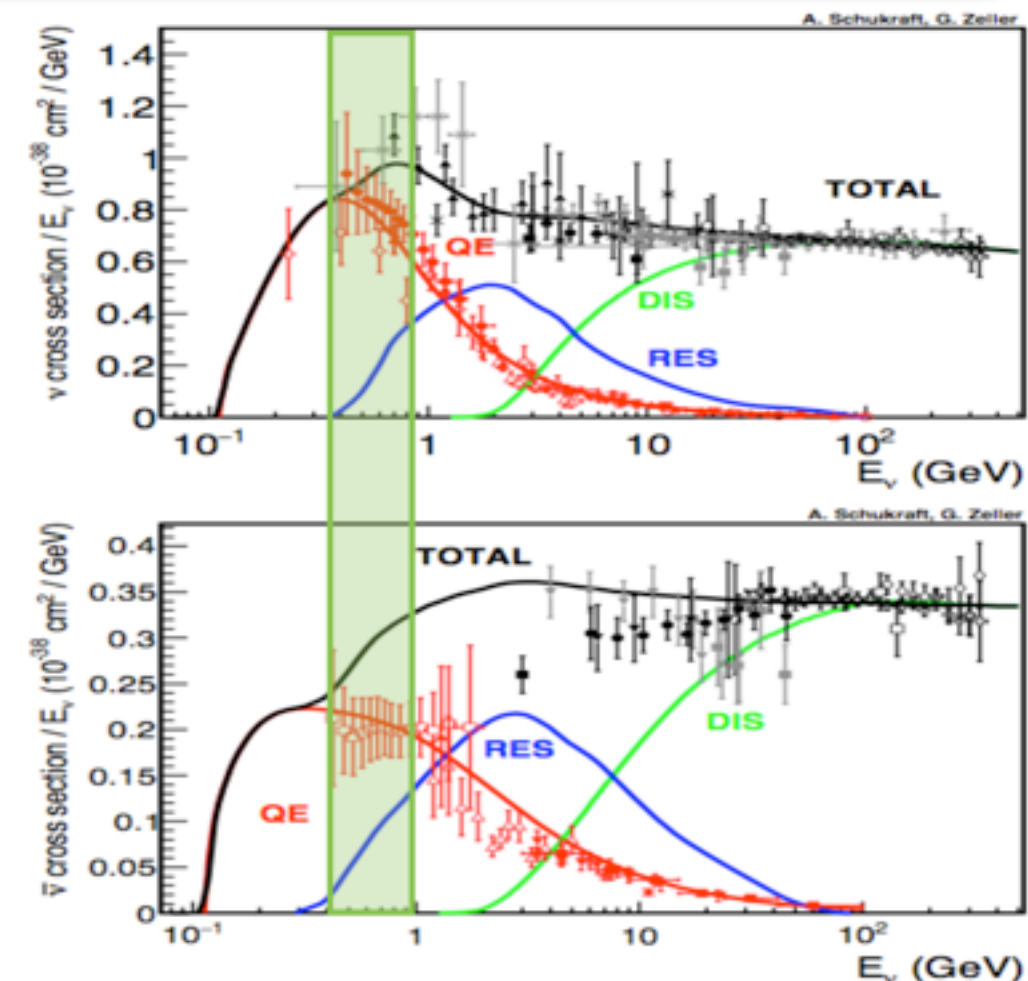
- 30 GeV proton beam on 90 cm long graphite target
- ν_μ and $\bar{\nu}_\mu$ produced by pion and kaon decay:
 - $\pi^+ \rightarrow \mu^+ + \nu_\mu$
 - $\pi^- \rightarrow \mu^- + \bar{\nu}_\mu$
- Invert magnet polarity to produce a $\bar{\nu}_\mu$ beam
- First off-axis neutrino beam experiment (2.5°)
 - narrow spectrum peaked at 0.6 GeV, on the expected oscillation maximum



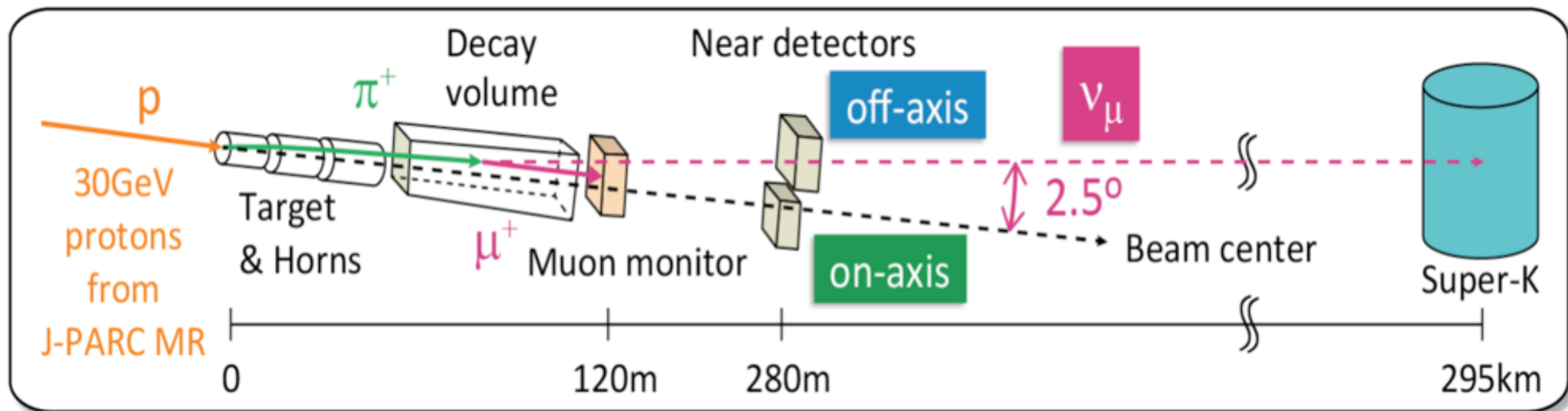
Design principle: the off-axis angle



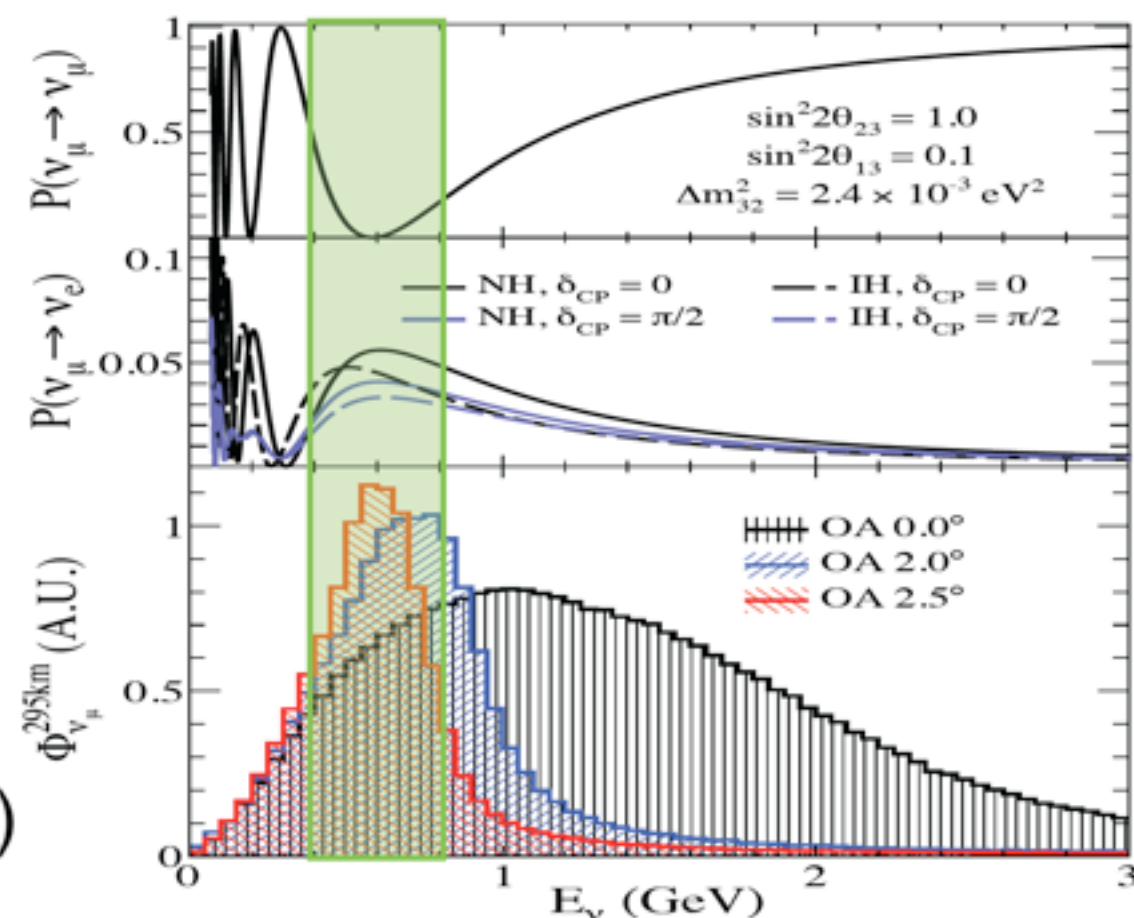
- 30 GeV proton beam on 90 cm long graphite target
- ν_μ and $\bar{\nu}_\mu$ produced by pion and kaon decay:
 - $\pi^+ \rightarrow \mu^+ + \nu_\mu$
 - $\pi^- \rightarrow \mu^- + \bar{\nu}_\mu$
- Invert magnet polarity to produce a $\bar{\nu}_\mu$ beam
- First off-axis neutrino beam experiment (2.5°)
 - narrow spectrum peaked at 0.6 GeV, on the expected oscillation maximum



Design principle: the off-axis angle

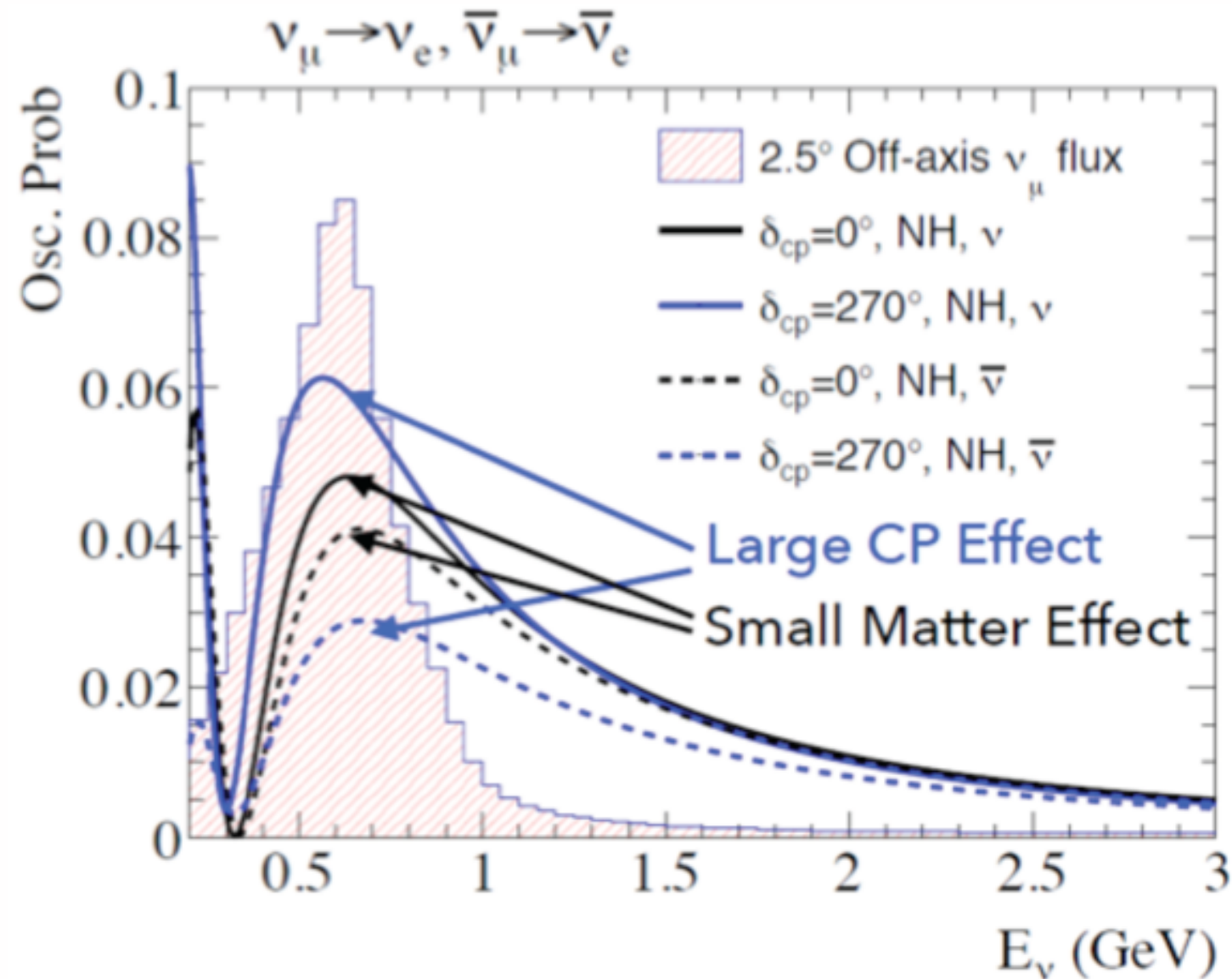


- 30 GeV proton beam on 90 cm long graphite target
- ν_μ and $\bar{\nu}_\mu$ produced by pion and kaon decay:
 - $\pi^+ \rightarrow \mu^+ + \nu_\mu$
 - $\pi^- \rightarrow \mu^- + \bar{\nu}_\mu$
- Invert magnet polarity to produce a $\bar{\nu}_\mu$ beam
- First off-axis neutrino beam experiment (2.5°)
 - narrow spectrum peaked at 0.6 GeV, on the expected oscillation maximum



Effect of CP violation at T2K

T2K



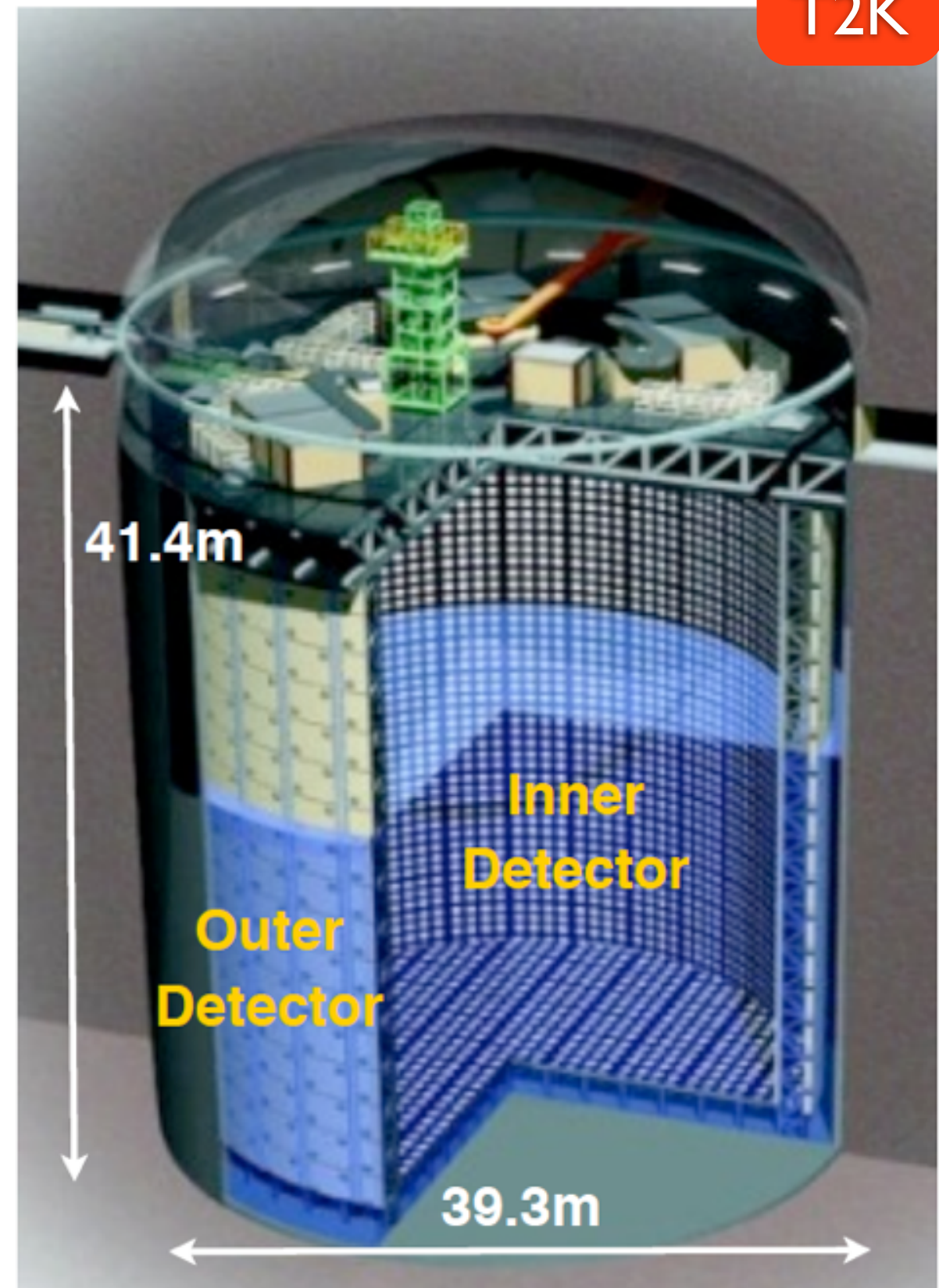
Correlation between CPV and matter effects present

- Asymmetric effect on $P(\nu_\mu \rightarrow \nu_e)$ and $P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$:
 - $\delta_{CP} = -\pi/2 \rightarrow$ maximizes $P(\nu_\mu \rightarrow \nu_e)$ and minimizes $P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$
 - $\delta_{CP} = +\pi/2 \rightarrow$ minimizes $P(\nu_\mu \rightarrow \nu_e)$ and maximizes $P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$
- δ_{CP} and Mass Hierarchy have similar effects
- Effect of δ_{CP} on $\nu_\mu \rightarrow \nu_e$ and $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ is about $\pm 20\text{-}30\%$
- Effect of Mass Hierarchy is about $\pm 10\%$

T2K far detector: Super-Kamiokande

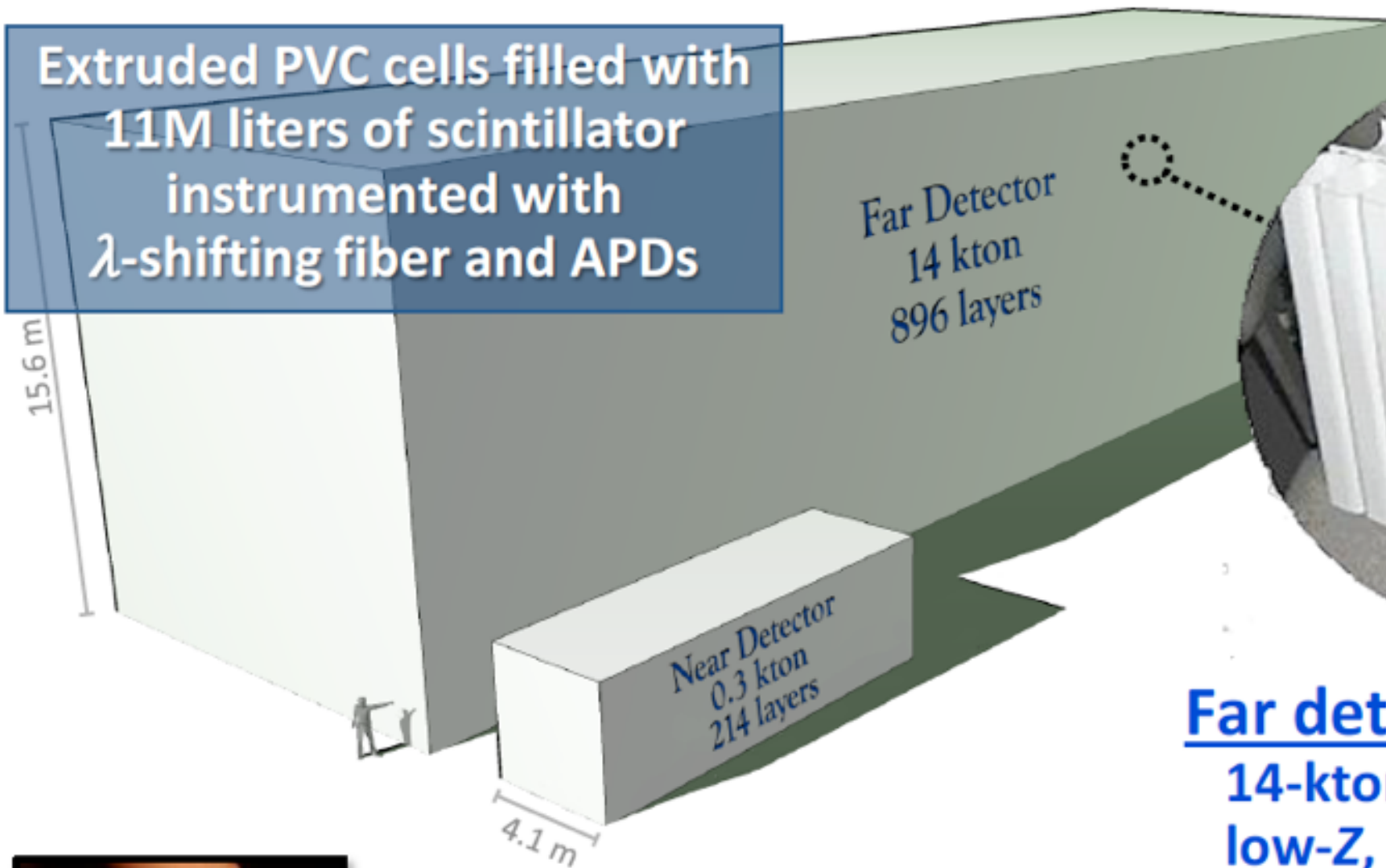
T2K

- Located in Mozumi mine
 - 2700 m.w.e overburden
- Water Cherenkov detector (50 kton)
- Fiducial mass 22.5 kton
- Inner detector
 - 11129 20-inch PMTs
- Outer veto detector
 - 1885 8-inch PMTs
 - determine fully-contained events
- New DAQ system: no dead time
- T2K beam event: $\pm 500 \mu\text{s}$ window



NO ν A detectors

Extruded PVC cells filled with
11M liters of scintillator
instrumented with
 λ -shifting fiber and APDs



A NO ν A cell

To APD



1560 cm

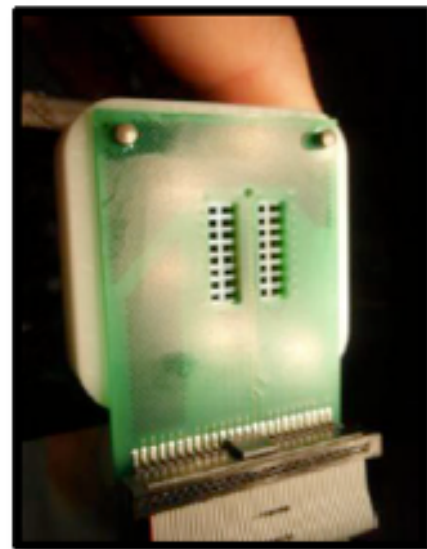
4 cm $\times$ 6 cm

Far detector:

14-kton, fine-grained,
low-Z, highly-active
tracking calorimeter
 $\rightarrow$ 344,000 channels

Near detector:

0.3-kton version of
the same
 $\rightarrow$ 20,000 channels

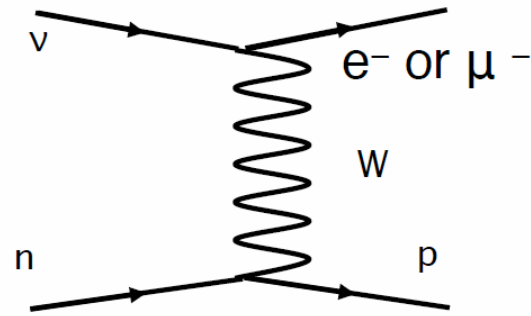


32-pixel APD

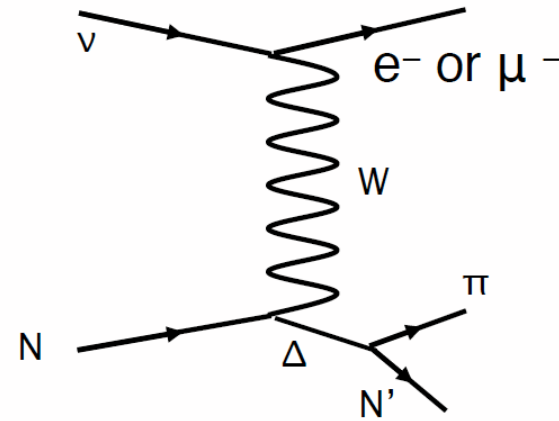
Fiber pairs
from 32 cells



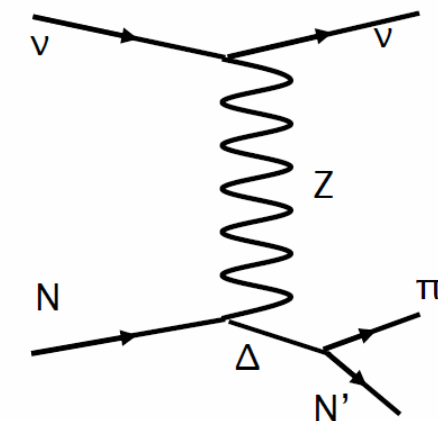
Charged-Current Quasi-Elastic (CCQE)



Charged-Current π



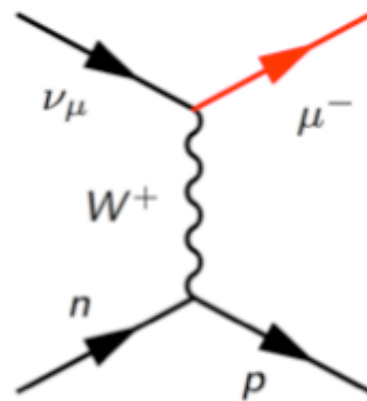
Neutral-Current π



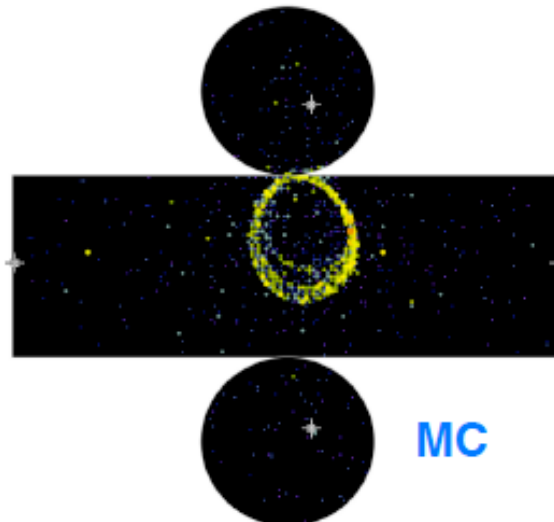
Super-Kamiokande events

T2K

ν_μ CCQE

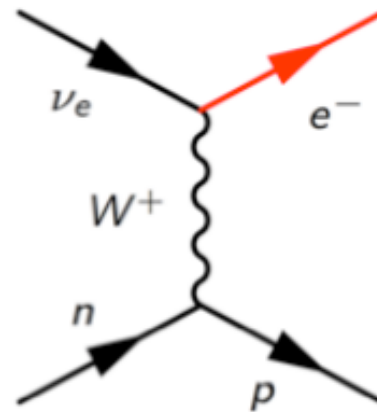


- Low scattering
- Ring with sharp edge
- Protons below Cherenkov threshold

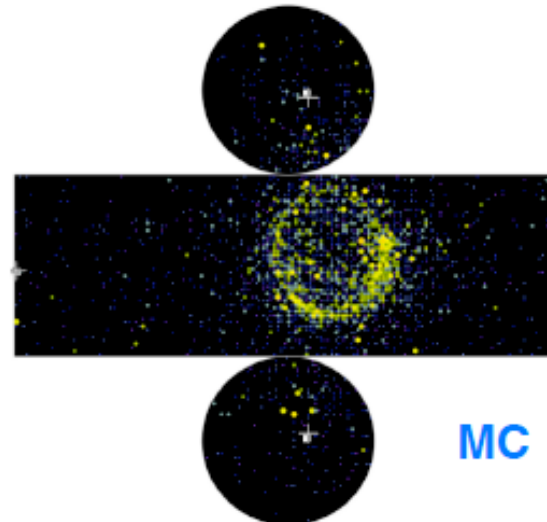


MC

ν_e CCQE

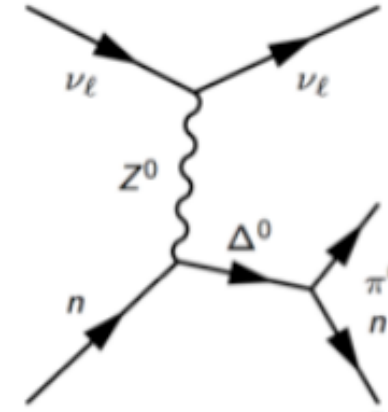


- Multiple scattering
- EM shower
- Ring with "fuzzy" edge

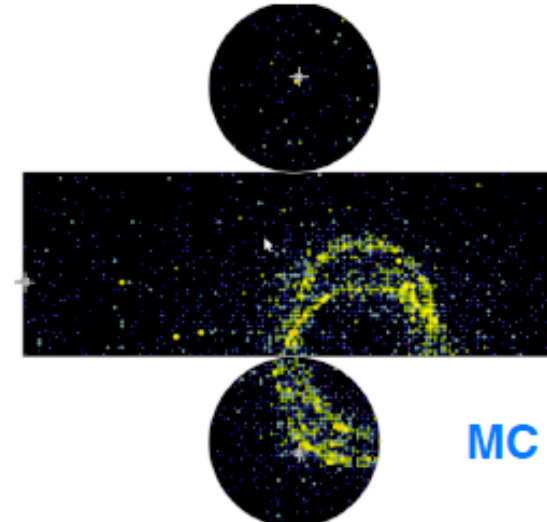


MC

Background

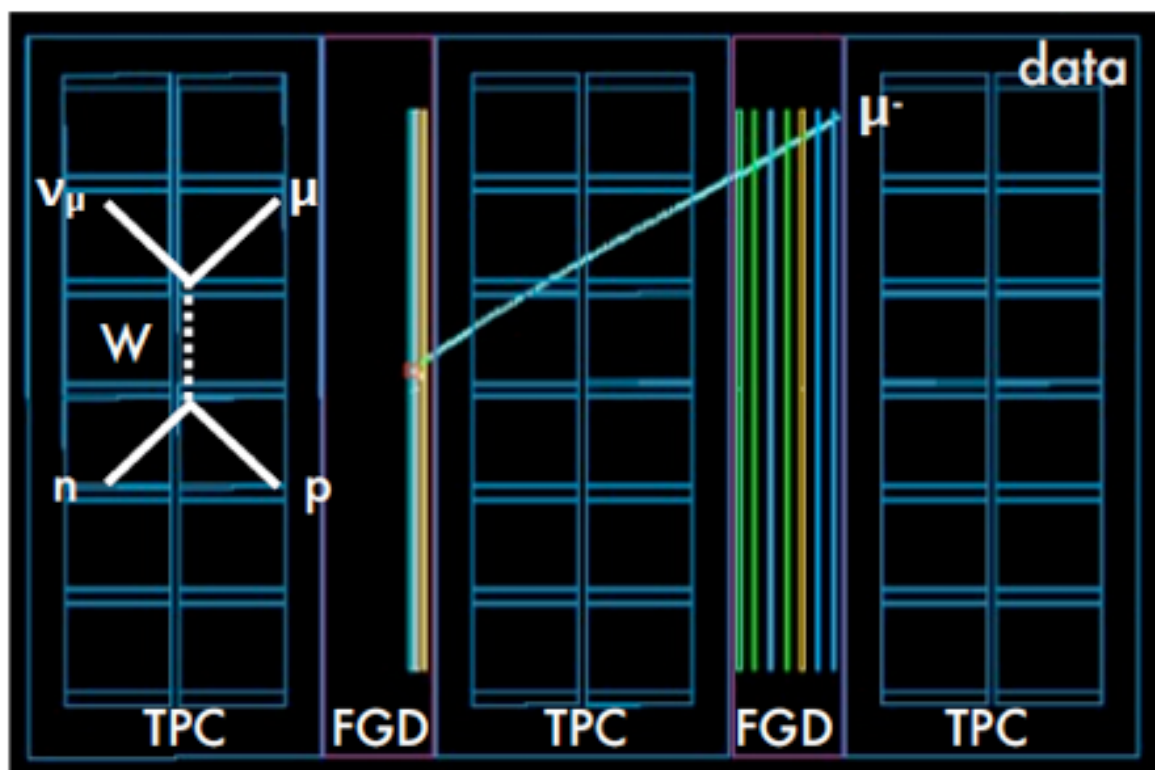


- EM shower from $\pi^0 \rightarrow \gamma\gamma$
- Can be misidentified as an electron

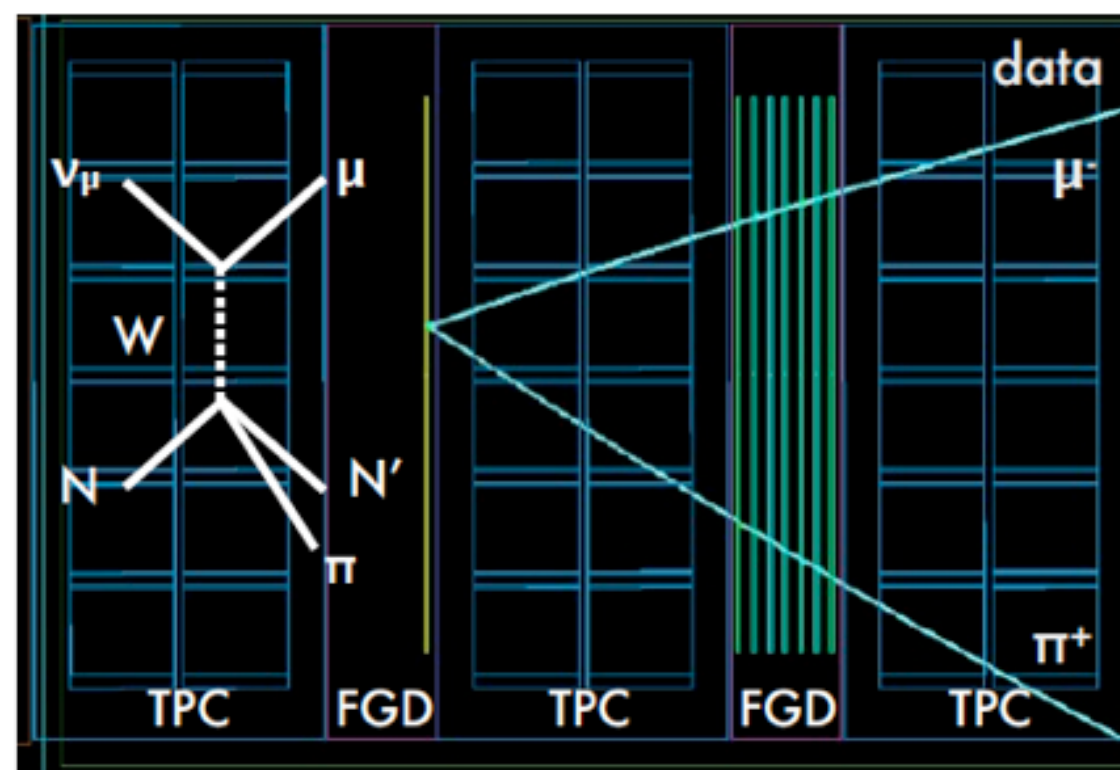


MC

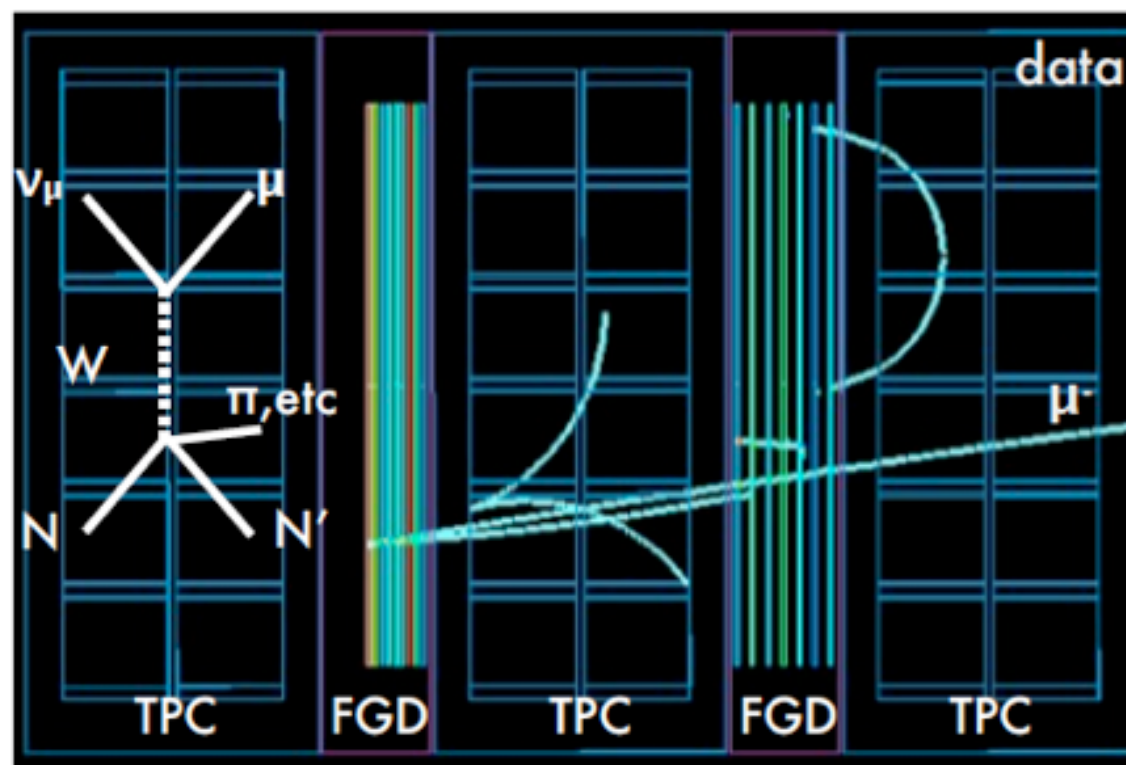
CC0 π



CC1 π^+

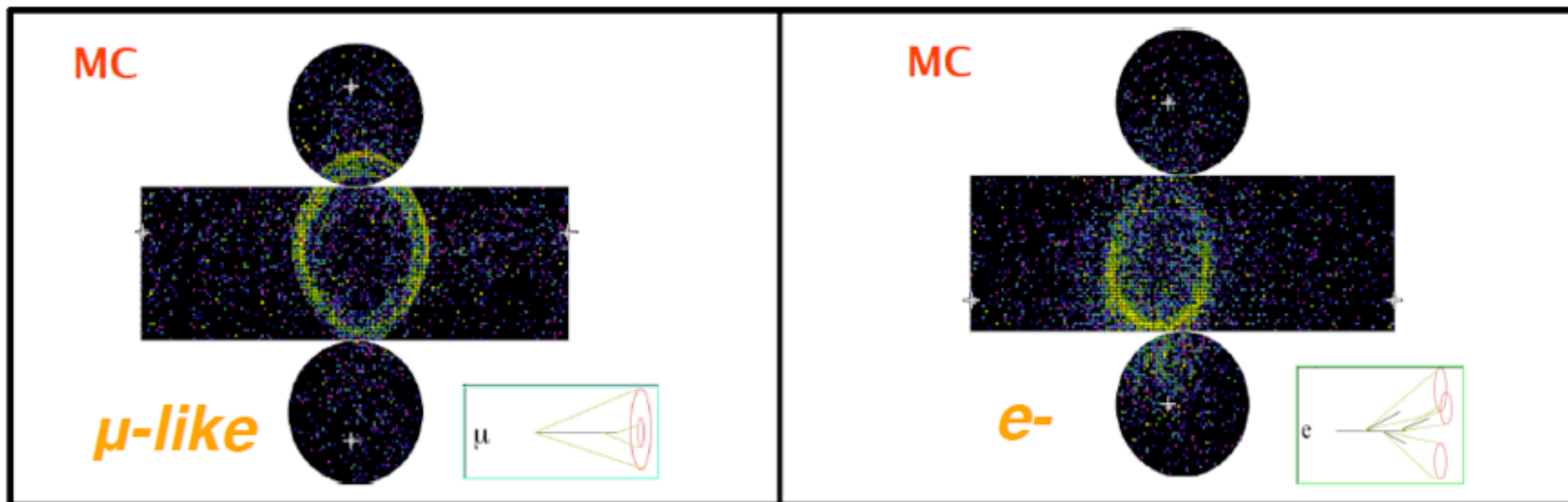


CC other



FHC Beam

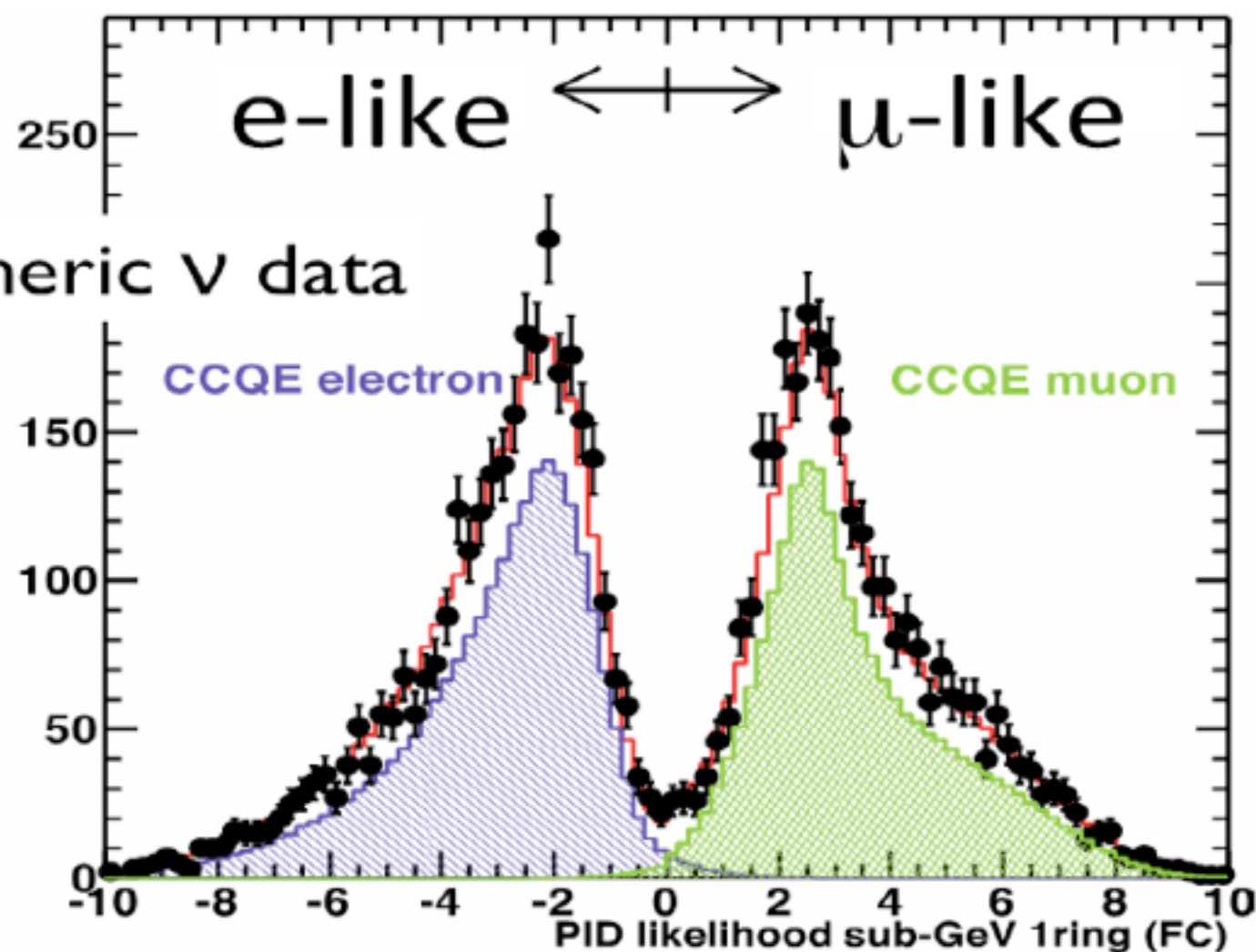
Particle Identification at the far detector



T2K

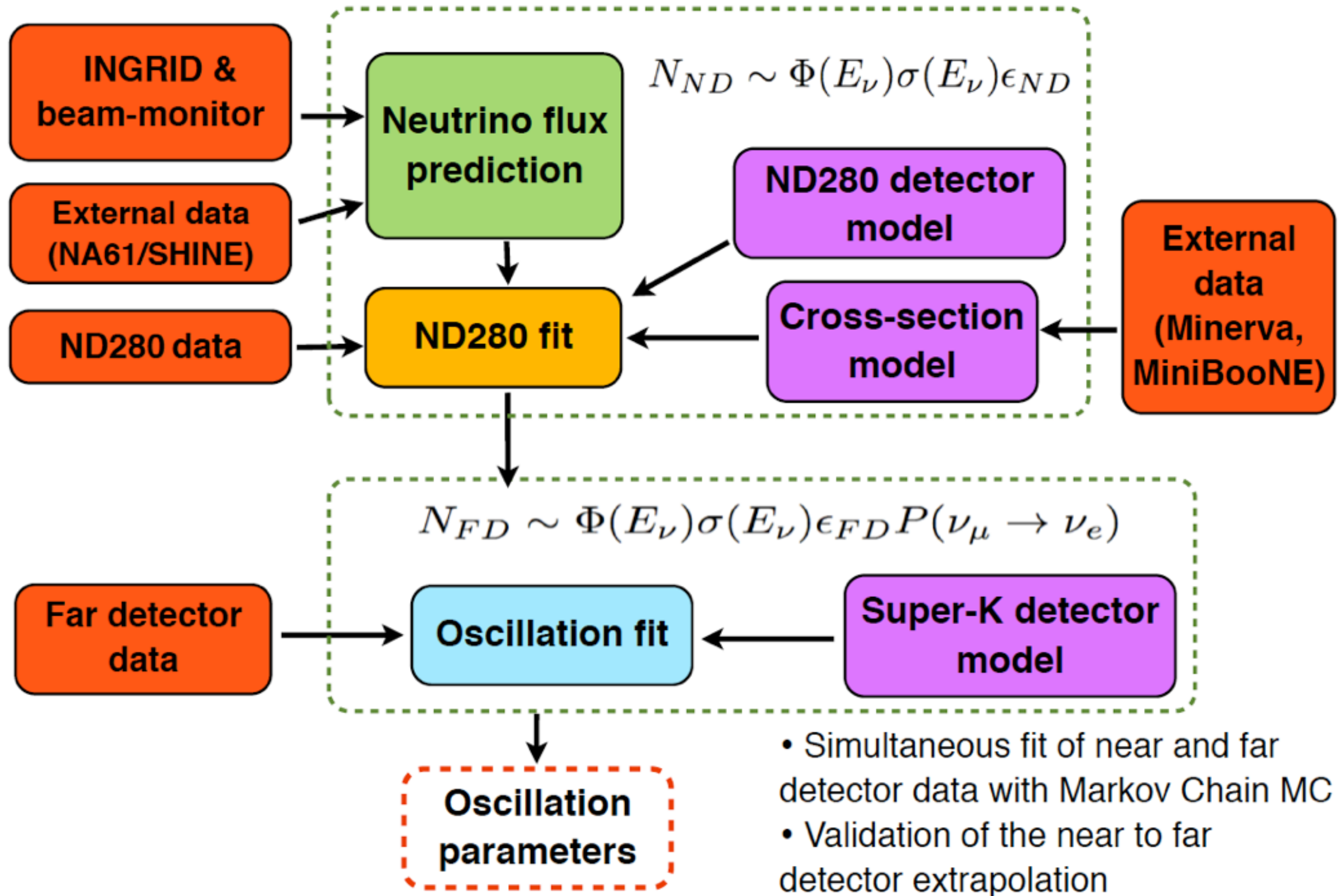
- Excellent e/ μ separation
- Probability to misidentify a muon as an electron is smaller than 1%

● atmospheric ν data
 □ MC



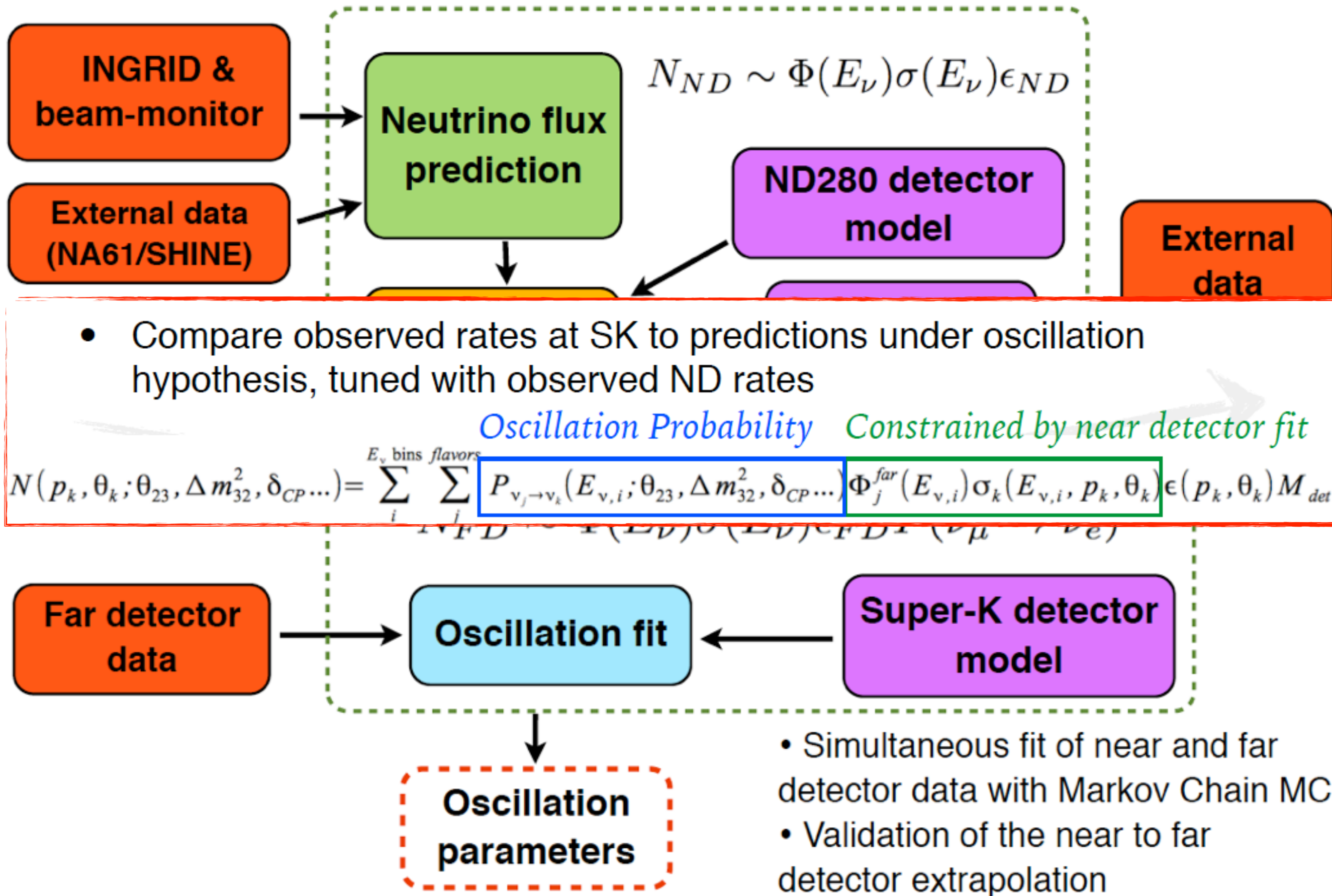
Strategy for oscillation analyses

T2K

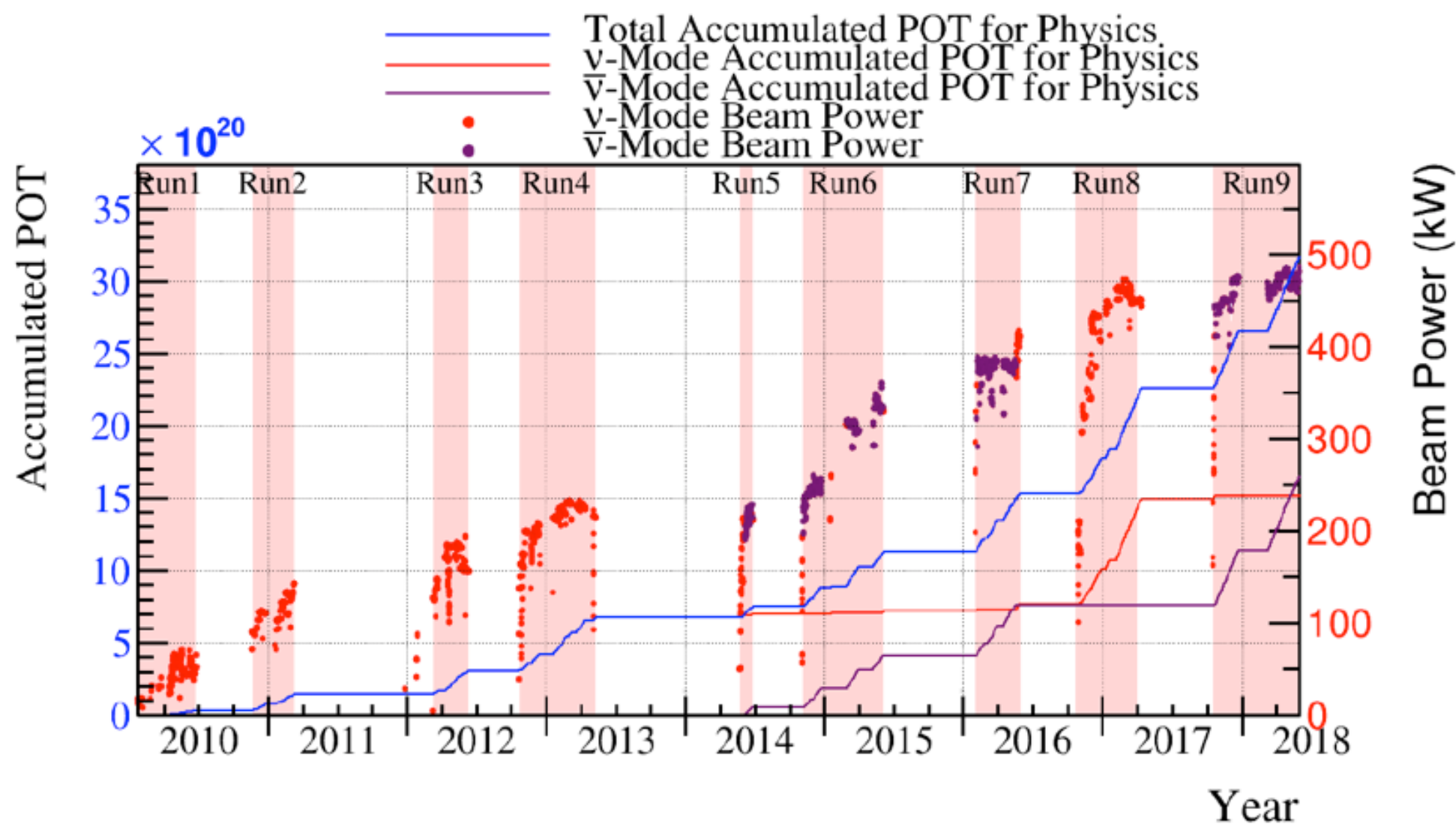


Strategy for oscillation analyses

T2K



Beam Operations



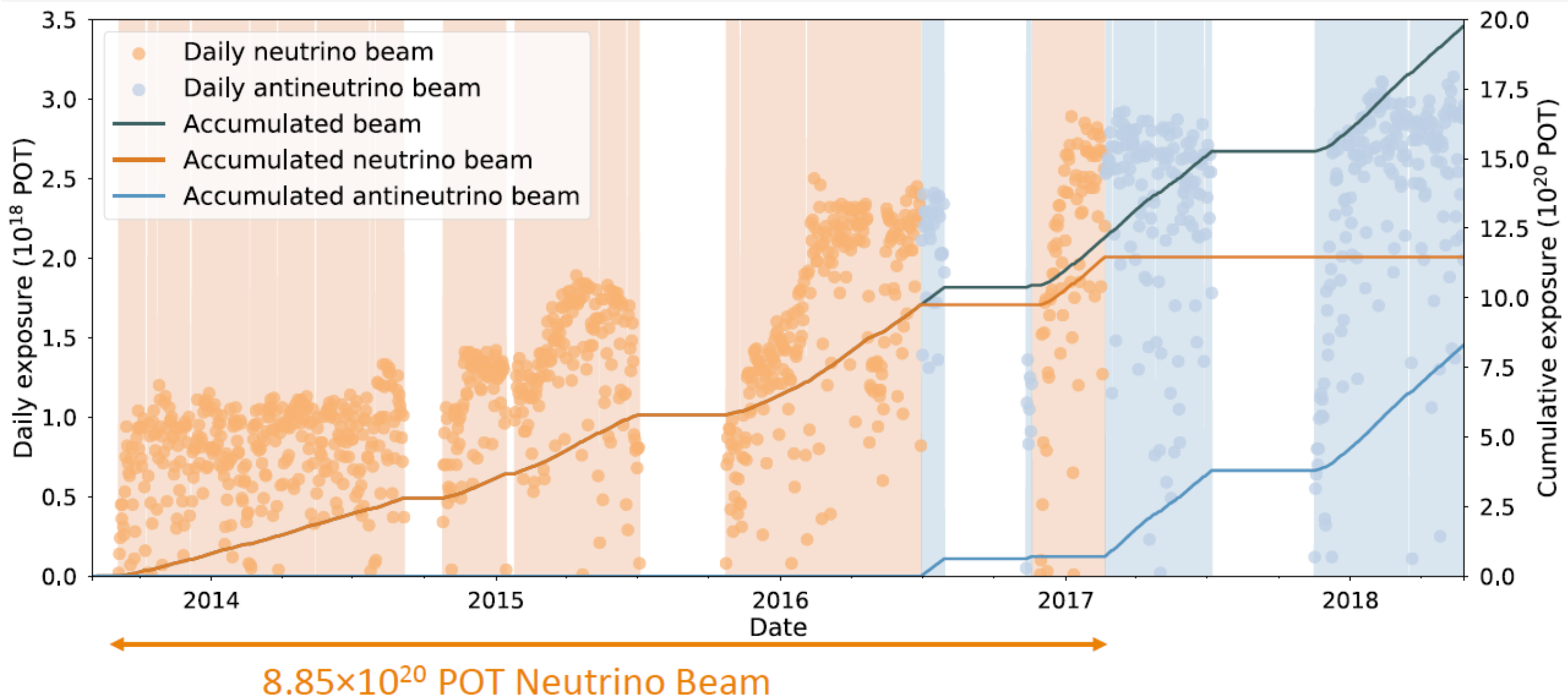
Used for this ND analysis: ν mode, Runs 2–4; $\bar{\nu}$ mode, Run 5–6

Used for this SK analysis: ν mode, Runs 1–8; $\bar{\nu}$ mode, Run 5–9

ν -mode is also known as "forward horn current" (FHC) or "positive focusing" (PF)

$\bar{\nu}$ -mode is also known as "reverse horn current" (RHC) or "negative focusing" (NF)

NB same accumulated statistics for ν and $\bar{\nu}$

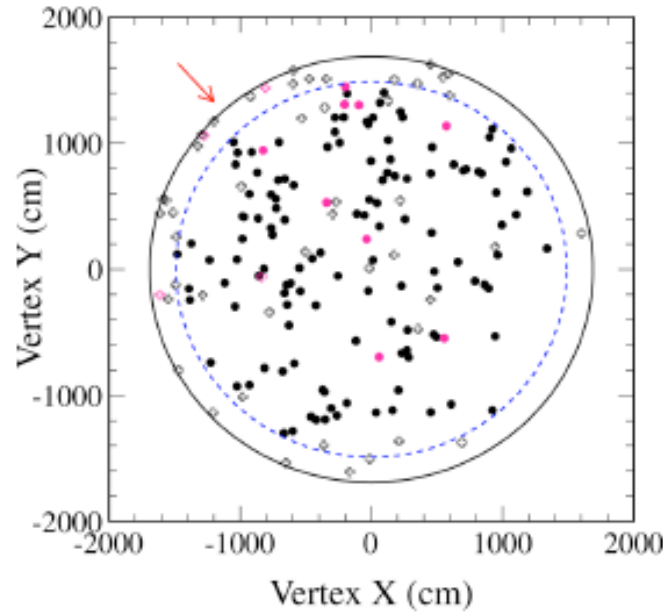


~2/3 of statistics of T2K overall
 $\bar{\nu}$ to ν ~70%

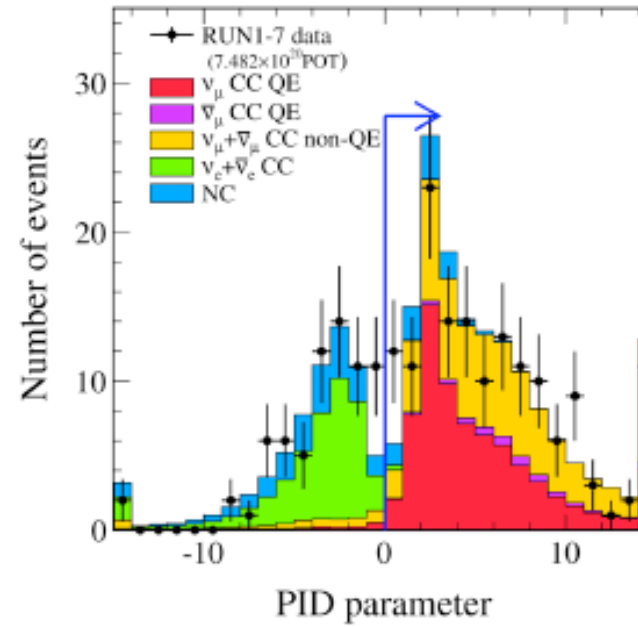
$\nu_\mu / \bar{\nu}_\mu$ selection at Far Detector

T2K

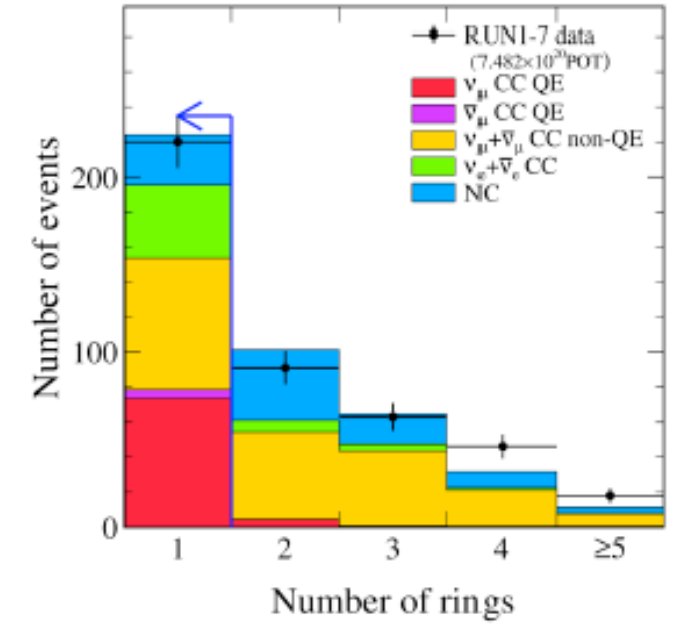
1) Fully contained in fiducial volume rings



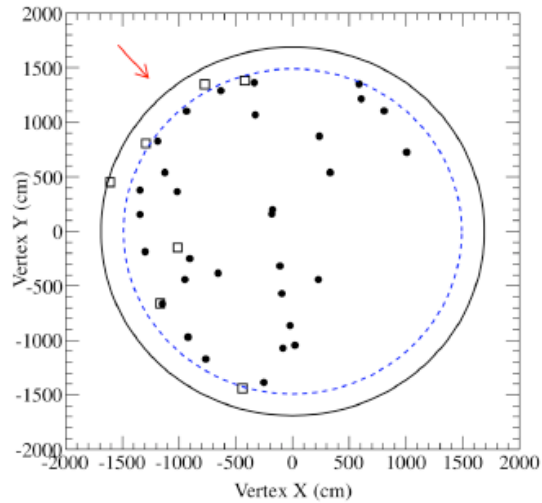
2) μ -like PID



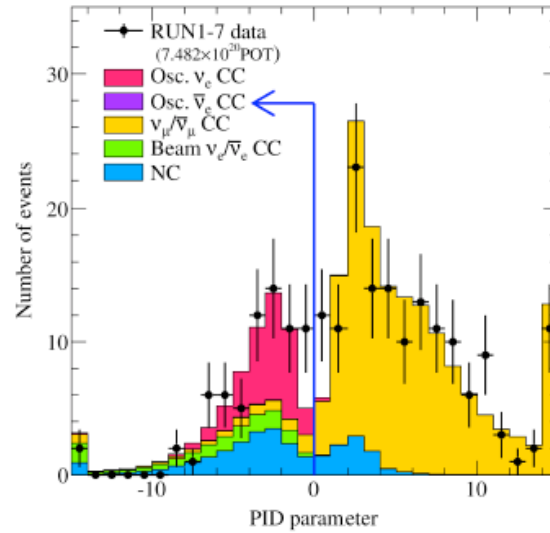
3) Single ring event



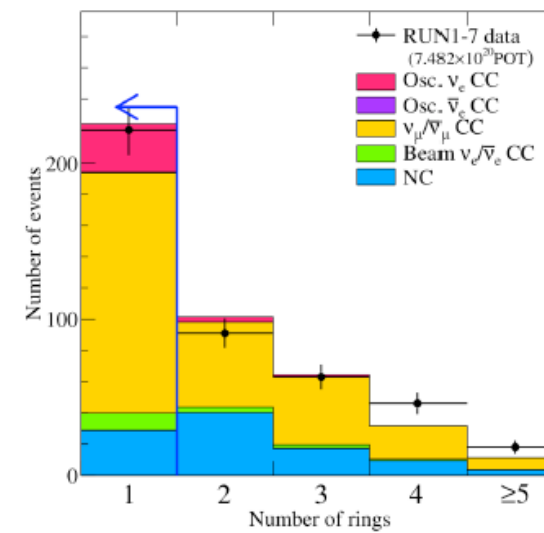
1) Fully contained in fiducial volume rings



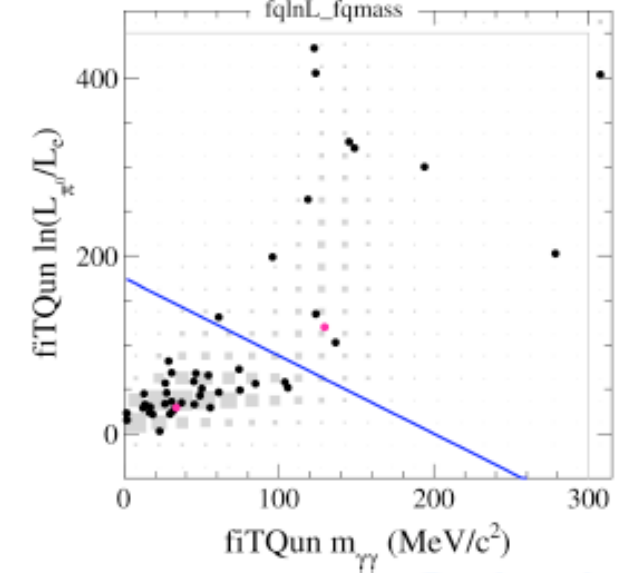
2) e-like PID



3) Single ring event



7) π^0 rejection cut

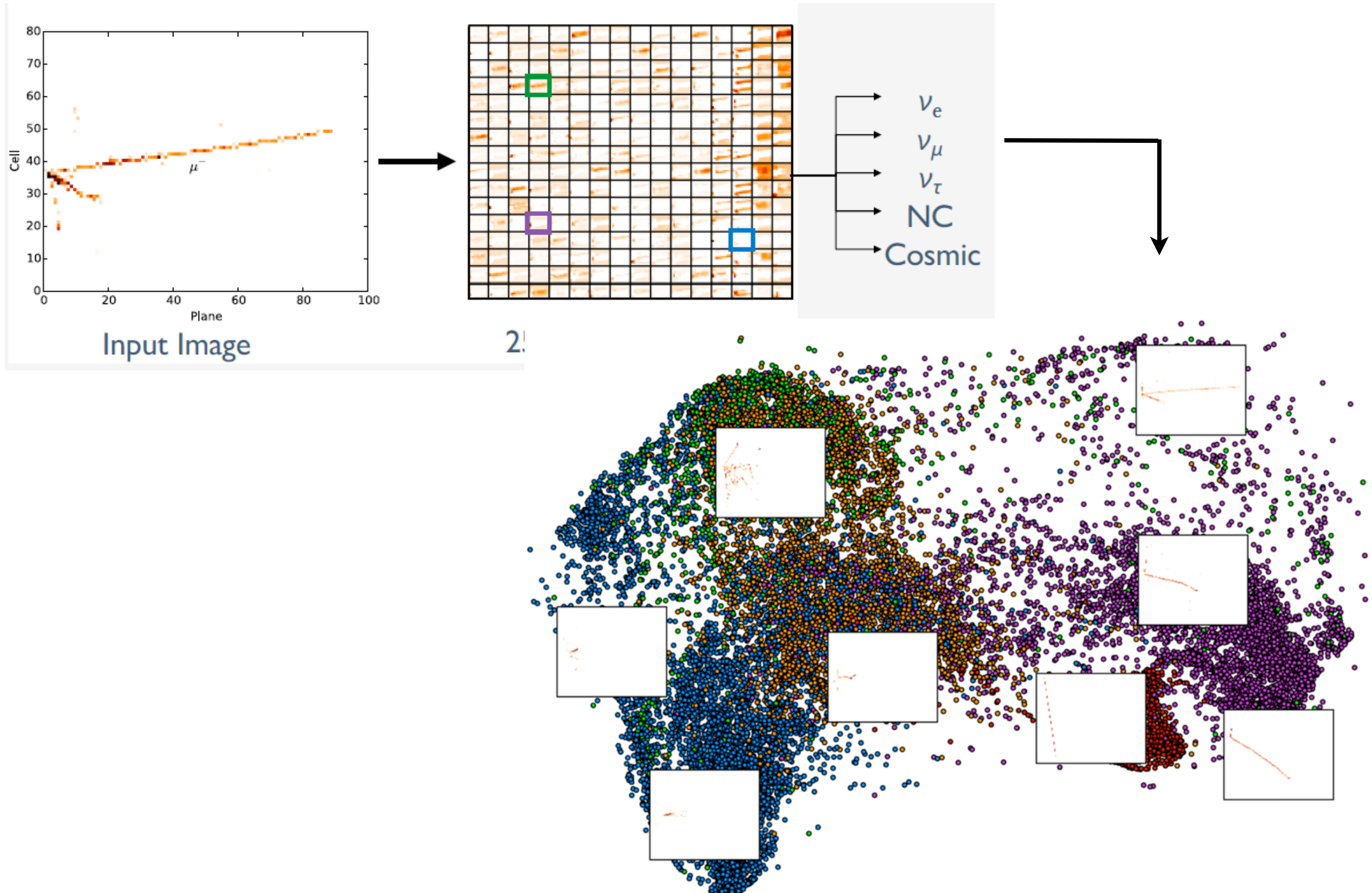


$\nu_e / \bar{\nu}_e$ selection at Far Detector

Validated using cosmic rays

Signal identification is done by CVN (Convolutional Visual Network).

- event classifier in the "image recognition" style.
- The network is trained on two dimensional views of the event's calibrated hits.
- trained separately on neutrinos and anti-neutrinos.



Updated $\bar{\nu}_\mu$ disappearance results

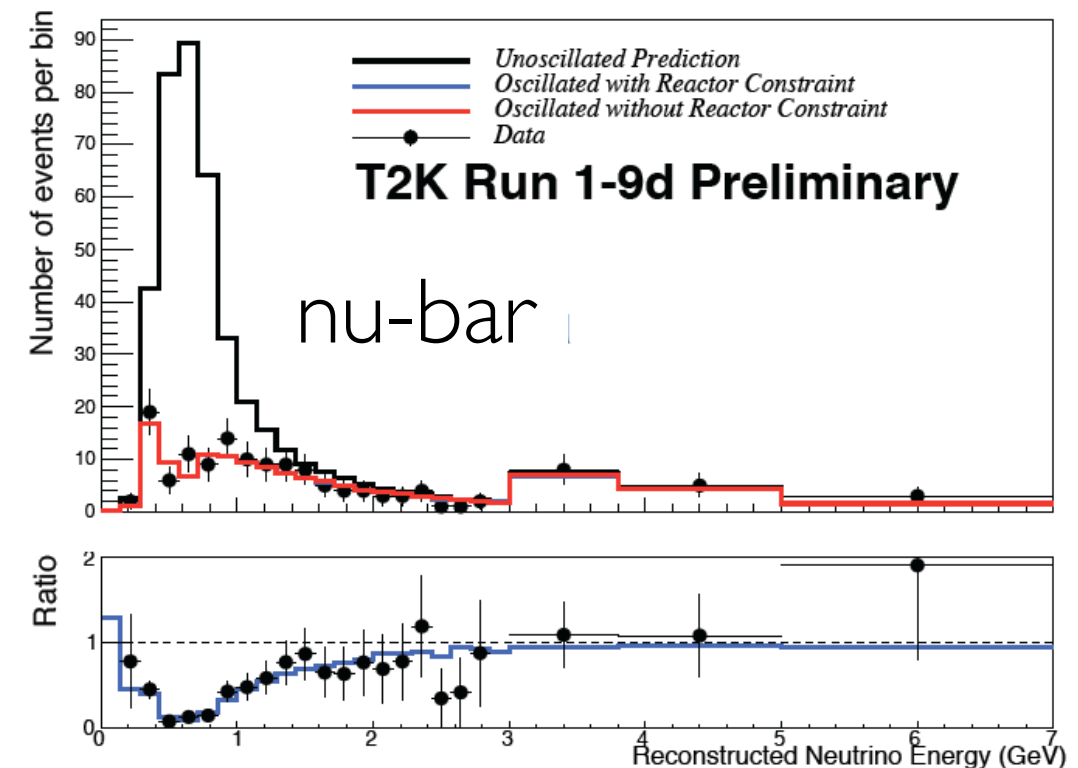
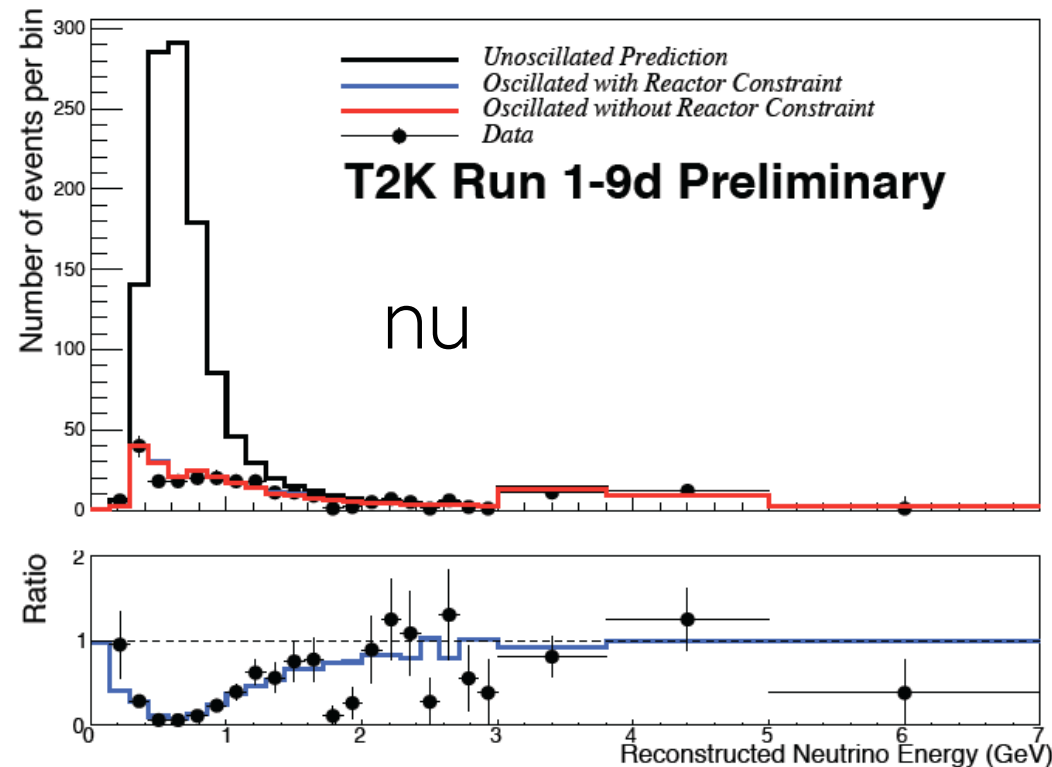
- In PMNS framework $P(\nu_\mu \rightarrow \nu_x) = P(\bar{\nu}_\mu \rightarrow \bar{\nu}_x)$ for any value of δ_{CP}
- No “ $\pm$ terms” for neutrino / antineutrino

$$P(\nu_\mu \rightarrow \nu_\mu) \simeq 1 - (\cos^4 \theta_{13} \sin^2 2\theta_{23}) \sin^2 \left(\Delta m_{31}^2 \frac{L}{4E} \right)$$

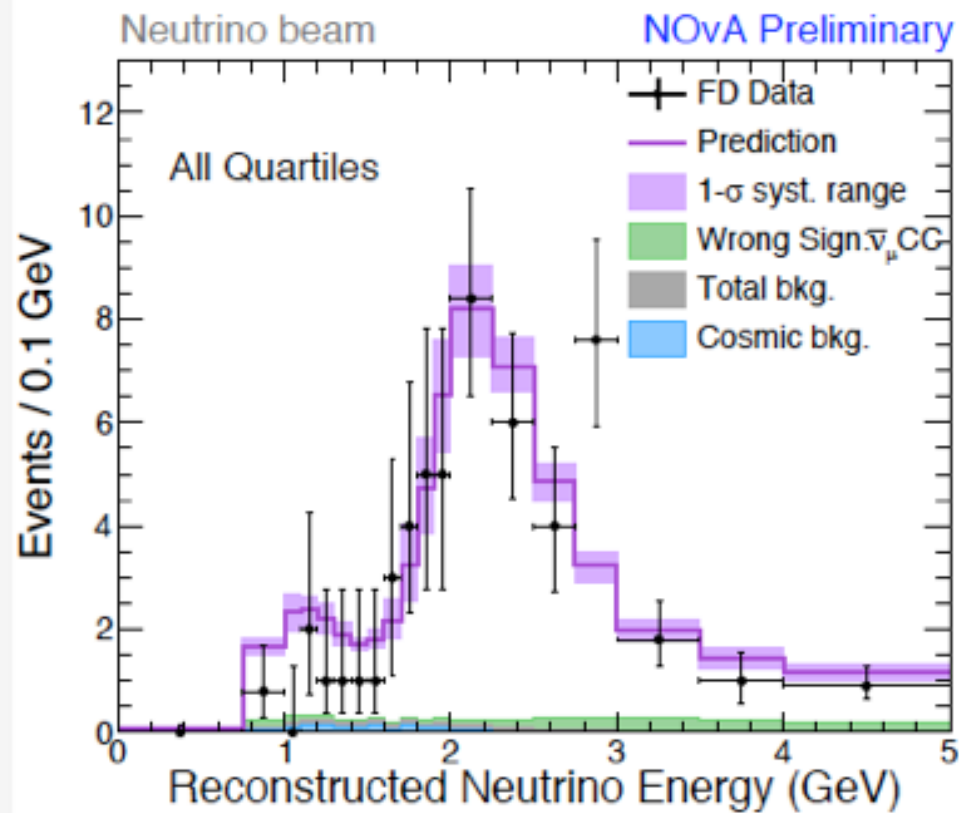
Predictions with: $\sin^2 \theta_{13} = 0.0212$, $\sin^2 \theta_{23} = 0.528$, $\Delta m_{32}^2 = 2.51 \times 10^{-3}$, NH

Sample	$\delta_{CP} = -\pi/2$	$\delta_{CP} = 0$	$\delta_{CP} = \pi/2$	$\delta_{CP} = \pi$	Observed
nu	272.4	272.0	272.4	272.8	243
nu-bar	139.5	139.2	139.5	139.9	140

T2K



MUON (ANTI)NEUTRINO DISAPPEARANCE RESULTS



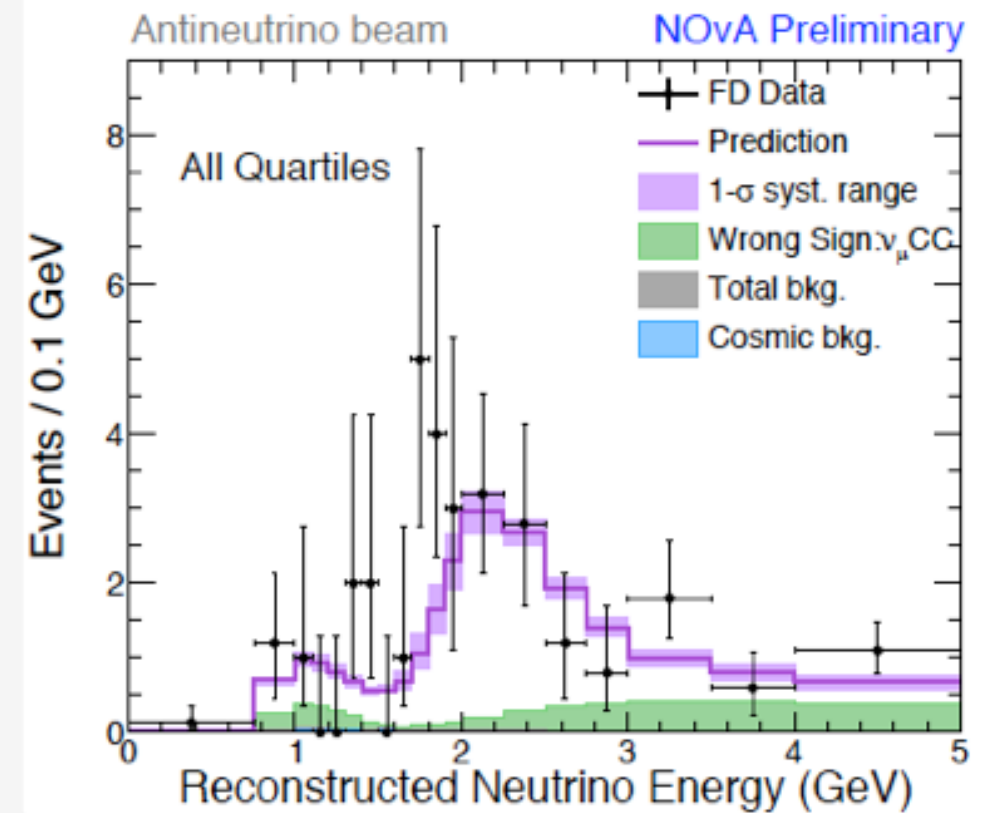
Observed	113
-----------------	------------

Best Fit Integral	121
-------------------	-----

Cosmic Background	2.1
-------------------	-----

Beam Background	1.2
-----------------	-----

Un-oscillated Prediction	730
--------------------------	-----



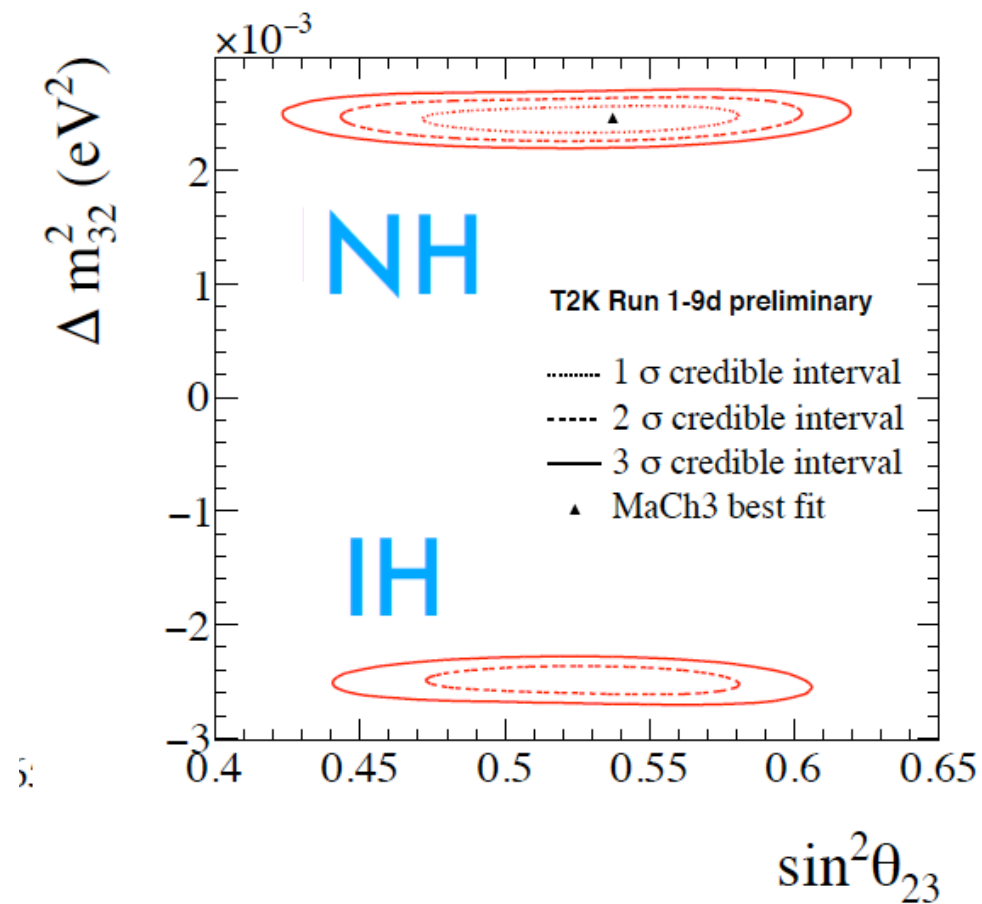
Observed	65
-----------------	-----------

Best Fit Integral	50
-------------------	----

Cosmic Background	0.5
-------------------	-----

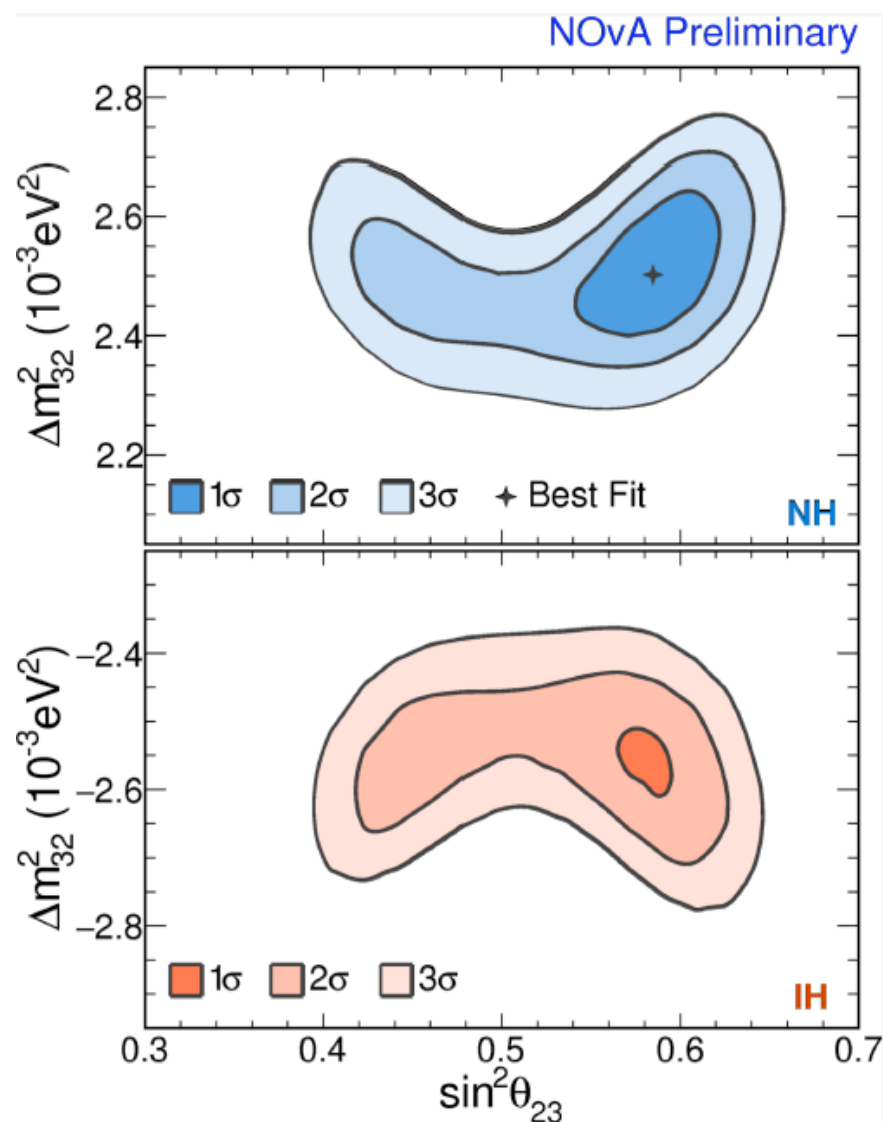
Beam Background	0.6
-----------------	-----

Un-oscillated Prediction	266
--------------------------	-----



T2K

- T2K prefers NH with a Bayes factor of 8.0, assuming an equal prior between NH and IH
- T2K is consistent with $\sin^2 \theta_{23} = 0.5$
- Best fit value of $\sin^2 \theta_{23} = 0.537$ (NH)
- Best fit value of $\Delta m_{32}^2 = 2.46 \times 10^{-3} \text{ eV}^2$ (NH)



NOvA

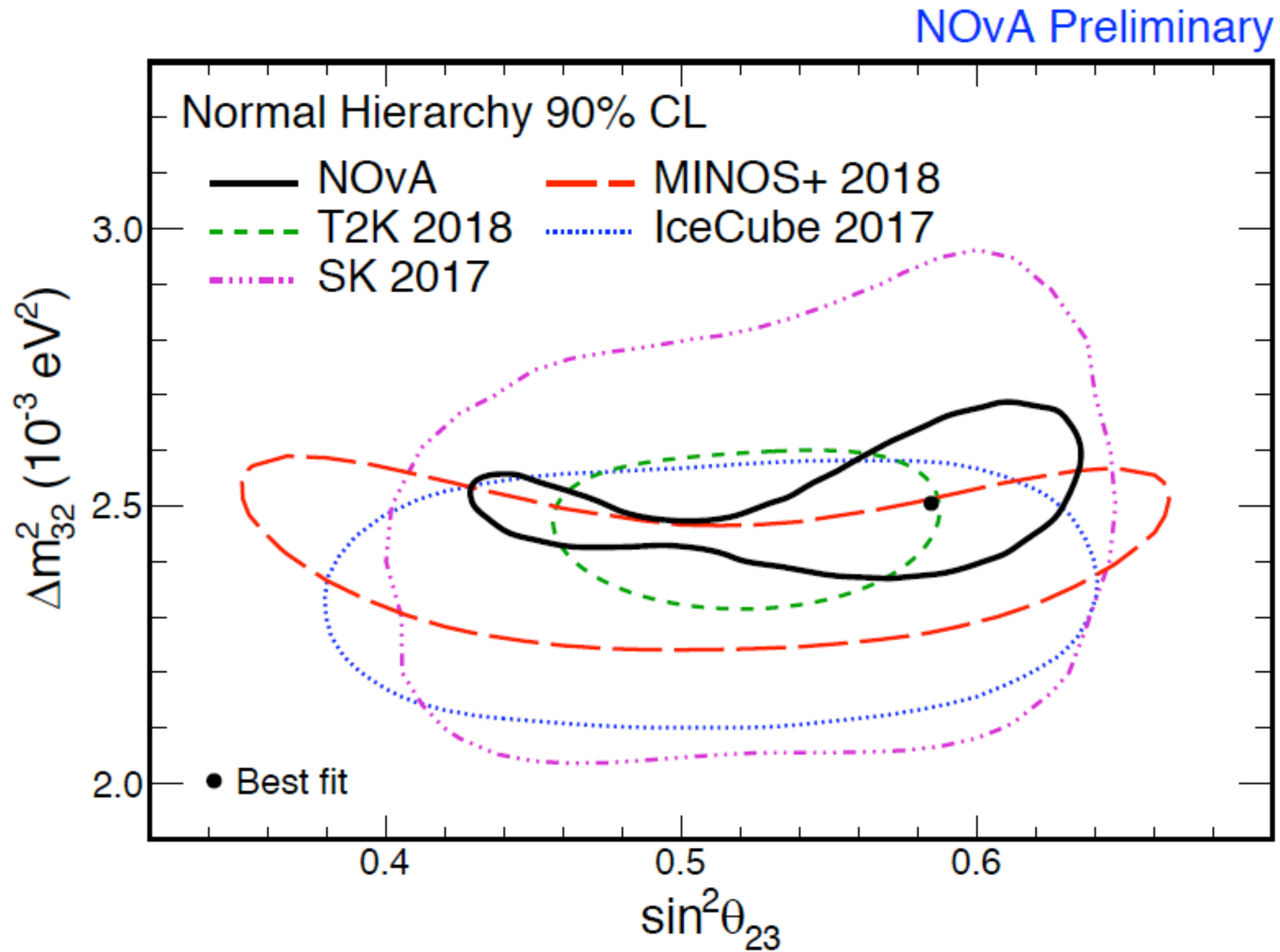
- Prefer non-maximal mixing at 1.8 σ .
- Favour upper octant at a similar level.

Best Fit

$$\Delta m_{32}^2 = 2.52^{+0.13}_{-0.18} \times 10^{-3} \text{ eV}^2 \text{ (NH)}$$

$$\sin^2 \theta_{23} = 0.58 \pm 0.03 \text{ (UO)}$$

- NOvA is consistent with other long baseline and atmospheric neutrino experiments.



Accelerator appearance experiment

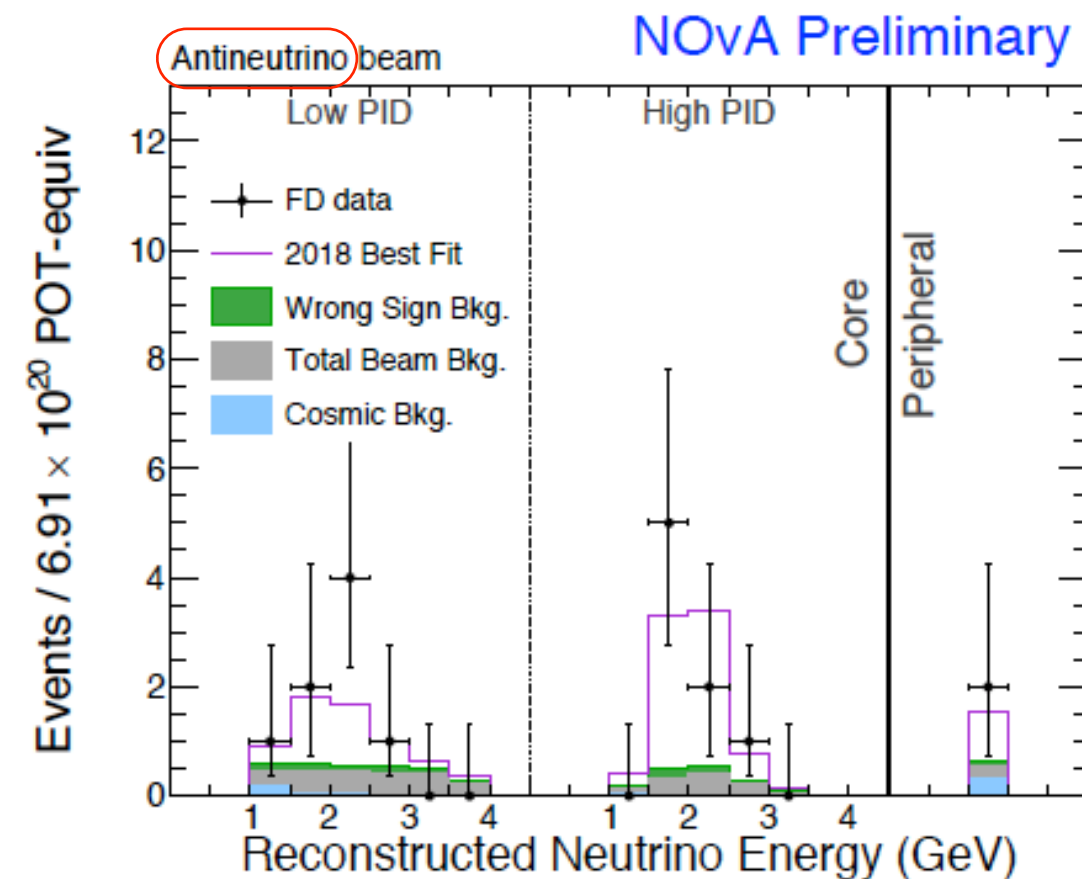
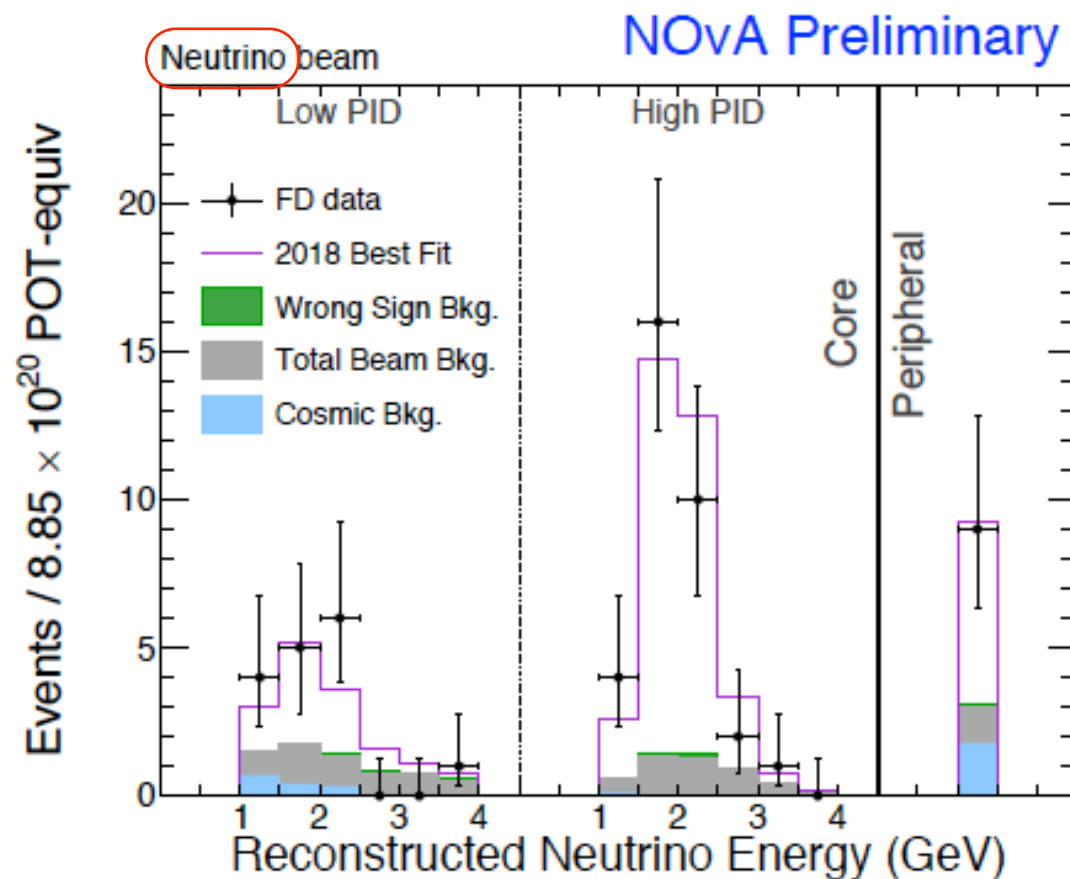
$$\begin{aligned}
P(\nu_\mu \rightarrow \nu_e) = & 4c_{13}^2 s_{13}^2 s_{23}^2 \sin^2 \Delta_{31} \\
& + 8c_{13}^2 s_{12} s_{13} s_{23} (c_{12} c_{23} \cos \delta - s_{12} s_{13} s_{23}) \cos \Delta_{32} \sin \Delta_{31} \sin \Delta_{21} \quad \text{CP non-violating} \\
& - 8c_{13}^2 c_{12} c_{23} s_{12} s_{13} s_{23} \sin \delta \sin \Delta_{32} \sin \Delta_{31} \sin \Delta_{21} \quad \text{CP violating} \\
& + 4s_{12}^2 c_{13}^2 (c_{12}^2 c_{23}^2 + s_{12}^2 s_{23}^2 s_{13}^2 - 2c_{12} c_{23} s_{12} s_{23} s_{13} \cos \delta) \sin^2 \Delta_{21} \quad \text{CP non-violating} \\
& - 8c_{13}^2 s_{13}^2 s_{23}^2 (1 - 2s_{13}^2) \frac{aL}{4E} \cos \Delta_{32} \sin \Delta_{31} \quad \text{matter effect}
\end{aligned}$$

MH

$$a = 2\sqrt{2}G_F N_e E \quad P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) \quad a \rightarrow -a, \delta \rightarrow -\delta$$

potential to measure $\left\{ \begin{array}{ll} \text{CP phase, } \delta & \\ \text{sign}(\theta_{23} - 45^\circ) & s_{23}^2 = \frac{1 \pm \sqrt{1 - \sin^2 2\theta_{23}}}{2} \\ \text{sign}(\Delta m_{31}^2) & \text{mass hierarchy} \end{array} \right.$

- *No chance to test CPV if it was $\theta_{13} = 0$ (it's small but not 0)*
- δ_{CP} never singled out, ambiguities remain and need to be solved with external inputs (e.g. reactor)
- Possible to test also w/o anti- ν , by fitting all parameters together instead of only δ_{CP} and a or a Δ_{ij} , but obviously less sensitive

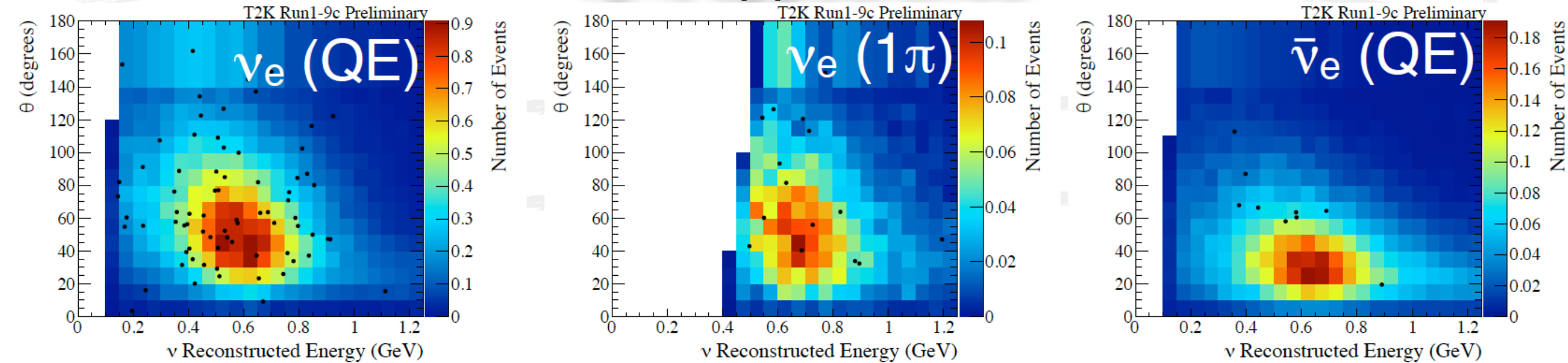


Observed	58
Best Fit Prediction	59
Cosmic Background	3.3
Beam Background	11.1
Wrong Sign Background	0.7

Observed	18
Best Fit Prediction	15.9
Cosmic Background	0.7
Beam Background	3.5
Wrong Sign Background	1.1

- Events are separated into two samples, based on imaging techniques
- Otherwise good events that pass either containment/cosmic rej are called “peripheral”

$\nu_e/\bar{\nu}_e$ appearance



Predictions with: $\sin^2\theta_{13}=0.0212$, $\sin^2\theta_{23}=0.528$, $\Delta m^2_{32}=2.51\times 10^{-3}$, NH

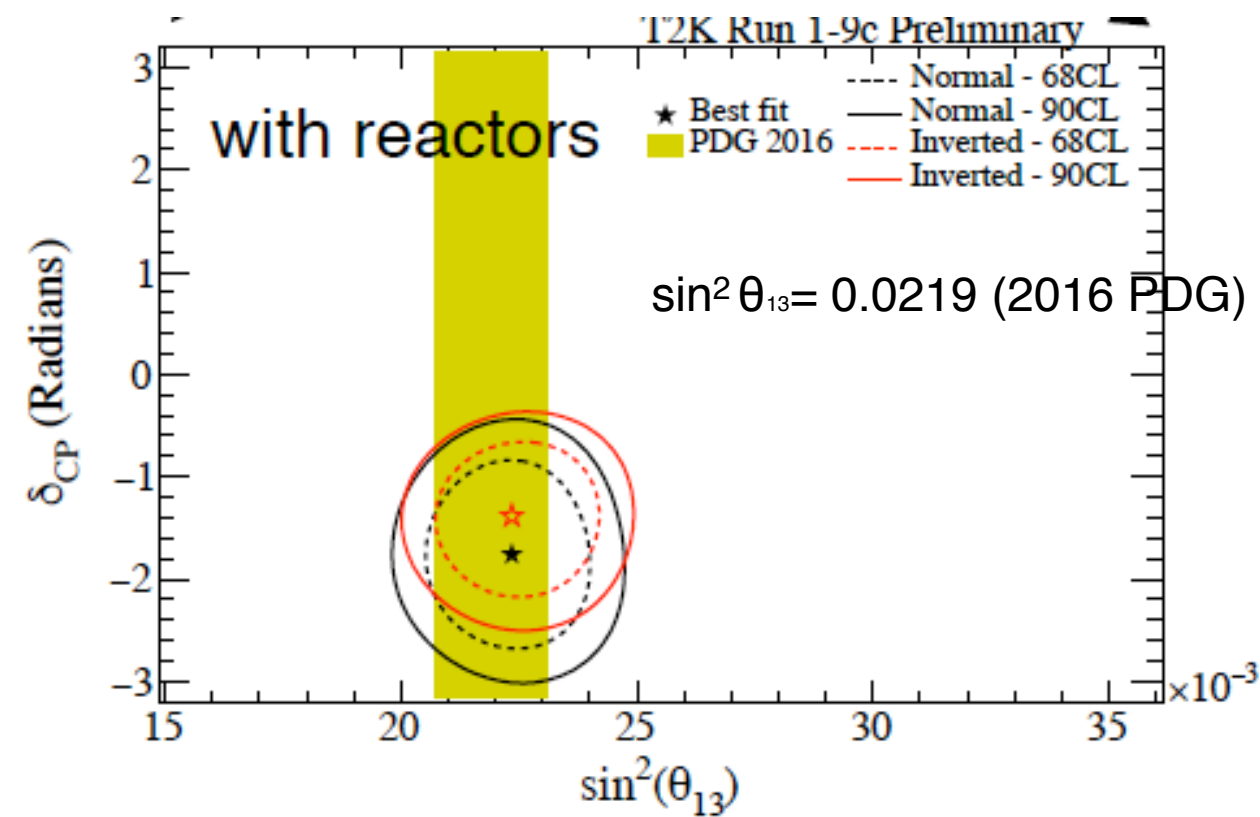
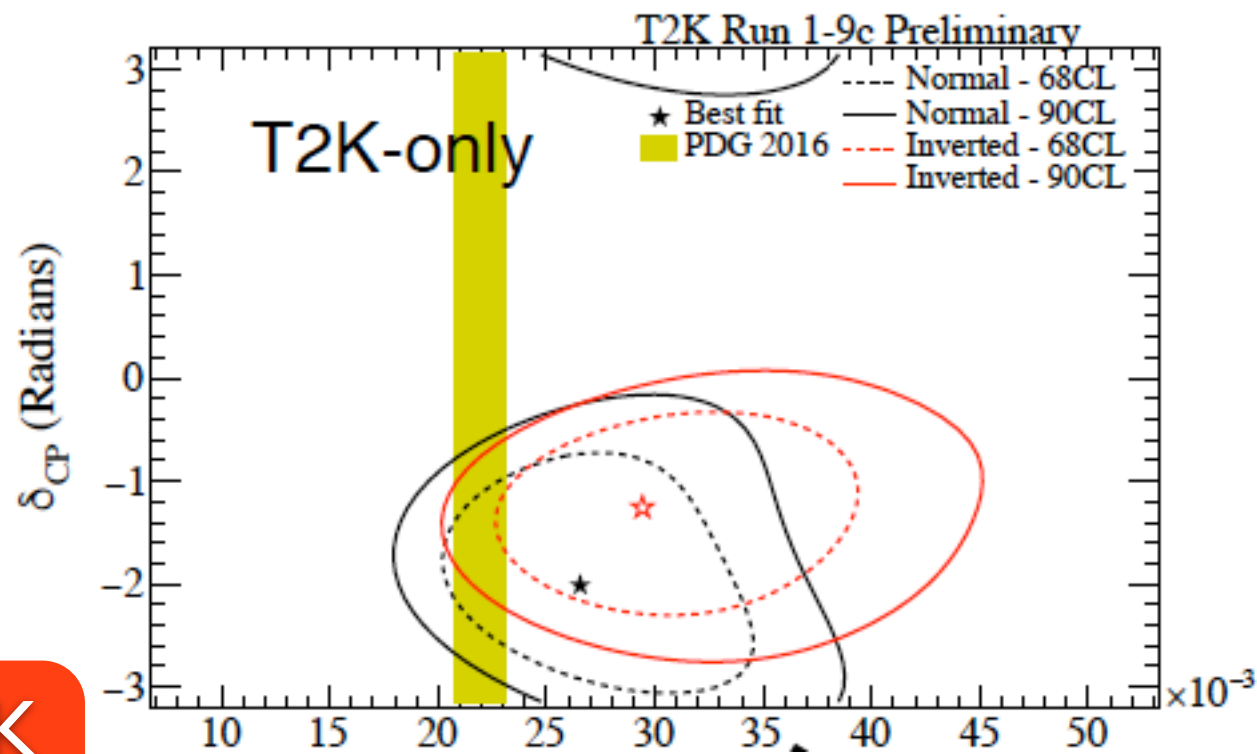
Sample	$\delta_{CP}=-\pi/2$	$\delta_{CP}=0$	$\delta_{CP}=\pi/2$	$\delta_{CP}=\pi$	Observed
nu	74.4	62.2	50.6	62.7	75
nu-bar	17.1	19.4	21.7	19.3	15
nu+ 1π	7.0	6.1	4.9	5.9	15

β	HYPOTHESIS	P-VALUE
$\beta=0$	NO appearance	$p=0.233$
$\beta=1$	PMNS appearance	$p=0.0867$

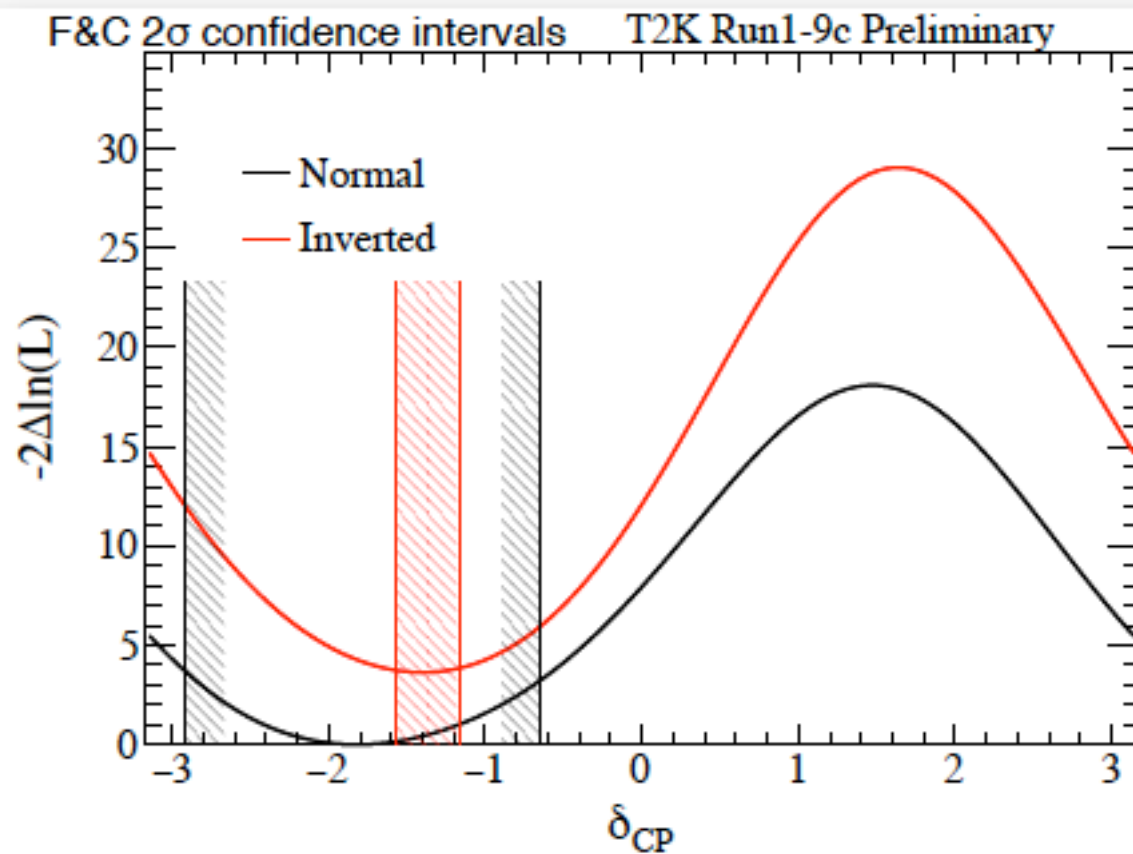
No sound statistical conclusions on ν_e -bar appearance yet

- SK event rates are in line with expectations based on oscillation model
- Of note: 15 events observed in CC 1π ν_e sample, with prediction of 6.9 maximum
 - p-value for up/down fluctuation in 1 of 5 samples is: $\sim 5\%$ (1% with single sample).

DATA FIT



DATA FIT with reactor constraint



δ_{CP}	Hierarchy	90%	2σ
0	NH	0.421	0.288
π	NH	0.388	0.248
0	IH	0.768	0.660
π	IH	0.783	0.685

JOINT FIT RESULTS

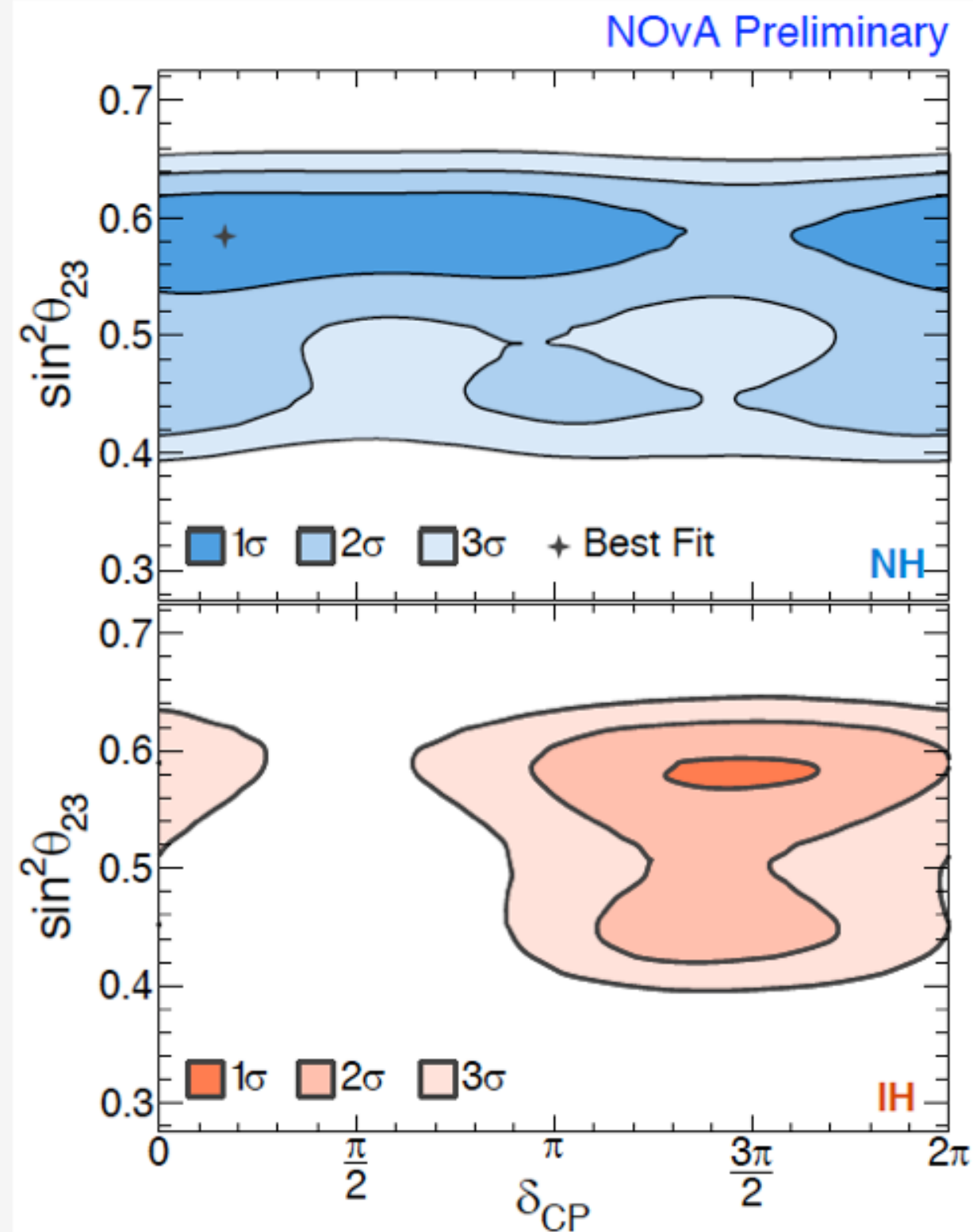
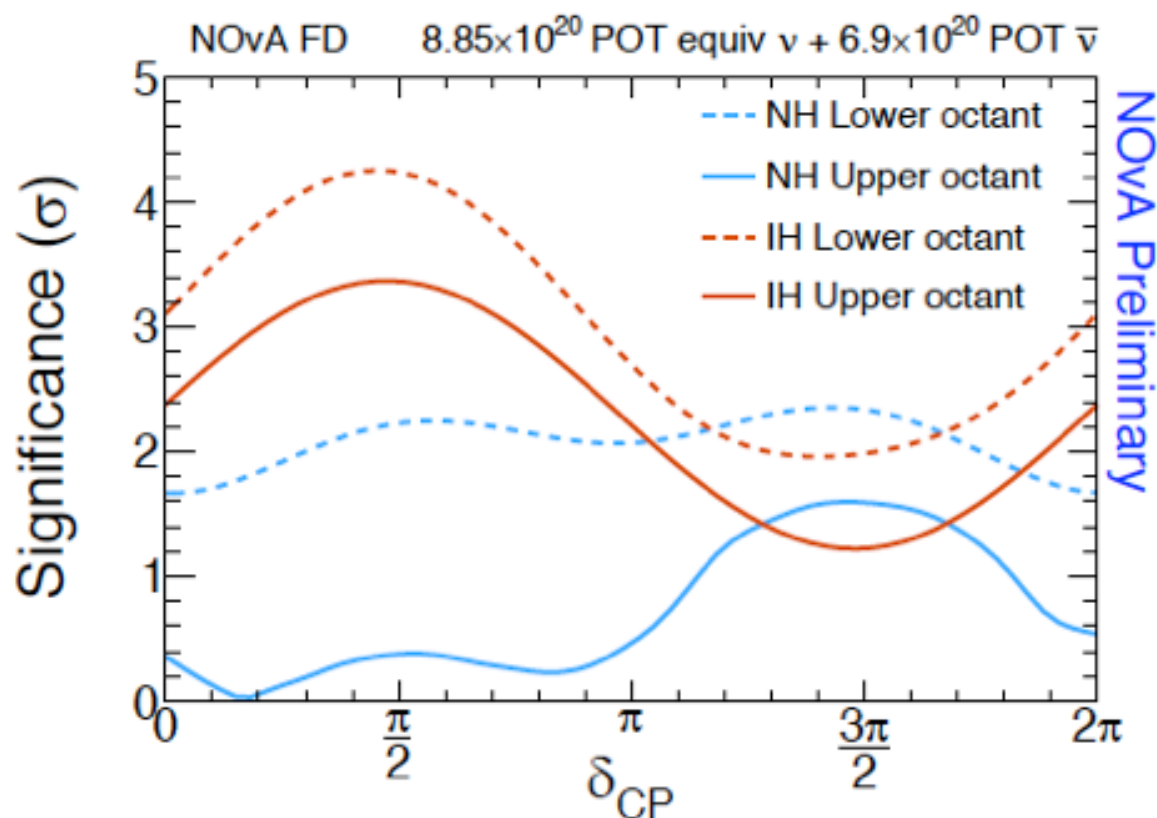
- Prefer NH by 1.8 σ .
- Exclude $\delta_{CP} = \pi/2$ for IH at $>3 \sigma$.

Best Fit

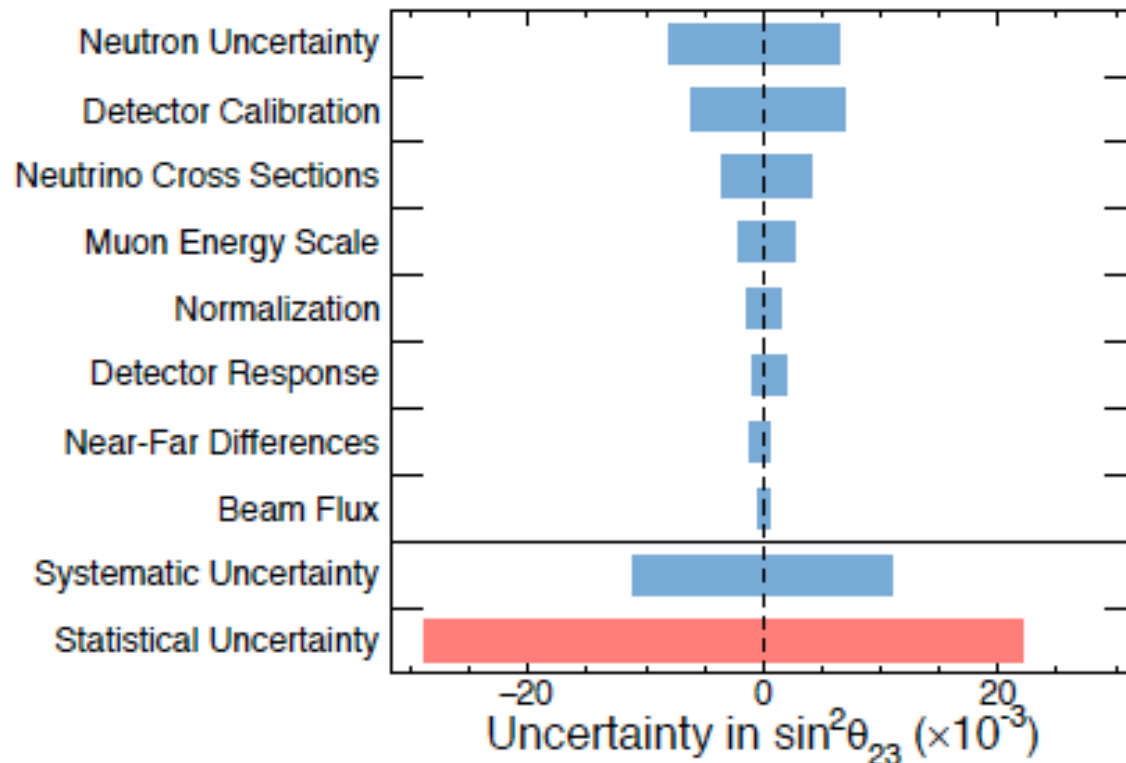
$$\delta_{CP} = 0.17\pi$$

$$\Delta m_{32}^2 = 2.52^{+0.13}_{-0.18} \times 10^{-3} \text{ eV}^2 \text{ (NH)}$$

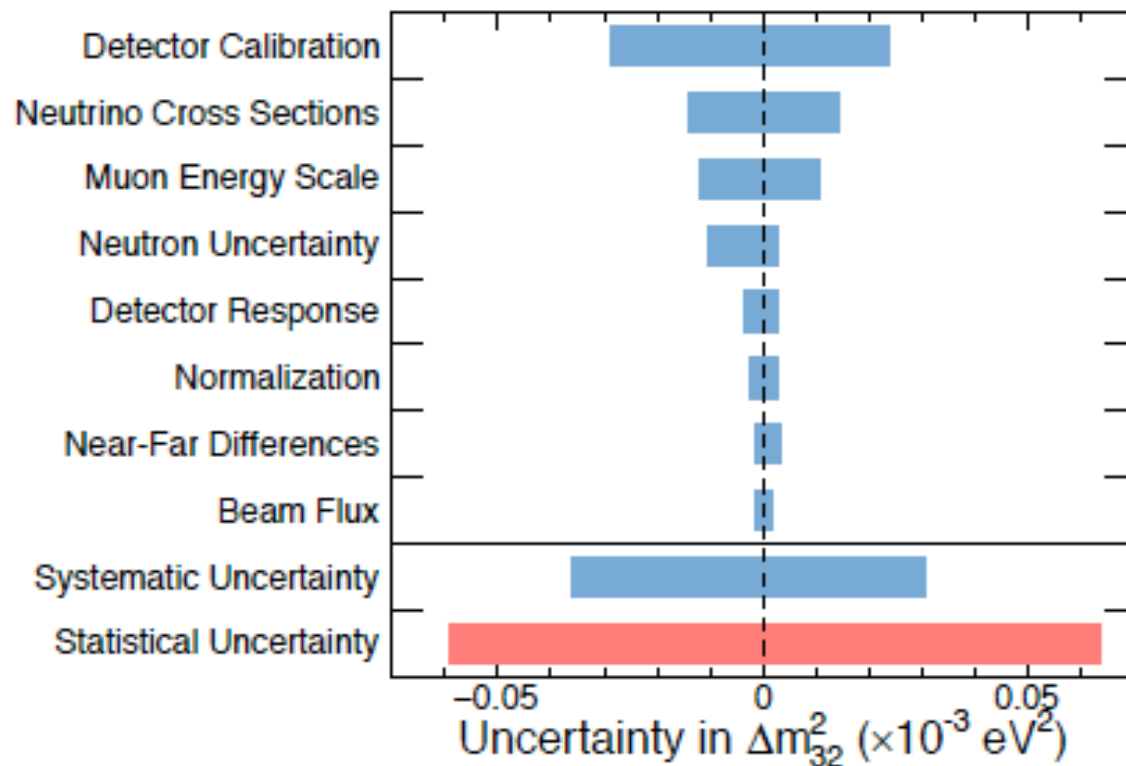
$$\sin^2 \theta_{23} = 0.58 \pm 0.03 \text{ (UO)}$$



NOvA Preliminary



NOvA Preliminary



Systematic uncertainties have been reduced in this analysis, however **analyses are still statistics limited**.

- The upcoming test beam program will improve the calibration and detector response systematics.
- Neutron uncertainty important (and new) for $\bar{\nu}$.
- Neutrino cross-sections (MEC,RPA) also important.

Both NOvA and T2K have extensive upgrade ahead for both ND and FD

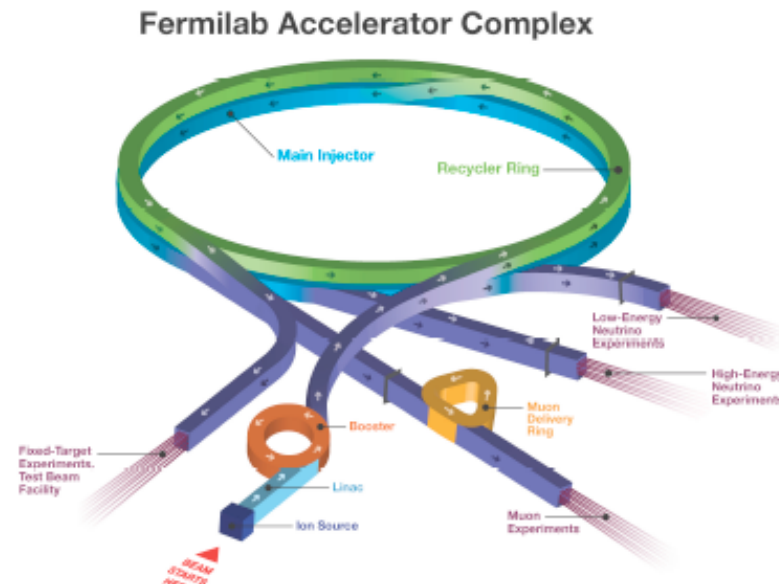
T2K: <https://zenodo.org/record/1286758#.XFwZyNF7mi4>

NOvA

Future LBL experiments

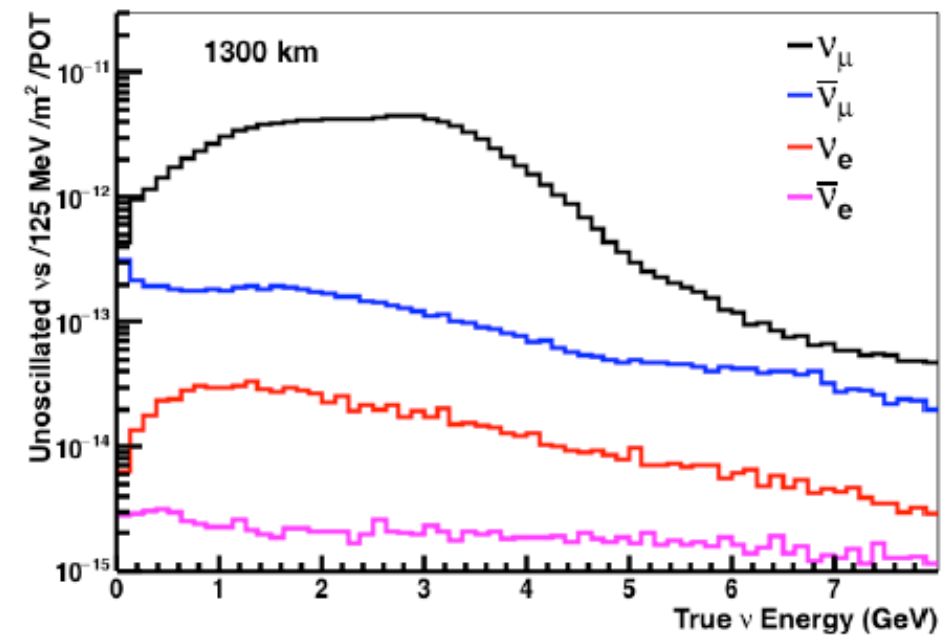
DUNE

LBNF Beam



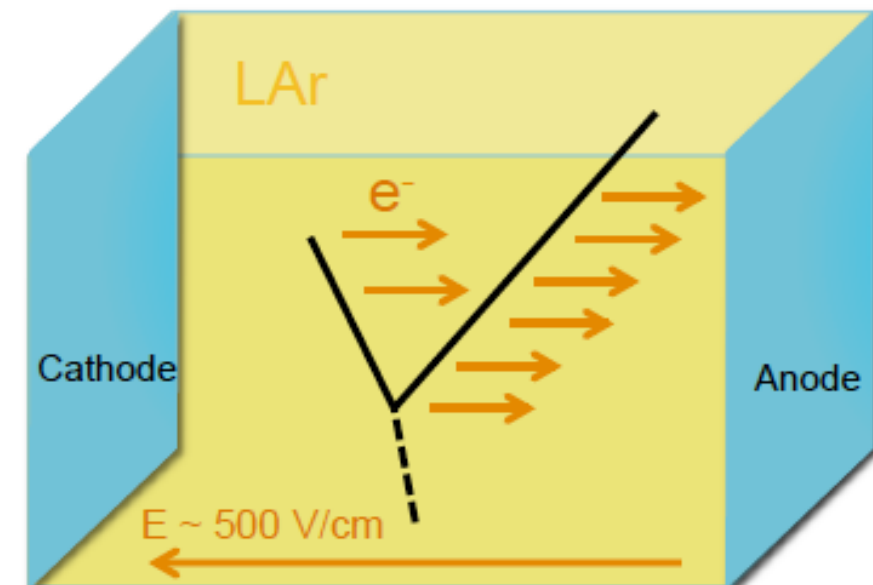
- 60-120 GeV proton beam

Neutrino Flux at 1300 km
(CDR Optimized Beam)

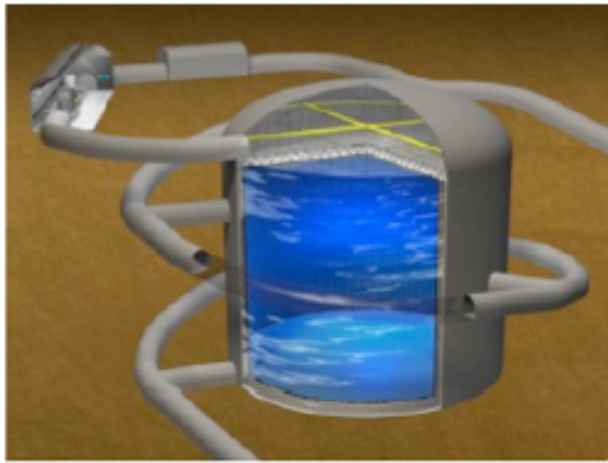


DUNE Far Detector

- 4 10-kt (fiducial) liquid argon TPC modules
- **Single-** and dual-phase detector designs (1st module will be single phase)
- Integrated photon detection
- Modules will not be identical



Hyper-Kamiokande



Hyper-K



J-PARC
Accelerator Complex



- ✓ Gigantic neutrino and nucleon decay detector
 - ✓ 186 kton fiducial mass : $\sim 10 \times$ Super-K
 - ✓ $\times 2$ higher photon sensitivity than Super-K
 - ✓ Superb detector capability, technology still evolving
 - ✓ 2nd oscillation maximum by 2nd tank in Korea under study
- ✓ MW-class world-leading ν -beam by upgraded J-PARC
- ✓ Project now is a priority project by MEXT's Roadmap
 - ✓ Aiming to start construction in FY2019, operation in FY2026

Future experiments/DUNE

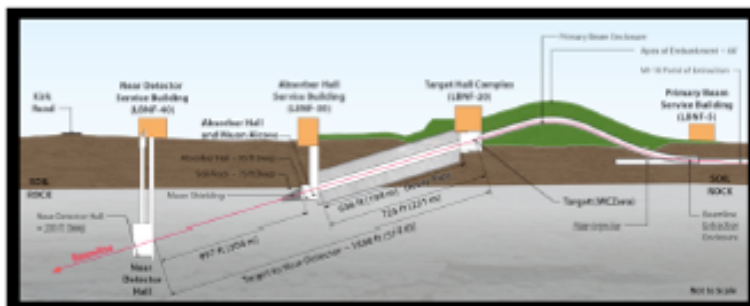
DEEP UNDERGROUND NEUTRINO EXPERIMENT

Timeline



Physics data as soon as 1st module complete

- Atmospheric vs
- SNB and solar vs
- Baryon number violation
- Detector calibration



2018: protoDUNEs at CERN



2019: Technical Design Report



2019: Far Site Primary Excavation Begins

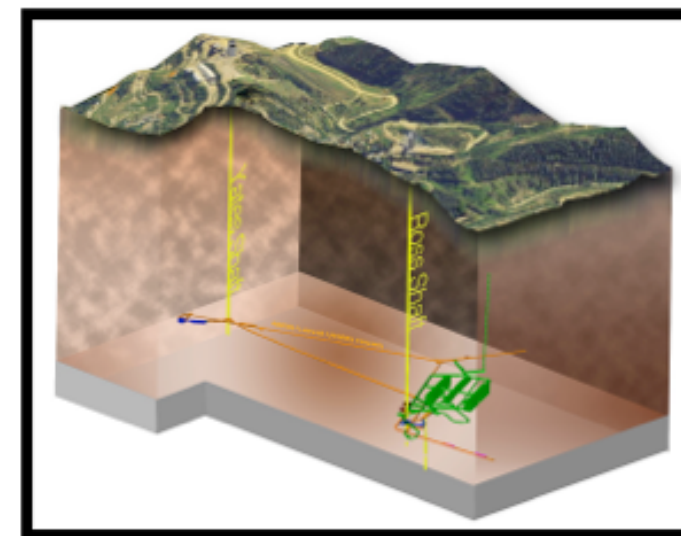


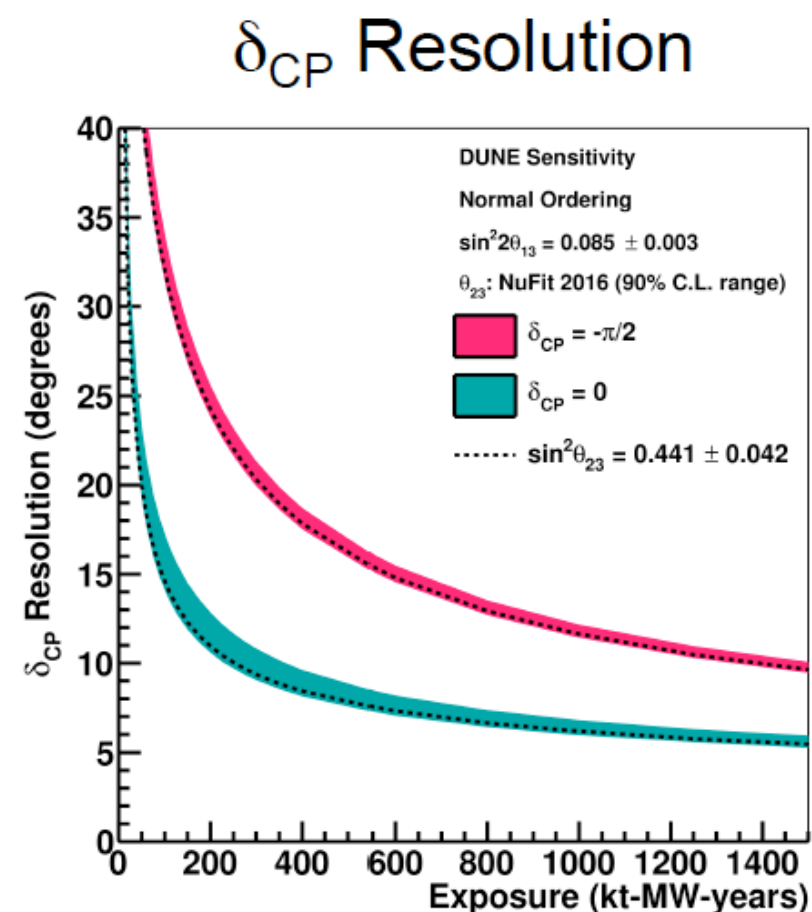
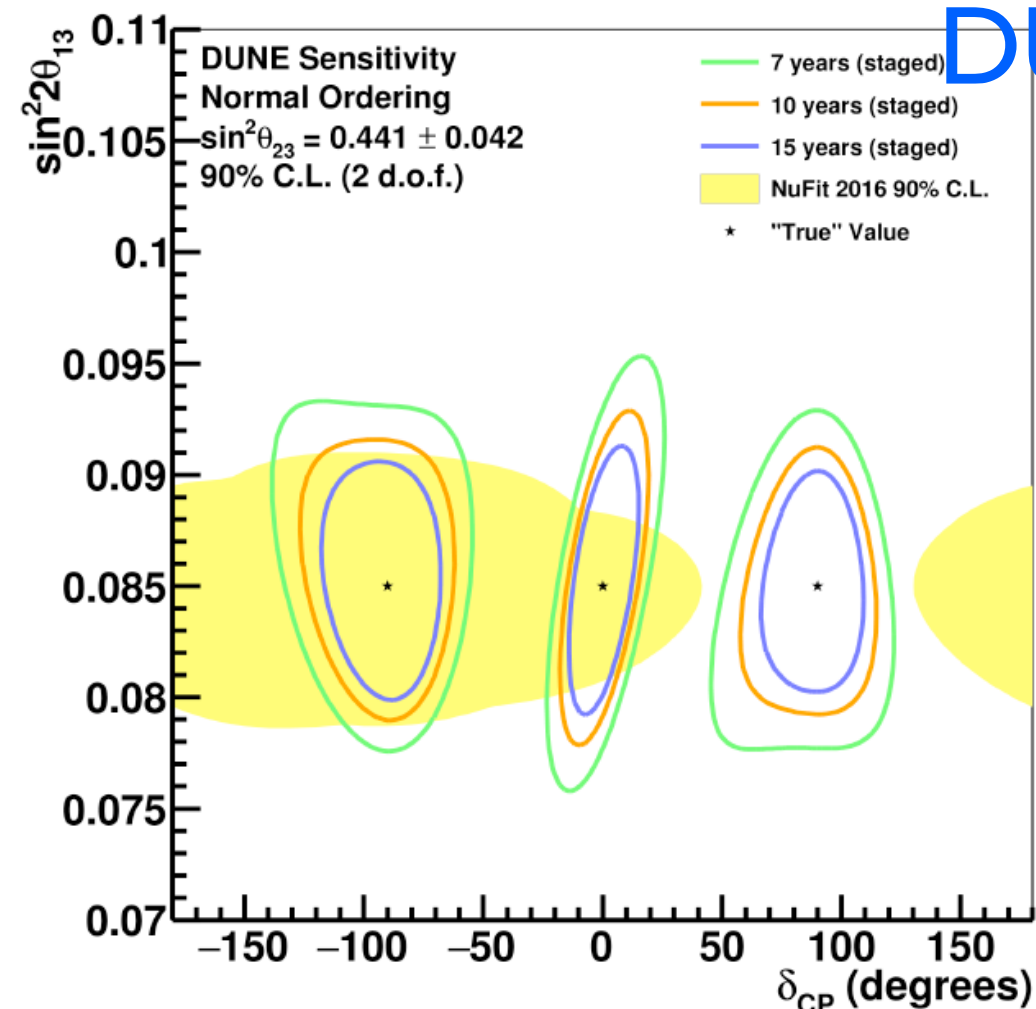
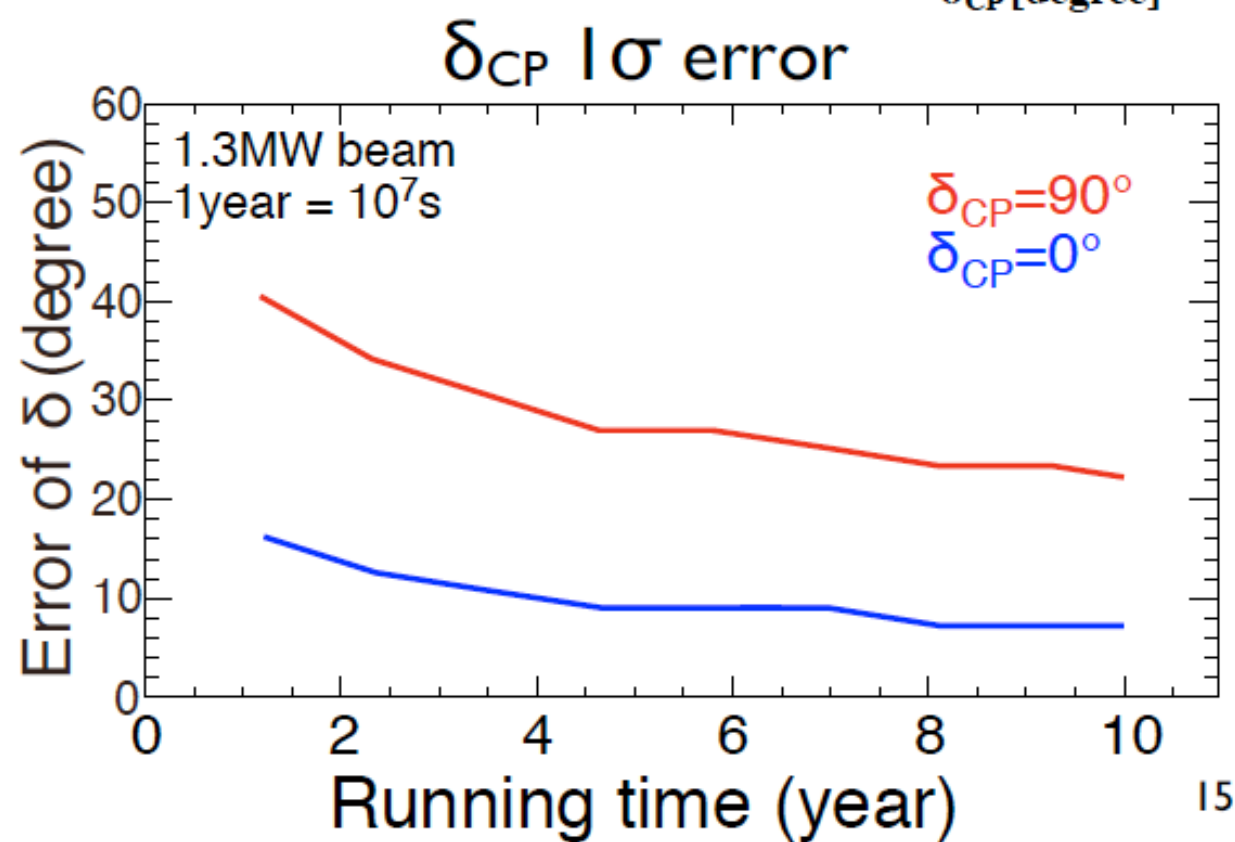
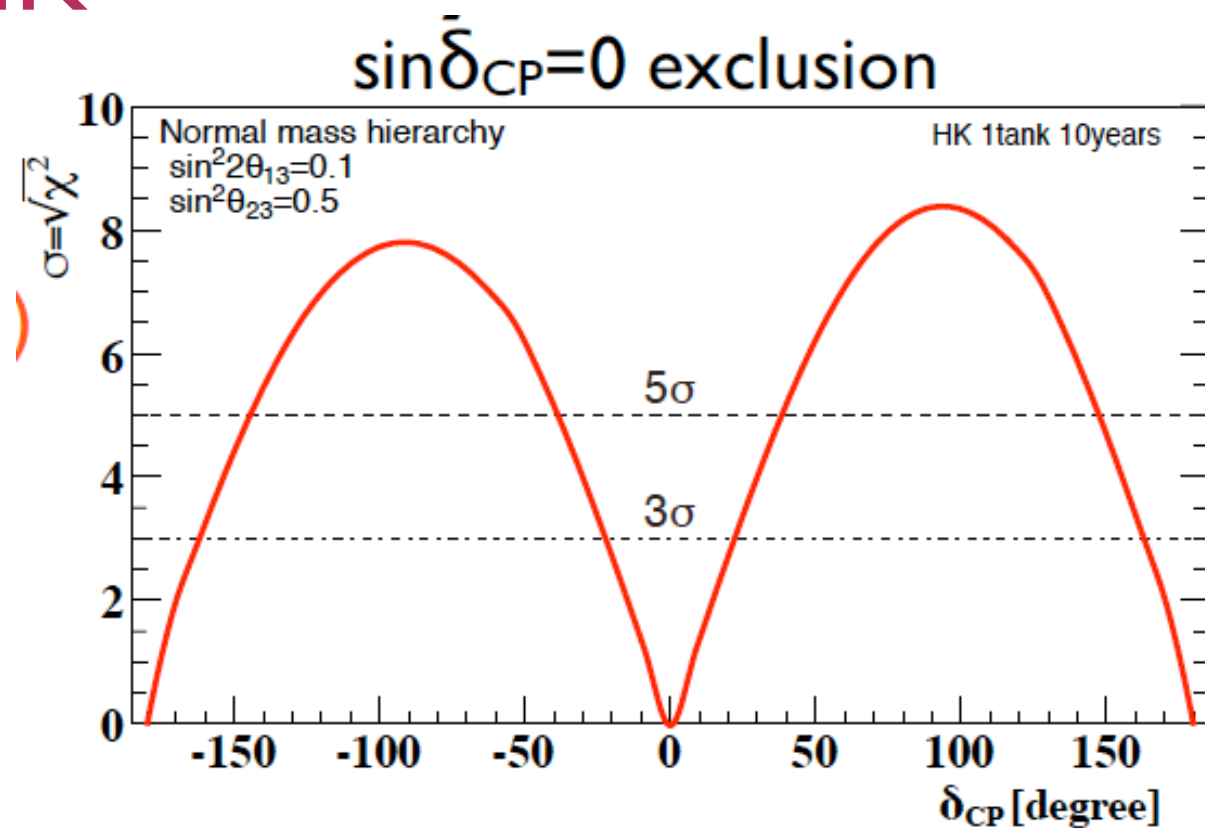
2022: First Module Installation Begins



2026: Neutrino Beam Available

DUNE Far Detector Interim Design Report (2018)
Will be made public soon...





Additional material

Matter effect, MSW

2-flavour, vacuum:

$$i \frac{d}{dt} \begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} = M_V \begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} = \left[\frac{m_1^2 + m_2^2}{4p} \right] \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} + \left(\frac{\Delta m^2}{4p} \right) \begin{pmatrix} -\cos 2\theta & \sin 2\theta \\ \sin 2\theta & \cos 2\theta \end{pmatrix} \begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix}$$

In ordinary matter (e.g. sun or earth) an additional interaction of ν_e with $\mathbf{e}$ occurs, with potential:

$$V_e = G_F \sqrt{2} N_e$$

$$m^2 = E^2 - p^2 \rightarrow (E + V_e)^2 - p^2 = m^2 + 2EV_e$$

$$\Delta m_{(e)}^2 = 2\sqrt{2}G_F N_e E$$

N_e = electron density

$$\left\{ \frac{1}{2} (m_1^2 + m_2^2) \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} + 2\sqrt{2}G_F N_e p \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix} \right\} = \left[\frac{1}{2} (m_1^2 + m_2^2) + \sqrt{2}G_F N_e p \right] \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} + \sqrt{2}G_F N_e p \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$$

Therefore, time evolution of 2-flavour, in matter:

$$A' = 2\sqrt{2}G_F N_e p / \Delta m^2$$

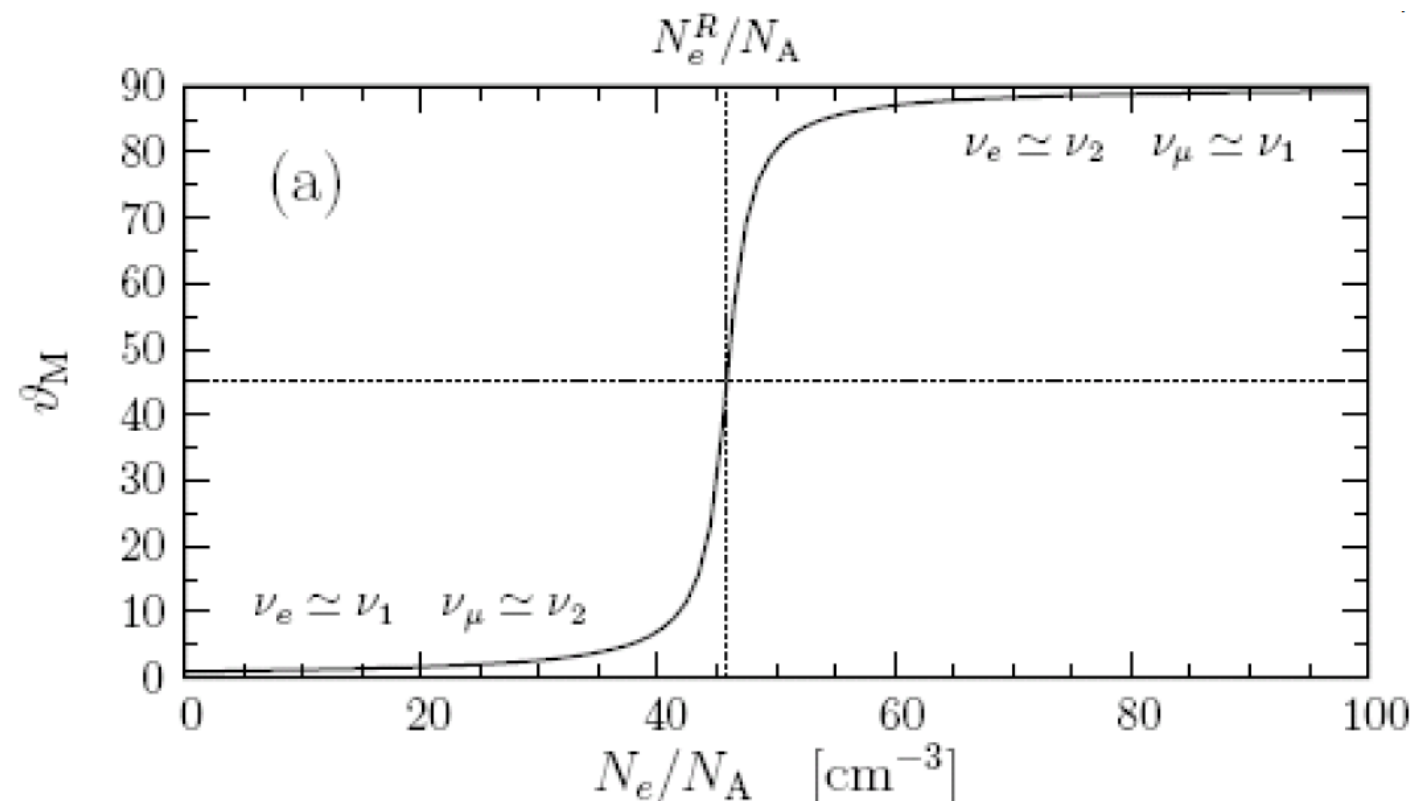
$$i \frac{d}{dt} \begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} = M_m \begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} = \left[\frac{(m_1^2 + m_2^2)}{4p} + \frac{\sqrt{2}G_F N_e p}{2} \right] \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} + \left[\frac{\Delta m^2}{4p} \begin{pmatrix} -\cos 2\theta + A' & \sin 2\theta \\ \sin 2\theta & \cos 2\theta - A' \end{pmatrix} \right] \begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix}$$

$$\boxed{M_m} \left[\frac{\Delta m_m^2}{4p} \begin{pmatrix} -\cos 2\theta_m & \sin 2\theta_m \\ \sin 2\theta_m & \cos 2\theta_m \end{pmatrix} \right] \begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} \longrightarrow \tan 2\theta_m = \frac{\sin 2\theta}{\cos 2\theta - A'} = \frac{\tan 2\theta}{1 - \frac{A'}{\cos 2\theta}}$$

- Effectively this translates into a “revised” mixing angle
- But with a resonance effect, when $A' = \cos 2\vartheta$ (ϑ =mixing angle in vacuum)
- i.e. an electron density

$$N_e(ris) = \Delta m^2 \frac{\cos 2\theta}{2\sqrt{2}G_F p}$$

- Correspondingly, new mass difference: $\Delta m_m^2 = \Delta m^2 \sqrt{(\cos 2\theta - A')^2 + \sin^2 2\theta}$



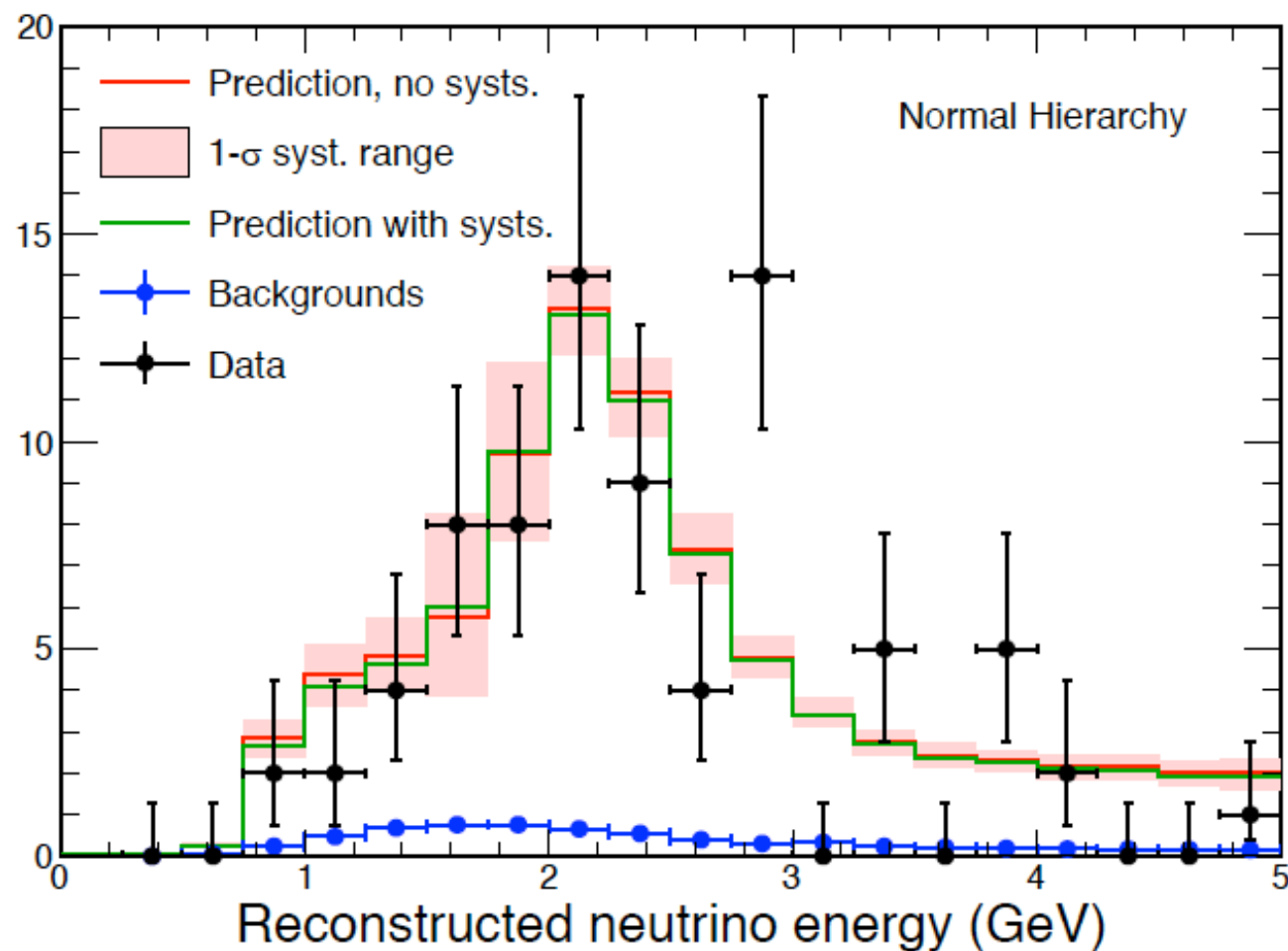
Evolution in the case of slow change of matter density along the neutrino path

Systematics

	% errors on predicted event rates				
	1R μ -like		1R e-like		
	ν -mode	$\bar{\nu}$ -mode	ν -mode	ν -mode (+1 π)	$\bar{\nu}$ -mode
SK detector	1.9 %	1.5%	3.0%	16.7%	4.2%
SK FSI+SI+PN	2.2%	2.0%	3.0%	11.4%	2.3%
ND constraint (flux & cross-section)	3.2%	2.7%	3.2%	4.1%	2.9%
$\sigma(\nu_e)/\sigma(\nu_\mu)$	<0.05 %	<0.05 %	2.6%	2.6%	1.5%
Neutral currents	0.3%	0.3%	1.1%	1.0%	2.6%
Total	4.4%	3.8%	6.1%	20.9%	6.5%

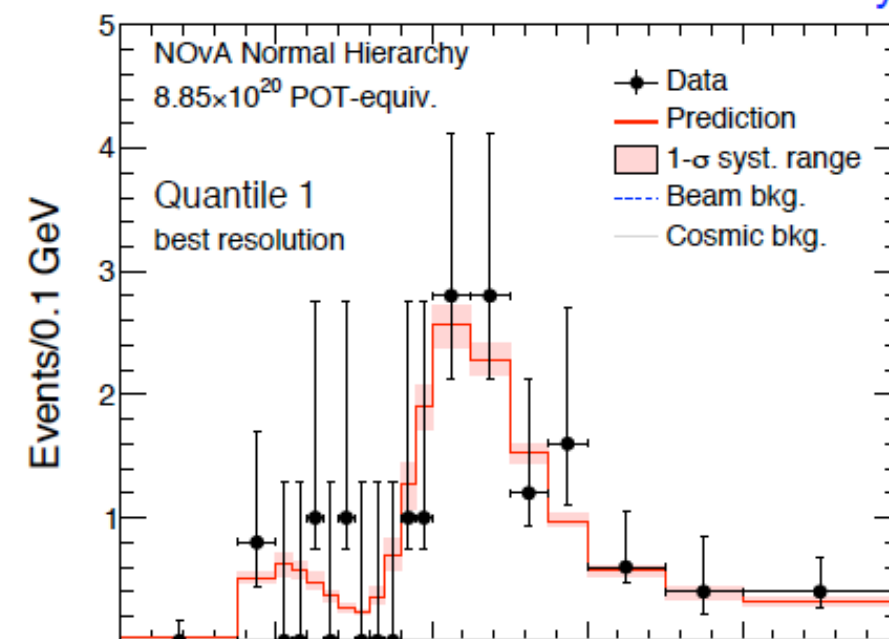
- ▶ **Uncertainties between 4% and 7% (except e-like+1 π $\rightarrow$ small stat.)**
- ▶ **Contributions from flux and cross-section constrained by ND280**
- ▶ **SK detector and FSI+SI uncertainties (not constrained by ND280)**
- ▶ **Only use ν_μ selection at ND280 $\rightarrow$ uncertainties due to possible ν_e/ν_μ cross-section (theoretical uncertainties)**

Events / 0.25 GeV

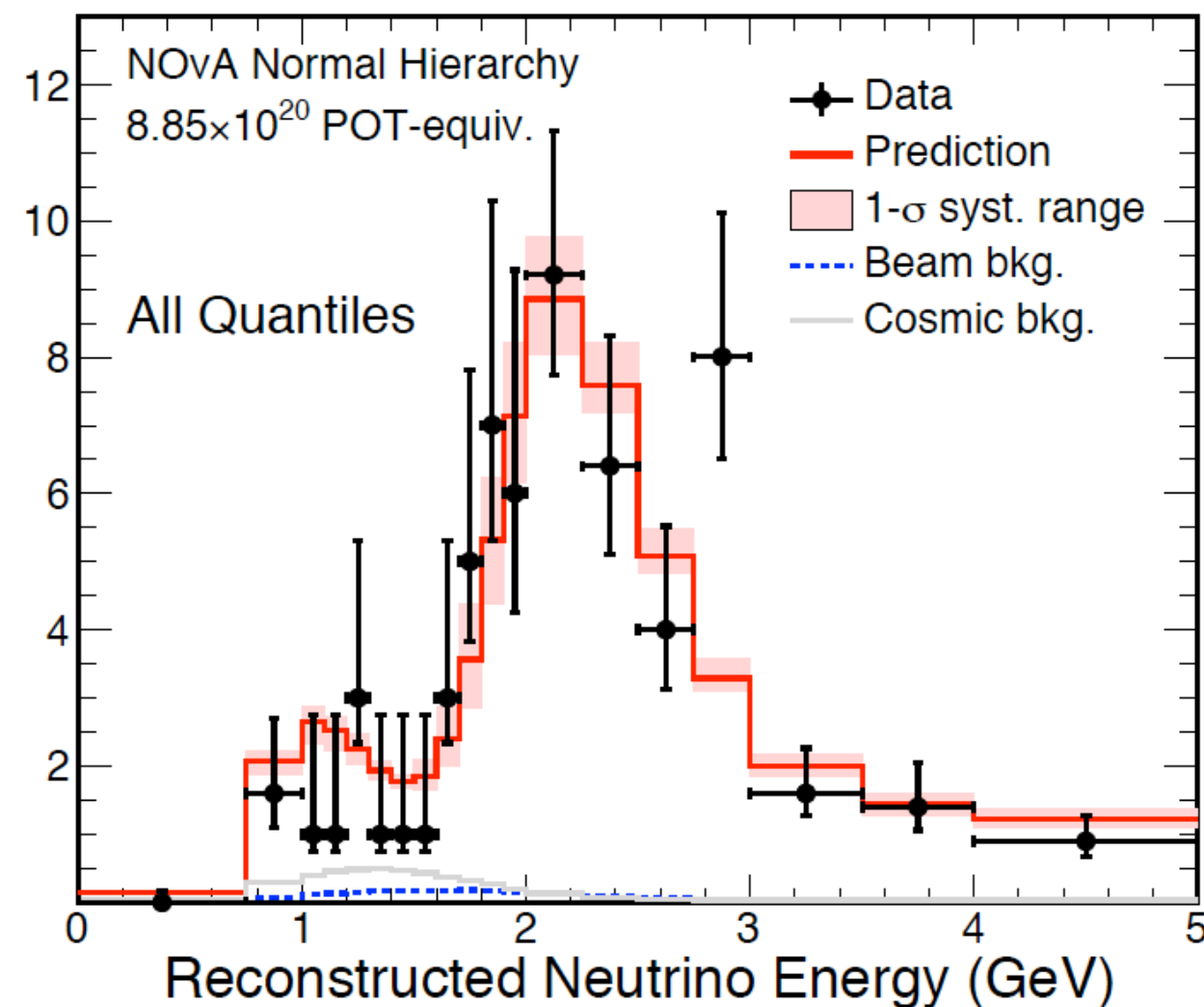


Quantile with best resolution

NOvA Preliminary



Events/0.1 GeV



Off-axis neutrino beam

[arXiv:1005.0574v2](#) [hep-ex]

- In the charged pion decay the neutrino in the CM frame has $E^*=29.8\text{MeV}$
- In the LAB frame:

$$\begin{aligned}E &= \gamma E^*(1 + \beta \cos \theta^*) \\E \cos \theta &= \gamma E^*(\cos \theta^* + \beta) \\E \sin \theta &= E^* \sin \theta^*\end{aligned}$$

$$\begin{aligned}\cos \theta &= \frac{\cos \theta^* + \beta}{1 + \beta \cos \theta^*} \\ \sin \theta &= \frac{\sin \theta^*}{\gamma(1 + \beta \cos \theta^*)}\end{aligned}$$

$$\theta_{\max}(E) = \arcsin \frac{E^*}{E} \approx \frac{30 \text{ MeV}}{E}$$

$$\sin \theta \leq \frac{E^*}{E}$$

For each given angle in the LAB there is a maximum neutrino energy

$$E_{\max}(\theta) = \frac{E^*}{\sin \theta}$$

ν_e Near Detector Data

- Select ν_e CC interactions with 73% efficiency and 76% purity
- Use ND data to predict background in FD
 - NC, CC, beam ν_e each propagate differently
 - constrain beam ν_e using selected ν_μ CC spectrum
 - constrain ν_μ CC using Michel Electron distribution

beam ν_e up by 4%
 NC up by 17%
 ν_μ CC up by 10%

